

A Bayesian Inversion of Spatial Autocorrelation (SPAC) for Vs30

Hao Zhang, Kristine Pankow

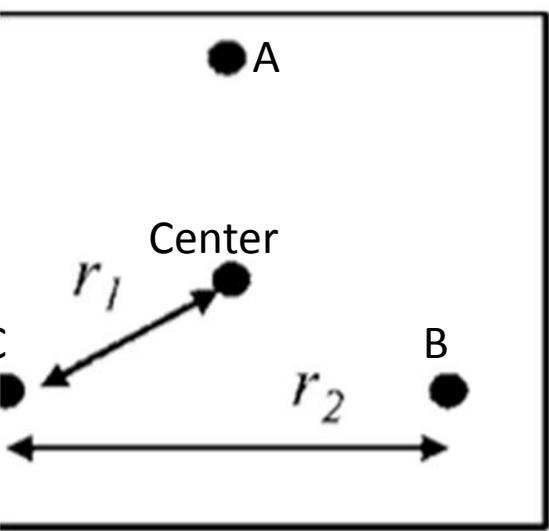
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February 13, 2018

Spatial Autocorrelation (SPAC)

Theoretical:

$$c(f) = \frac{1}{2\pi} \int_0^{2\pi} \exp\{irk \cos(\theta - \phi)\} d\theta$$
$$= J_0(rk) = J_0\left(\frac{2\pi fr}{v(f)}\right),$$



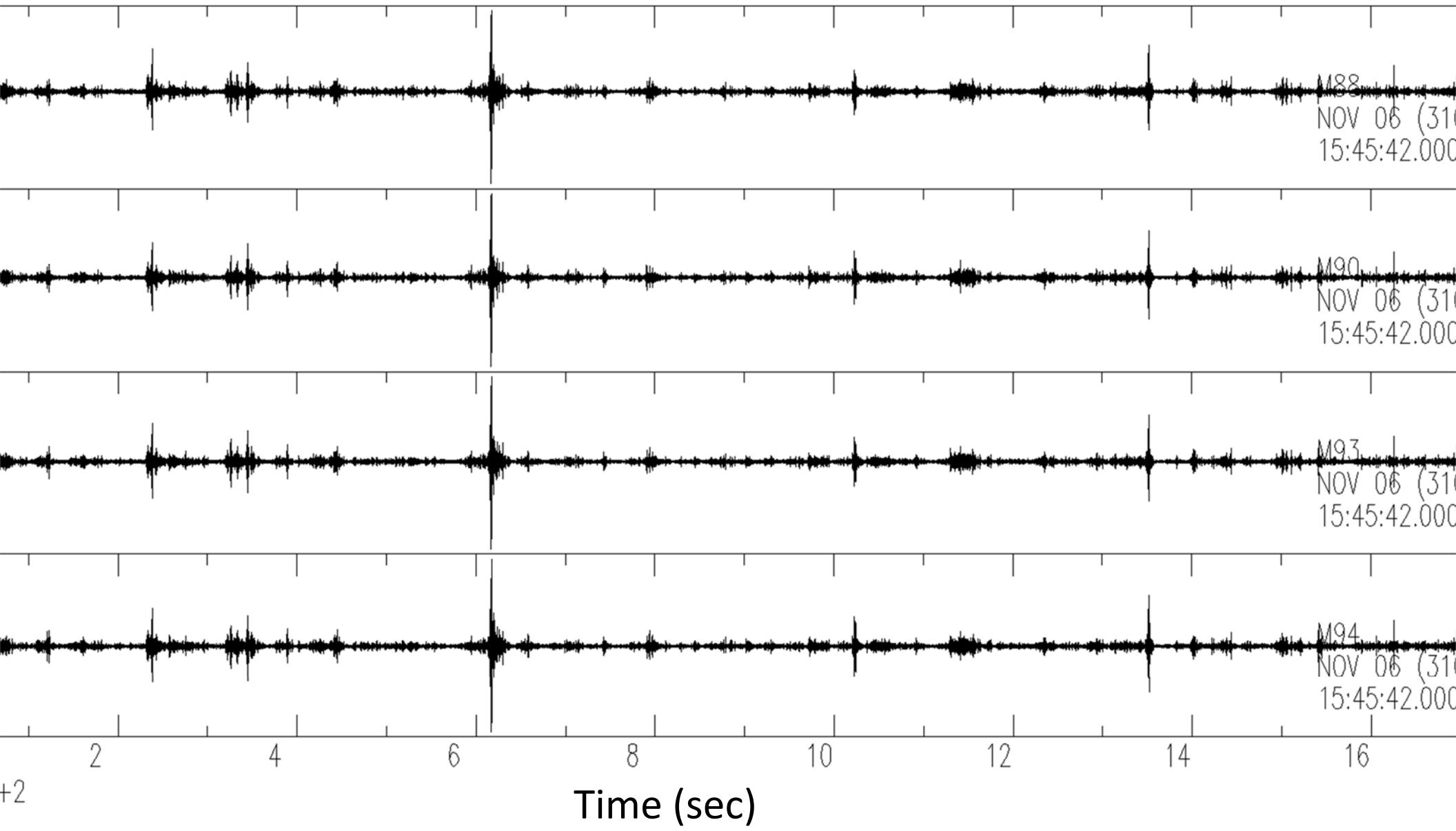
Observation:

$$c(f) = \frac{1}{2\pi} \int_0^{2\pi} \frac{C(f, r, \theta)}{\sqrt{P(f, 0)P(f, \theta)}} d\theta$$
$$= \frac{1}{N} \sum_{i=1}^N \frac{C(f, 0, r_i)}{\sqrt{C(f, 0, 0)C(f, r_i, r_i)}}$$

0: the average shear velocity of
the layer within the top 30 meters

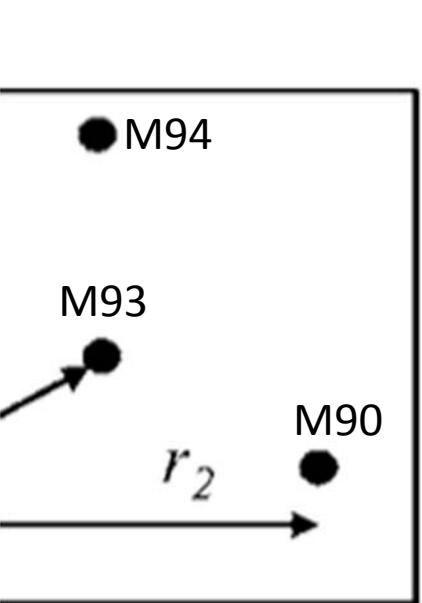
(Aki, 1957; Okada,

Data

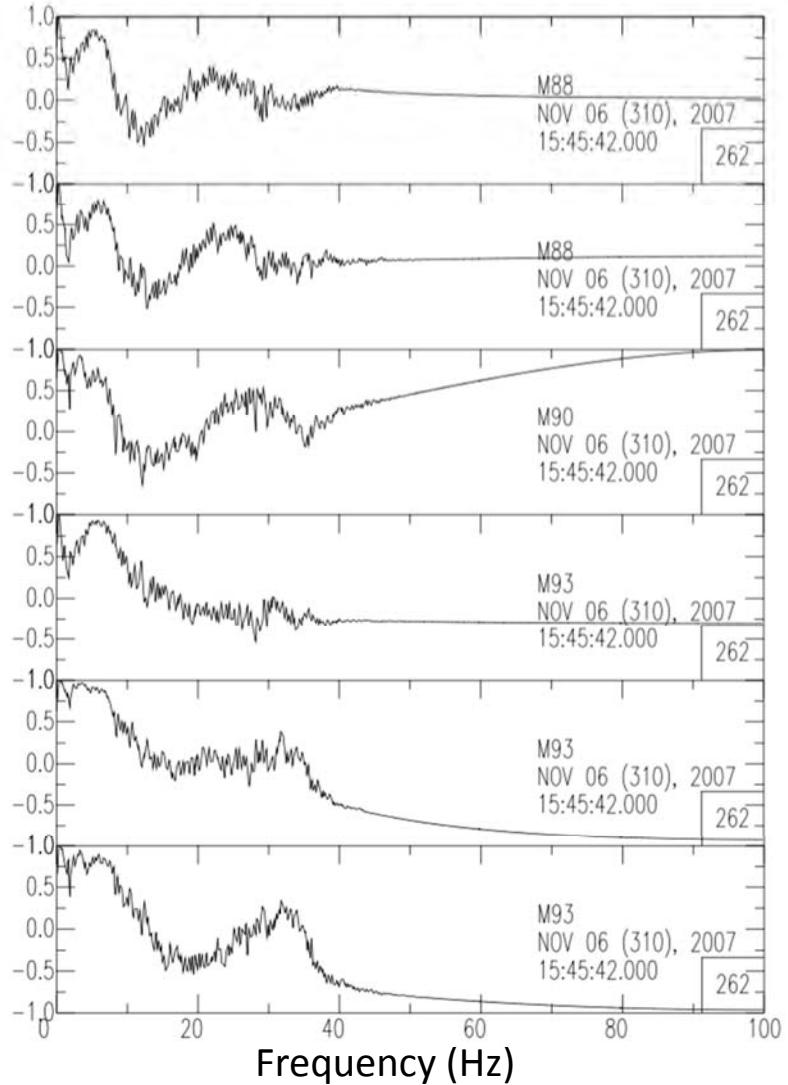


Coherency function for each station pair

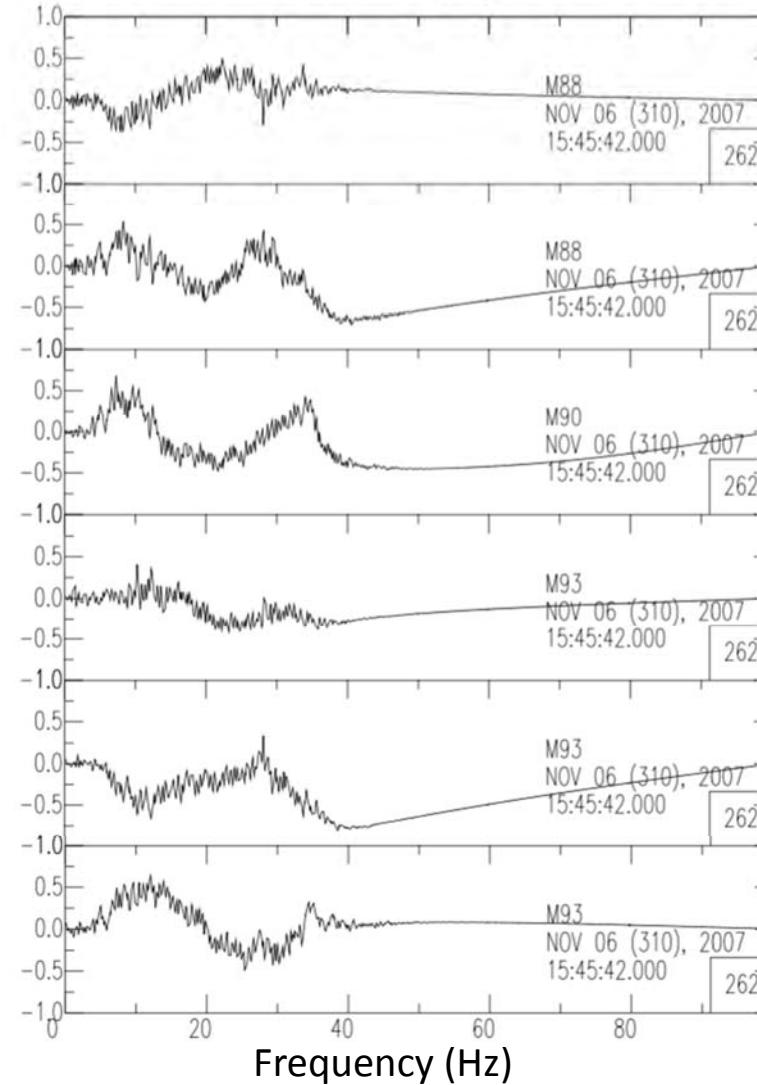
cohM88_M90_rl.sm cohM88_M94_rl.sm cohM90_M94_rl.sm cohM93_M88_rl.sm cohM93_M90_rl.sm cohM93_M94_rl.



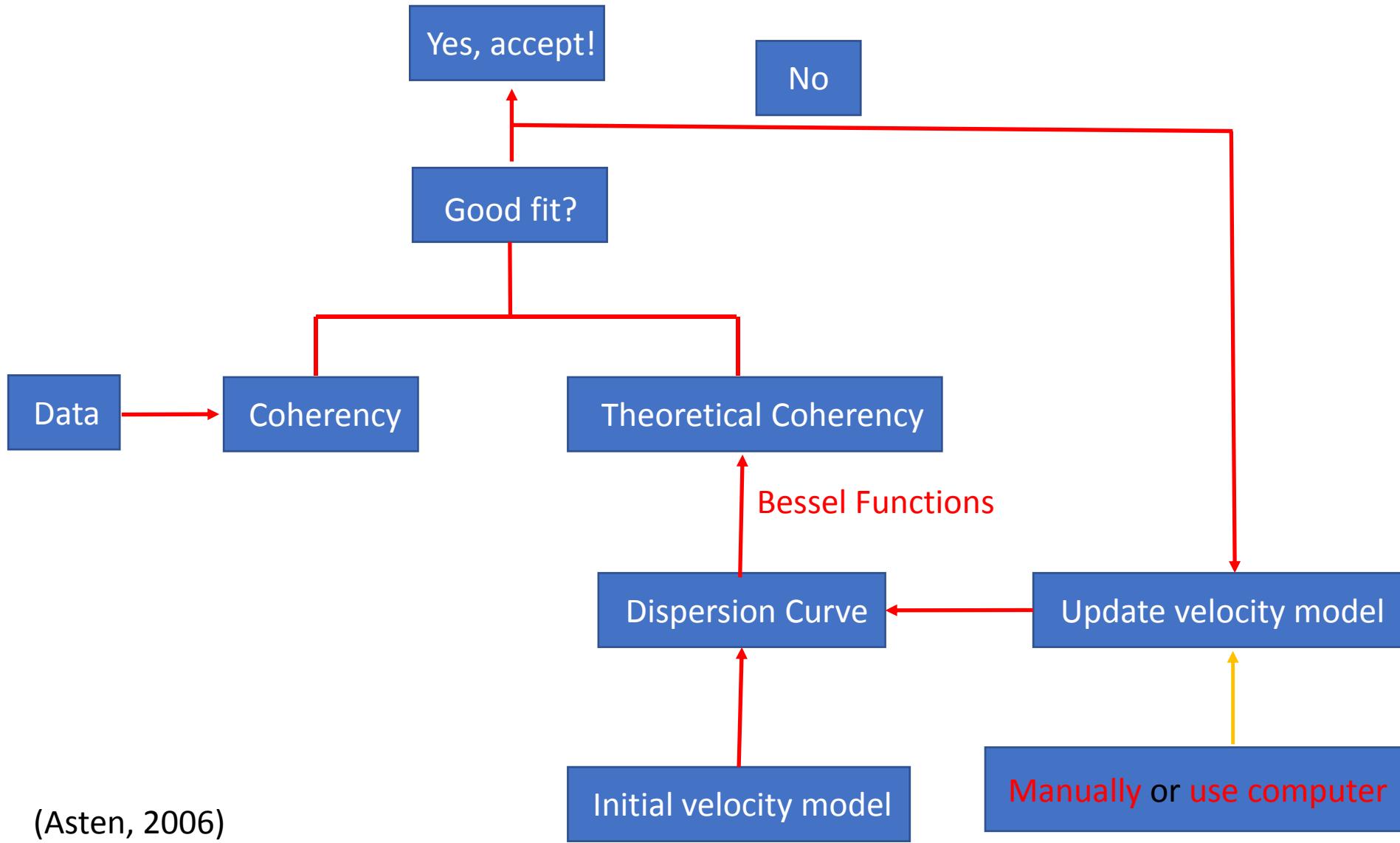
Real part



Imaginary part



Workflow of MMSPAC



Bayesian Method

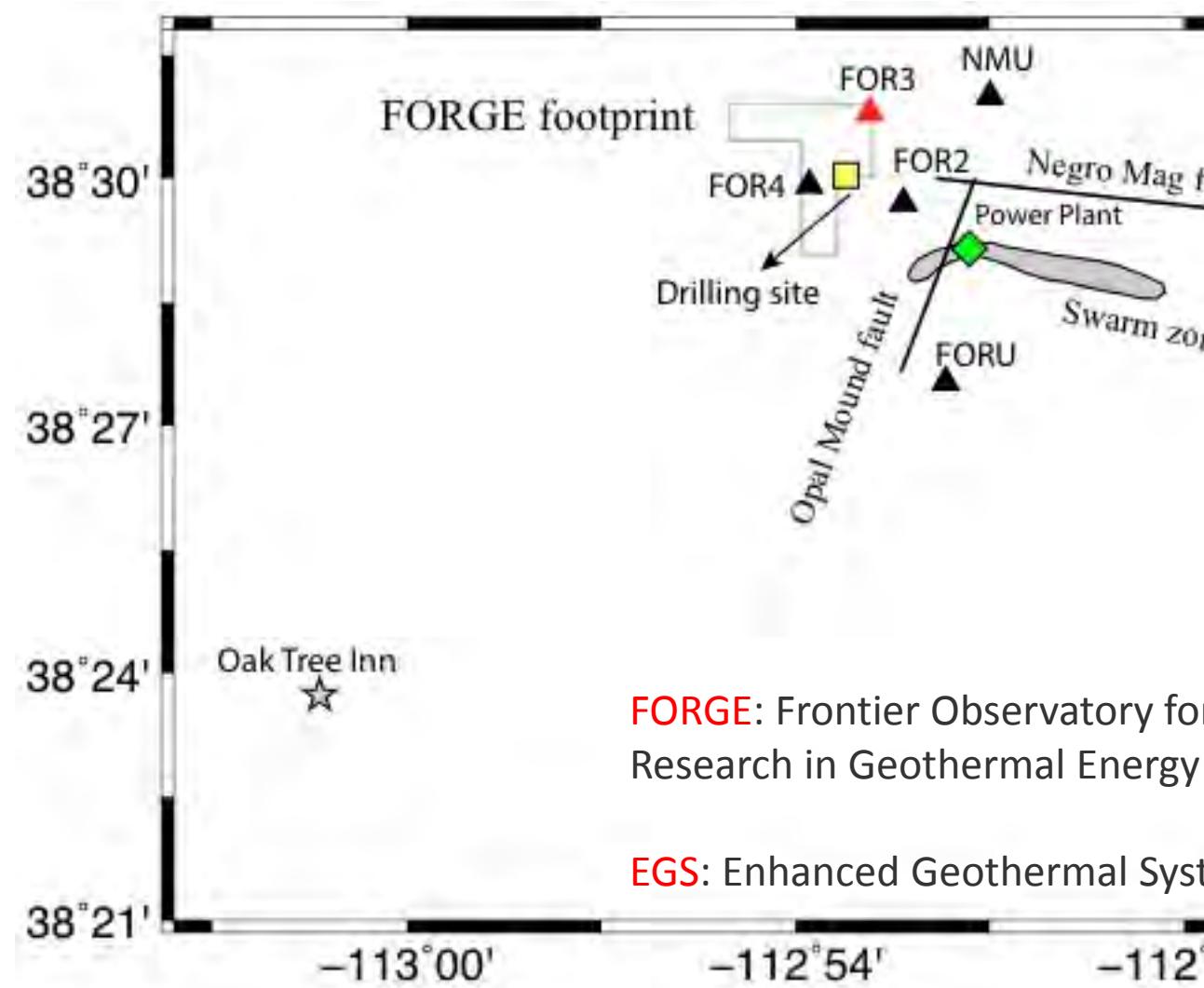
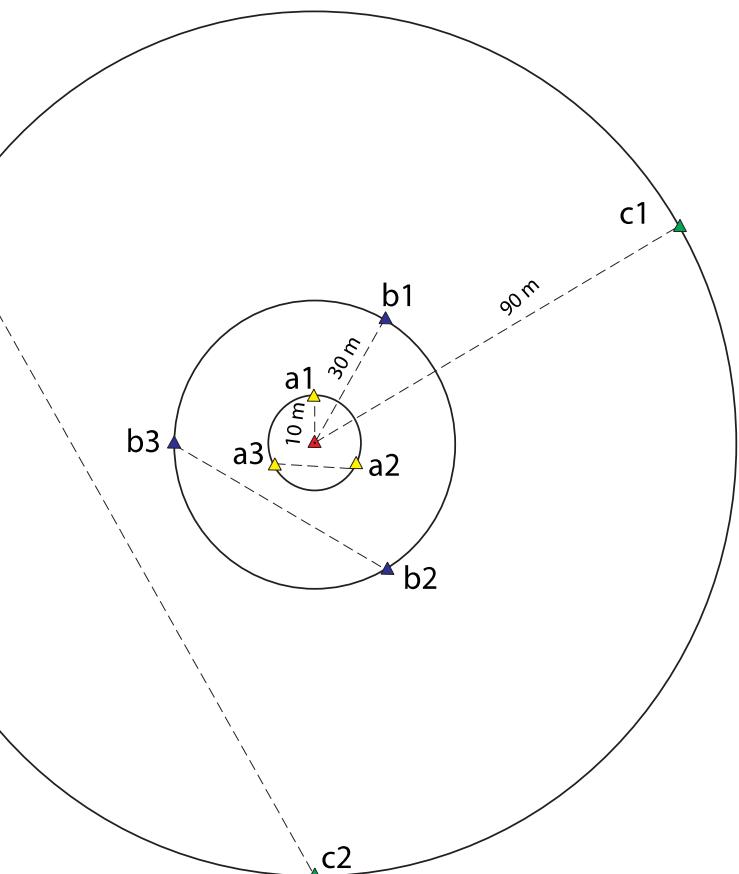
The Bayesian method is based on Bayes' theorem and is implemented in a Markov Chain Monte Carlo (MCMC) – Metropolis Hasting scheme

3000 models are randomly generated and for each model shear velocities and thicknesses of the top five layers are the variables to be modified

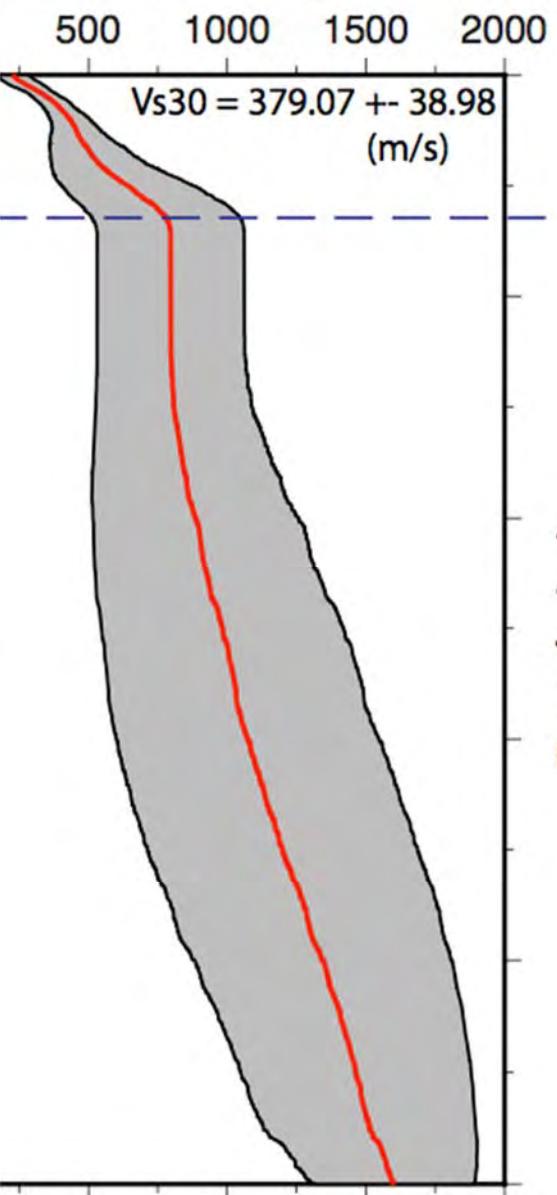
For the resultant 3000 models, a burning point of 1500 best models is used

Application to the FOR3 array

Array configuration at station FOR3

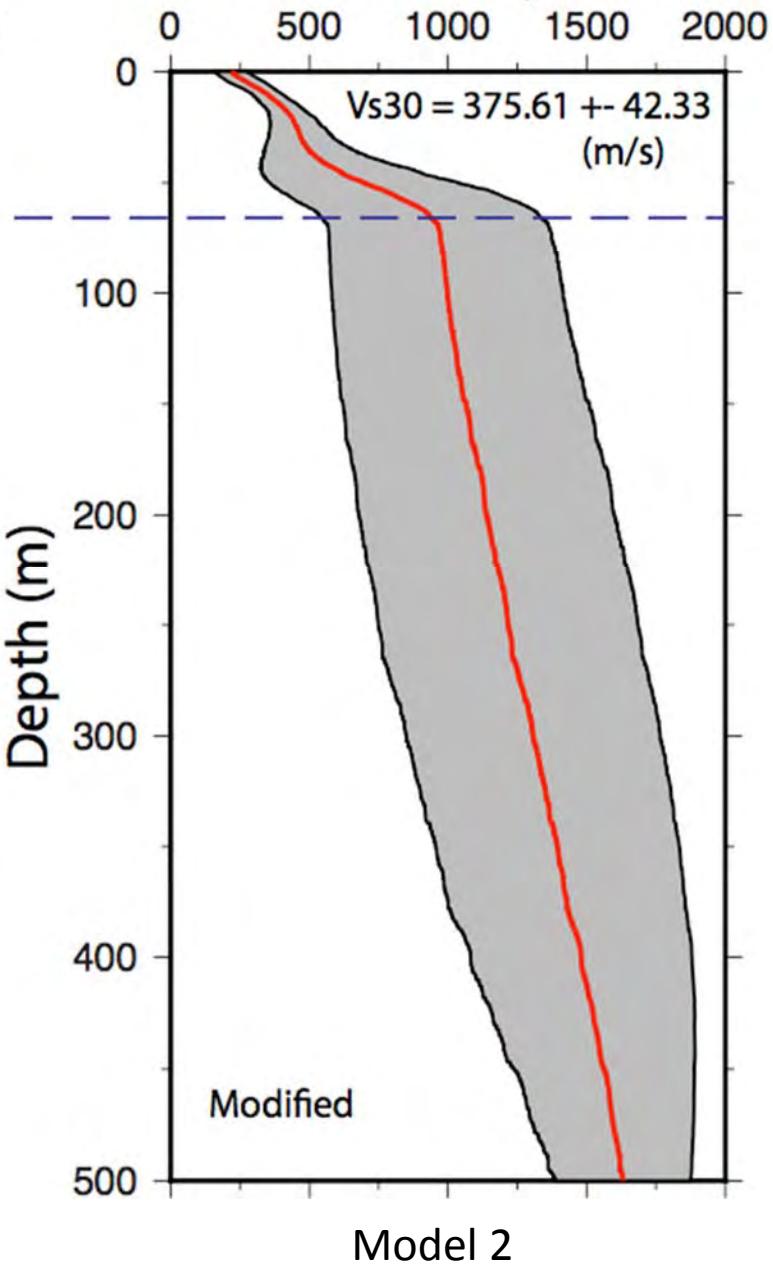


Shear Velocity (m/s)



Model 1

Shear Velocity (m/s)



Model 2

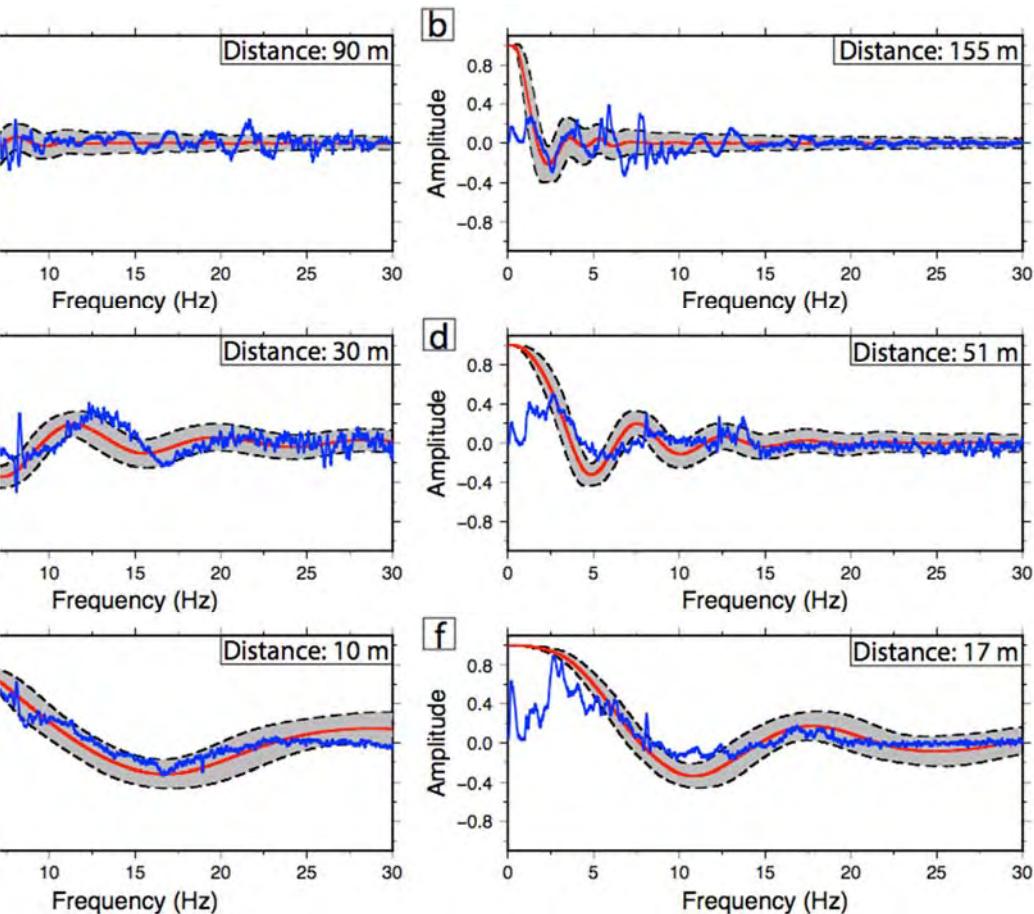
Parameter Table

	Thickness (m)	Vs (m/s)
Layer 1	$h_1 \in [0, 10]$	$Vs_1 \in [100, Vs_2]$
Layer 2	$h_2 \in [0, 10]$	$Vs_2 \in [Vs_1, Vs_3]$
Layer 3	$h_3 \in [0, 10]$	$Vs_3 \in [Vs_2, Vs_4]$
Layer 4	$H_4 \in [0, 50]$	$Vs_4 \in [Vs_3, Vs_5]$
Layer 5	h_5	Vs_5
Layer 6	1000	2000
Layer 7	0.0	3490

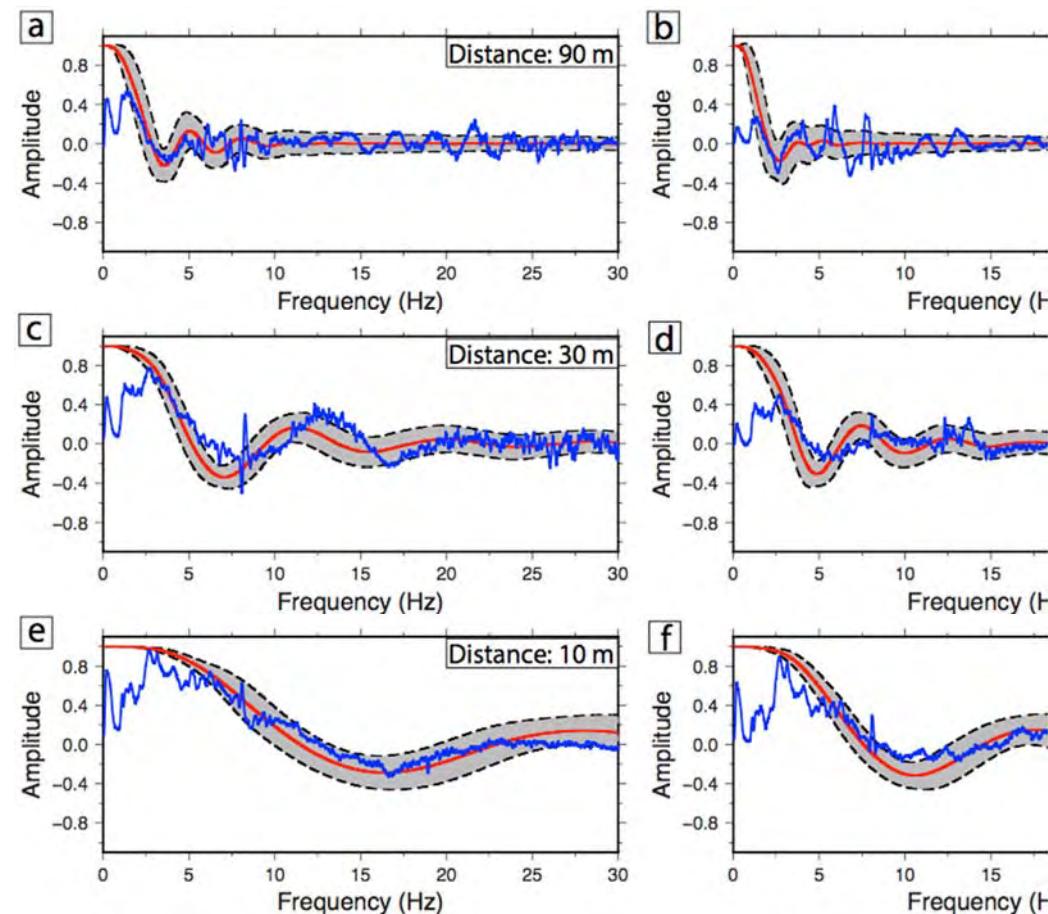
Model 1 : $h_5 \in [100, 500]$, $Vs_5 \in [Vs_4, Vs_5]$

Model 2 : $h_5 \in [0, 500]$, $Vs_5 \in [Vs_4, Vs_5]$

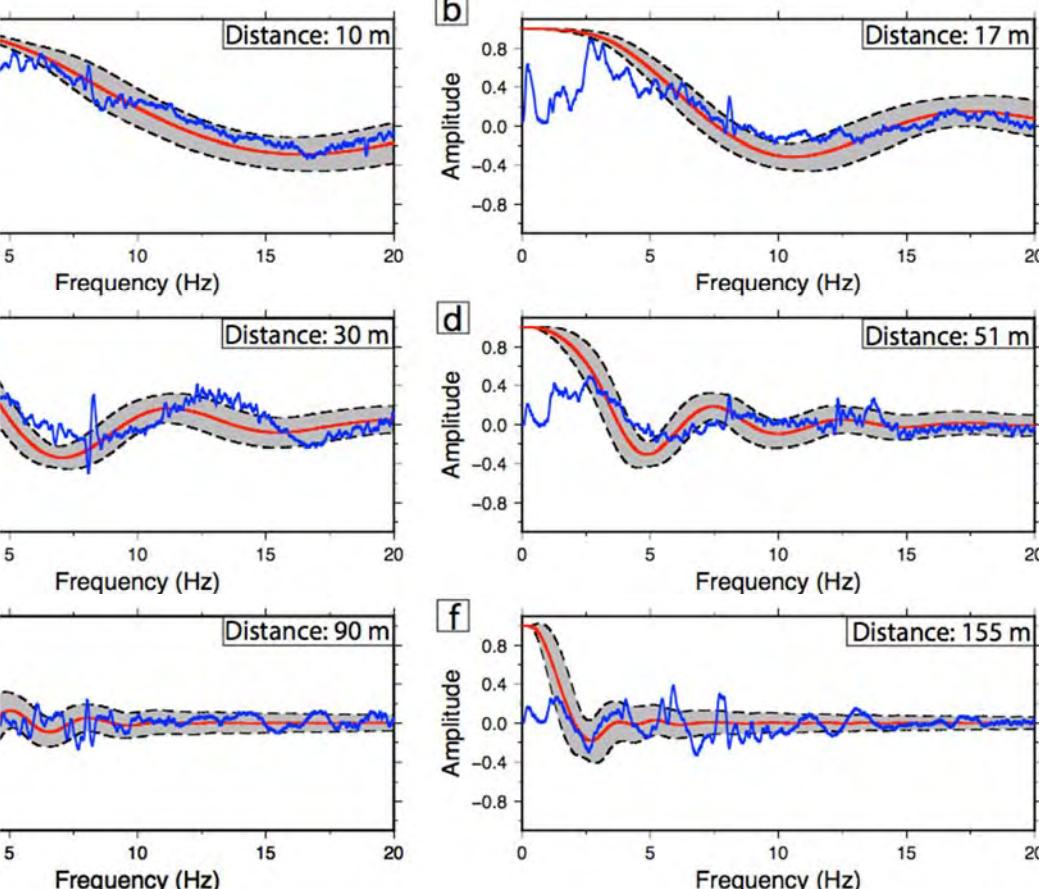
Model 1



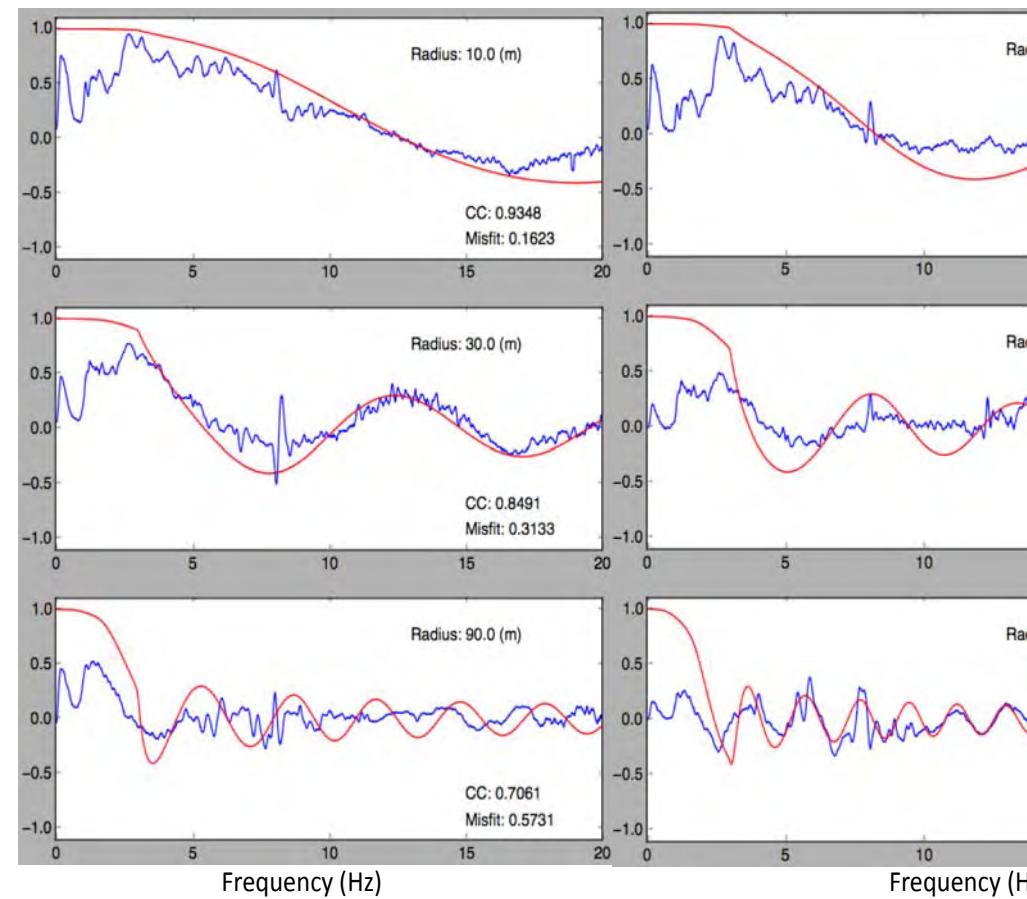
Model 2



Comparison of the SPAC between the Bayesian and forward iterative modeling

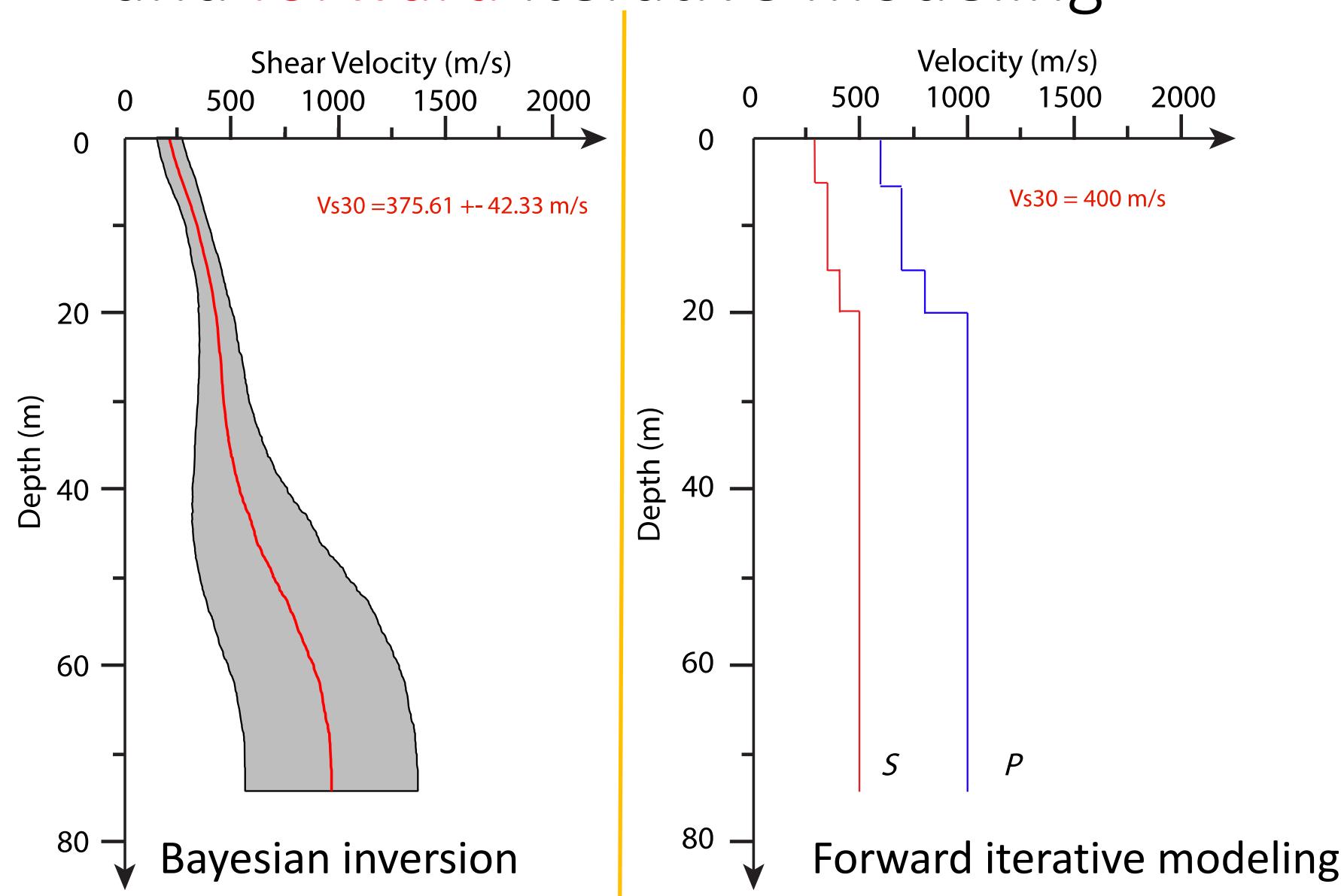


Bayesian inversion

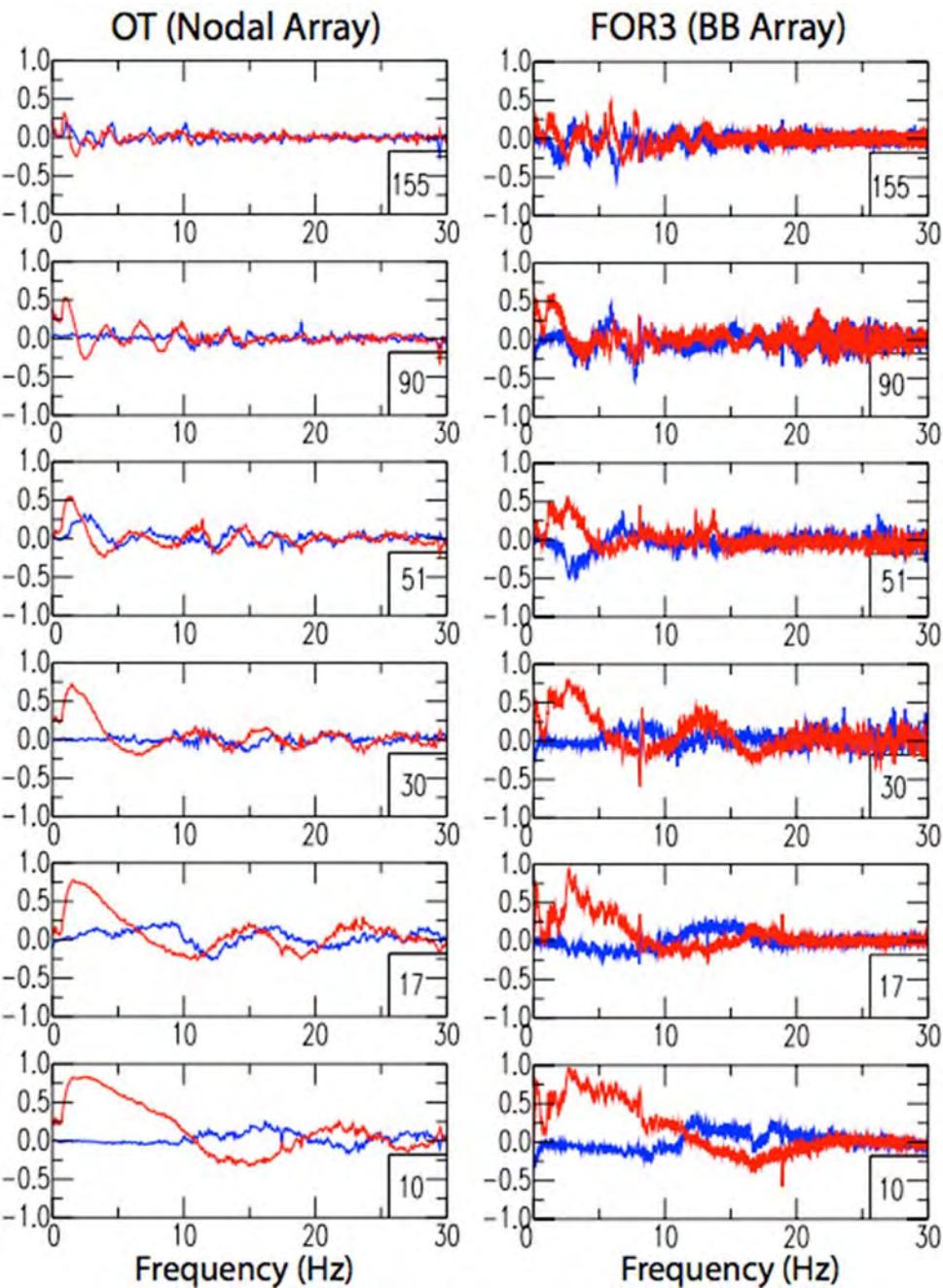


Forward iterative modeling

Comparison of the SPAC between the Bayesian and forward iterative modeling



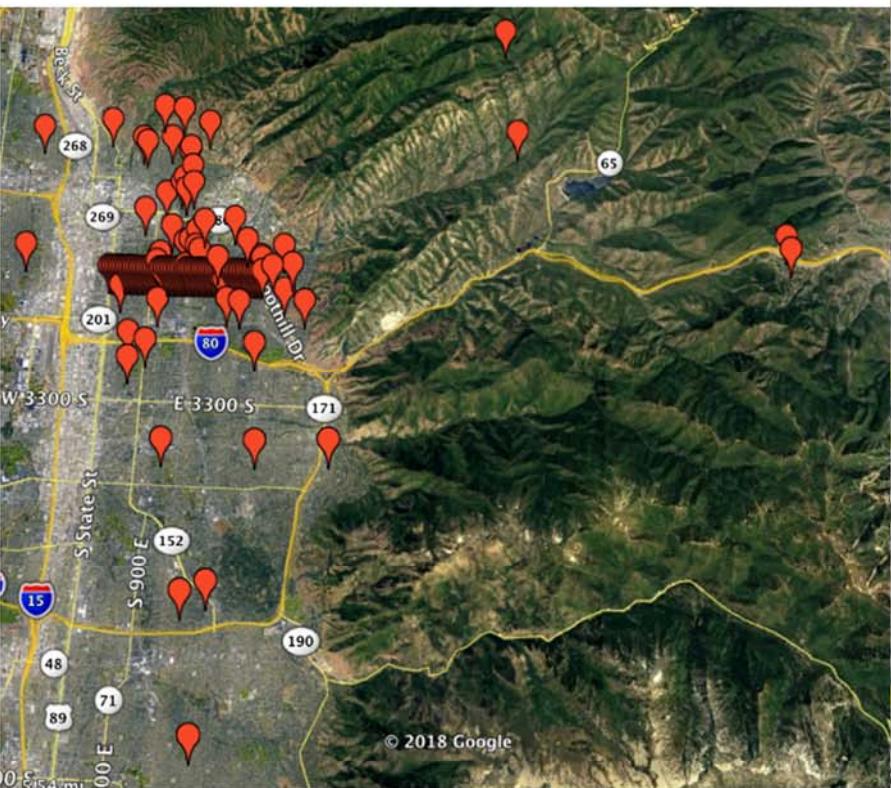
derived from Nodal and Broadband arrays



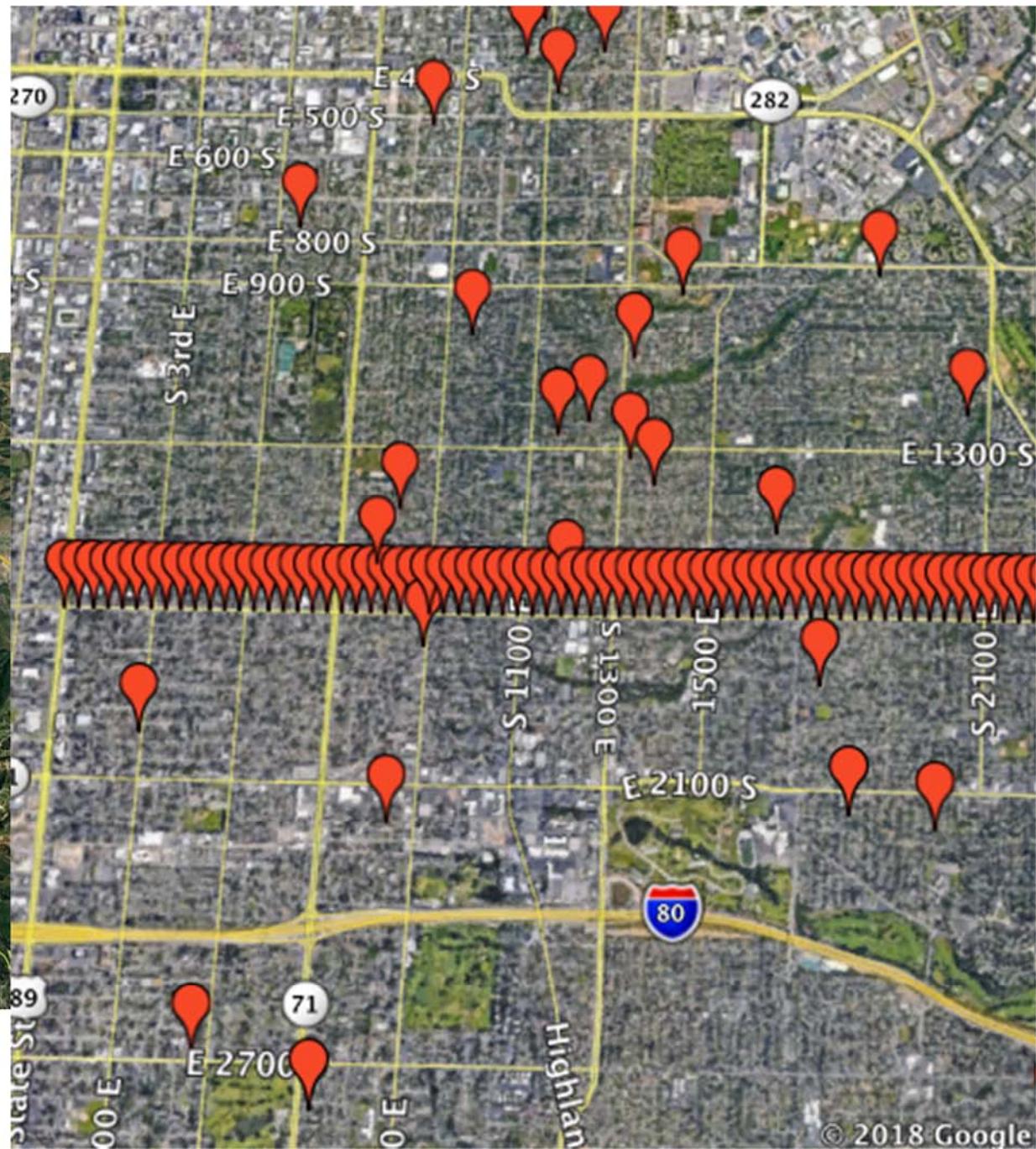
A node and a
broadband
station



n-going project



Professor Fan-Chi Lin's Group)



Conclusions

Compared to the traditional SPAC method, the stable Bayesian method can provide an uncertainty for velocity model and Vs30

The Nodal array has more potential than the broadband array in the application to get the Vs30

Thank you
for your
attention

'es' Theorem

$$p(\mathbf{x}|\mathbf{d}) = \frac{p(\mathbf{d}|\mathbf{x})p(\mathbf{x})}{\int_{-\infty}^{\infty} p(\mathbf{d}|\mathbf{x})p(\mathbf{x}) d\mathbf{x}}, \quad (3)$$

where $p(\mathbf{d}|\mathbf{x})$ is the PDF of \mathbf{d} given \mathbf{x} , and $\int_{-\infty}^{\infty} p(\mathbf{d}|\mathbf{x}) \times p(\mathbf{x}) d\mathbf{x}$ normalizes the posterior PDF. In this section, we present an explicit expression of $p(\mathbf{d}|\mathbf{x})$ and $p(\mathbf{x})$. We also present a method for estimating the posterior PDF, $p(\mathbf{x}|\mathbf{d})$.

(Fukuda and Johnson, 2008, BS)

Markov Chain Monte Carlo (MCMC) – Metropolis Hastings

algorithm:

$$\begin{aligned}\vec{\theta}_0, \\ k = 0, k+1, \\ u \sim U[0, 1], \\ \vec{\theta}^* \sim \text{pdf}(\vec{\theta}_k)\end{aligned}$$

$$f. u < \min\left(1, \frac{\pi(\vec{\theta}^*) L(\vec{\theta}^* | \vec{x})}{\pi(\vec{\theta}_k) L(\vec{\theta}_k | \vec{x})}\right)$$

$$\vec{\theta}_{k+1} = \vec{\theta}^*$$

$$\vec{\theta}_{k+1} = \vec{\theta}_k.$$

posterior \propto likelihood \times prior

$$p(\vec{m} | \vec{D}_{\text{obs}}) \propto p(D_{\text{obs}} | \vec{m}) p(\vec{m}),$$

misfit function:

$$\vec{\Phi}(\vec{m}) = (\vec{G}(\vec{m}) - \vec{D}_{\text{obs}})^T C_e^{-1} [\vec{G}(\vec{m}) - \vec{D}_{\text{obs}}]$$

Likelihood:

$$p(\vec{D}_{\text{obs}} | \vec{m}) = \frac{1}{\sqrt{(2\pi)^N |C_e|}} e^{-\frac{\vec{\Phi}(\vec{m})}{2}}$$

SEISMIC LAND STREAMER IMAGING BENEATH SALT LAKE CITY UTAH GROUND SHAKING WORKING GROUP – 2/13/18

Lee Liberty – Boise State University

Gabe Gribler, James St. Clair, Thomas Harper, Thomas Otheim



BOISE STATE UNIVERSITY

SEISMIC IMAGING OBJECTIVES

Earthquake hazard and risk assessments beneath urban centers

- Identify and characterize the [Warm Springs fault](#) beneath downtown SLC
- Identify and characterize the northern portions of the [East Bench fault](#)
- Identify and characterize faults within the step-over region of the Salt Lake front
- Generate a [Vs₃₀ map for Salt Lake City](#)
- Liquefaction susceptibility via [V_p and V_s measurements](#)
(map low V_s zones and identify shallow water table areas)
- Depth to bedrock/key boundaries via [gravity, V_p, V_s, and reflection imaging](#)
- Funding sources

USGS NEHRP #G15AP00054 – 2015 field campaign

USGS NEHRP #G17AP00052 – 2017 field campaign – [in progress](#)



BENEFITS OF SEISMIC LAND STREAMER COMPARED TO TRADITIONAL SEISMIC IMAGING



- Rapid data collection – 4-5 km/day
- Minimal field crew – one person operation
- Directly operate on city streets
- Predictable source/receiver geometry makes processing more simple
- Real time GPS allows for simple geometry
- Physical properties of road and sub road make for a uniform near surface
- Police or flagger assistance to control traffic and provide near continuous profiling
- Large seismic source relative to imaging depths allows for traffic noise during data collection



SUMMARY OF 2015/2017 FIELD CAMPAIGNS

May, 2015 → 3 field days

5,576 48 channel shot gathers

2 m spaced shots (gaps at major roads)

15 km length along 9 west-east profiles

Police escort along most roads allowed near continuous profiling

Offsets: 5-65 m

May, 2017 → 5 field days

9839 shot gathers

20 km length along 13 profiles

Offsets: 10-70 m

Total:

35 km along 22 streets

2m spaced shots, 1.25 m spaced receivers

400 m/hour or a shot every 15 seconds

15,419 hammer hits



PHYSICAL PROPERTY ESTIMATES SALT LAKE CITY

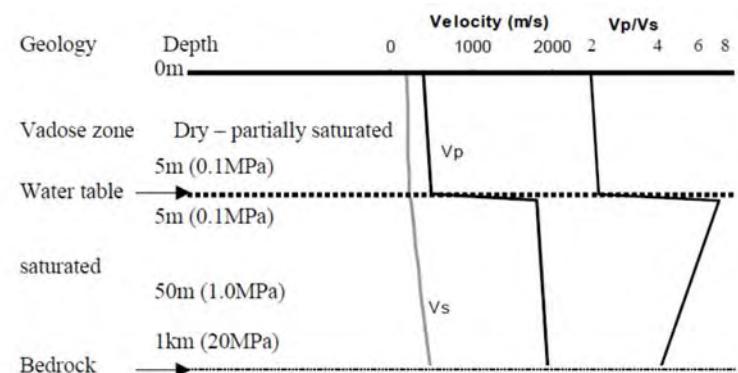
Low Vs & Vp for Bonneville deposits

Higher Vs & Vp for alluvial fan deposits

High Vp for water saturated sediments

Good reflectivity in lake deposits, shallow groundwater

Poor reflectivity in alluvial fans, deeper water table

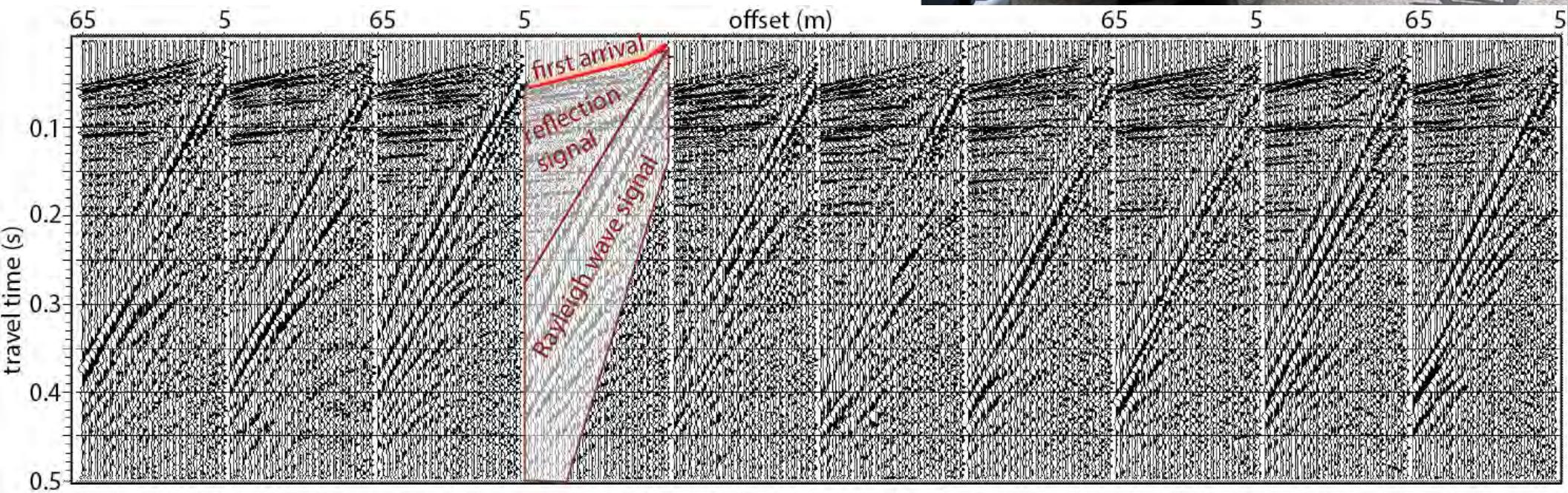


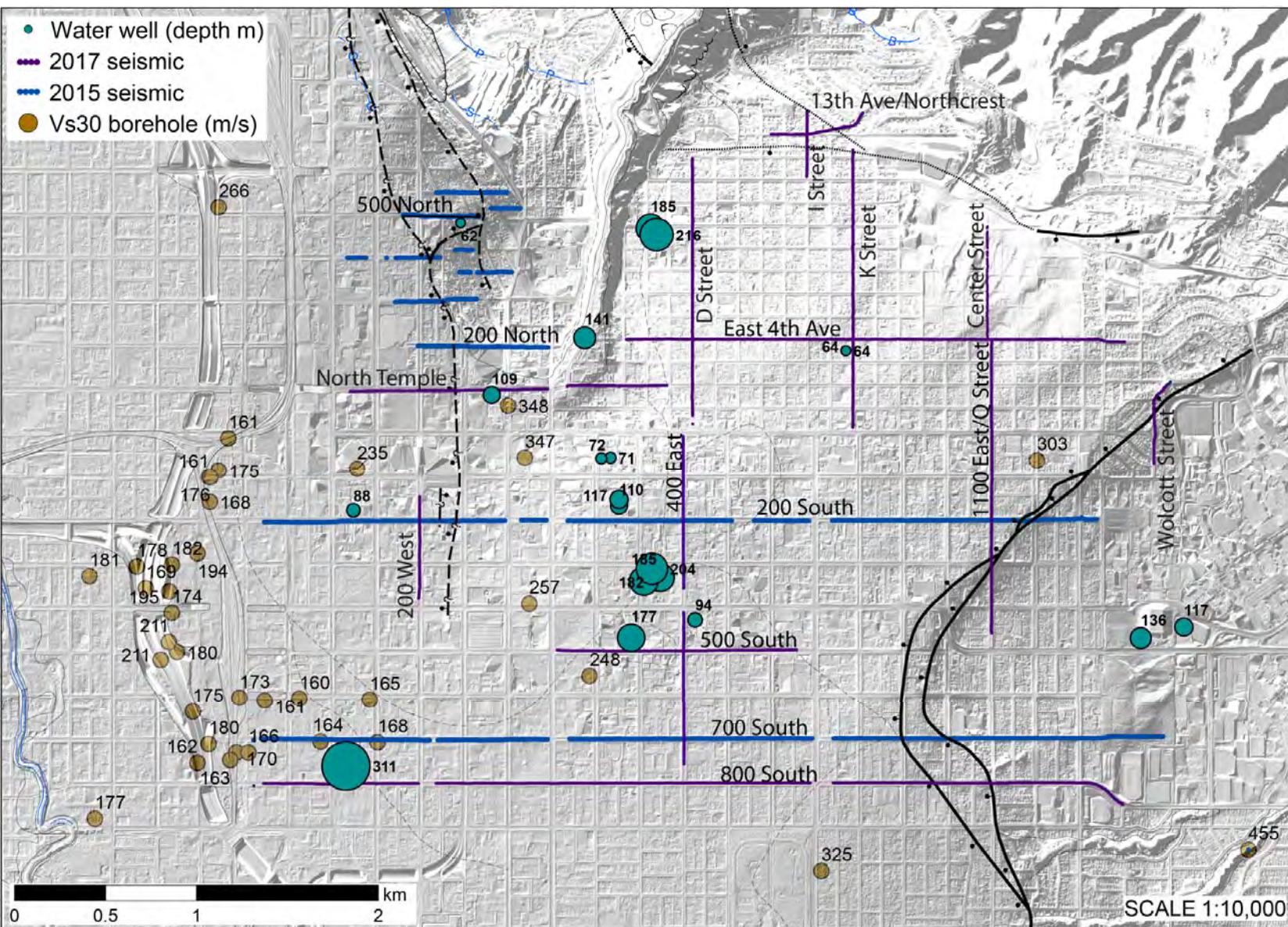
From Bartlett, S., 2004 - UDOT

Cone Penetrometer											Gardner alpha	0.3
											Gardner beta	0.25
Depth	Depth	Soil Type	Unit Weight	bulk density	Shear wave Velocity	Shear Modulus	Modulus	Vp - dry	Vp/Vs - dry	Vp - from Gardner	Vp/Vs - wet	
(m)	(m)		(kN/m³)	g/cc	(m/s)	(kPa)	(kPa)			wet, fcn of density		
0	5	Alluvium	19.2	1.96	146	41700	113000	293.3535	2.01	1818.9	12.46	
5	12	Upper Bonneville	18.2	1.86	170	53600	161000	353.7999	2.08	1468.6	8.64	
12	16	Interbeds	18.8	1.92	235	106000	318000	489.3258	2.08	1672.0	7.11	
16	22	Lower Bonneville	18.2	1.86	201	75000	225000	418.33	2.08	1468.6	7.31	
22	25	Pleistocene	19.5	1.99	237	112000	335000	493.3645	2.08	1935.3	8.17	

URBAN LAND STREAMER DESIGN

48 2-component shoes (vertical and in-line)
4.5 Hz geophones (interchangeable to 10, 40 Hz)
1.25 m spaced geophones (60 m aperture)
(now additional 30 m segment to extend to 90 m aperture)
2 m nominal shot spacing
Accelerated weight drop source (**Arduino controlled**)
One person performs all operations





DOWNTOWN SALT LAKE CITY LIDAR MAP WITH SEISMIC AND BOREHOLE LOCATIONS

36 Vs measurements

Mapped faults
McKean (2014)
Personious and Scott (2009)

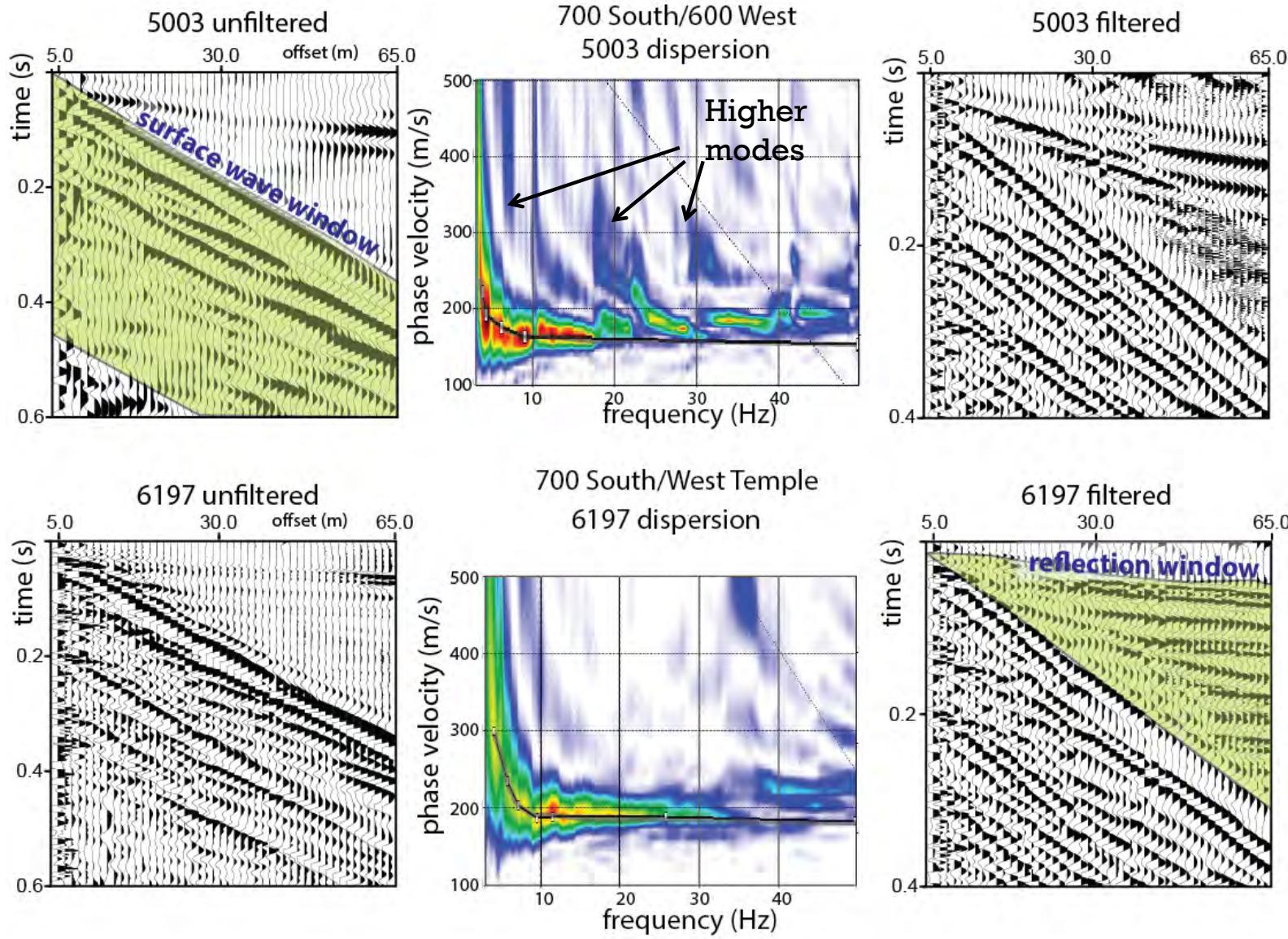


VS (MASW) PROFILING

700 SOUTH SHOTS AND DISPERSION CURVES

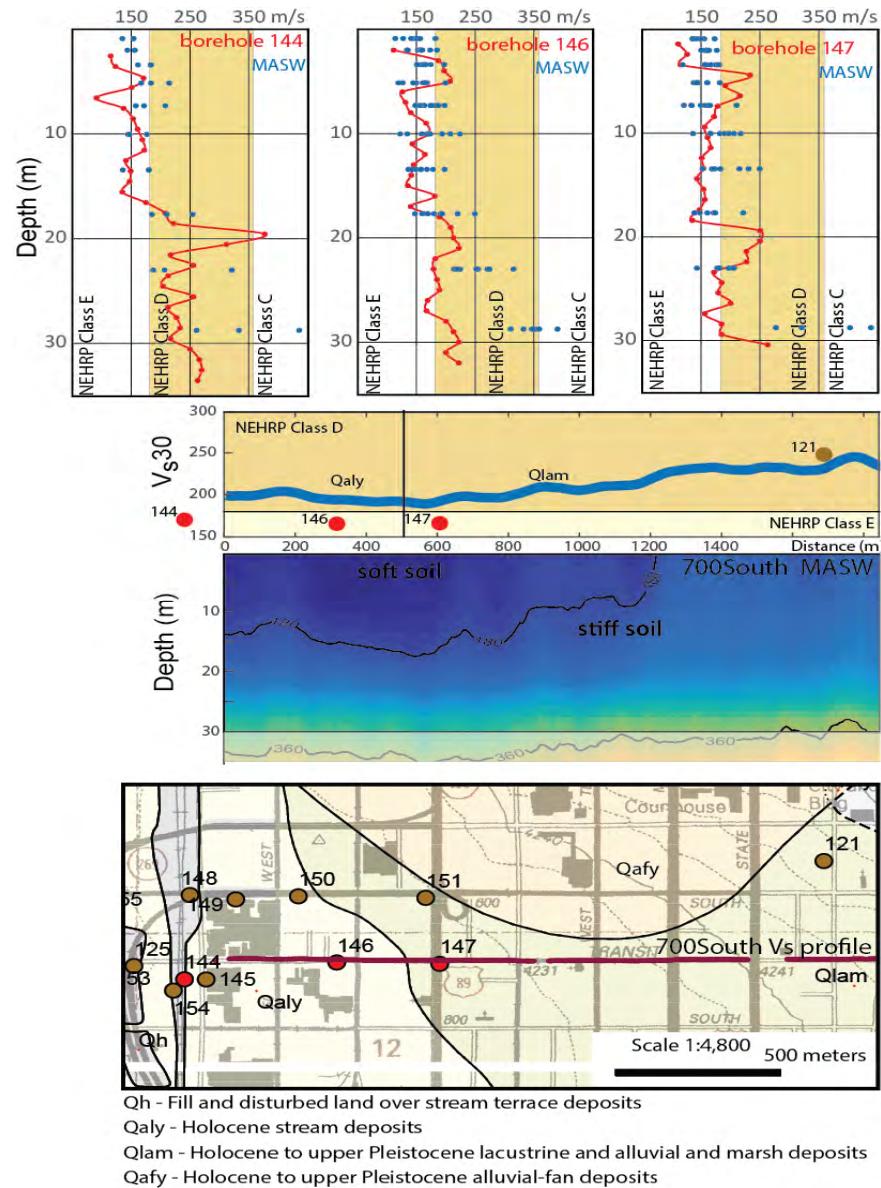
$$VS30M = \frac{\sum DI}{\sum TI} = \\ 30 / \sum(DI/VSI)$$

SUMMATION OF THICKNESS (DI)
DIVIDED BY VELOCITY (VSI)
OF EACH LAYER



DO ROAD SURFACE/UTILITIES IMPACT SEISMIC MEASUREMENTS?

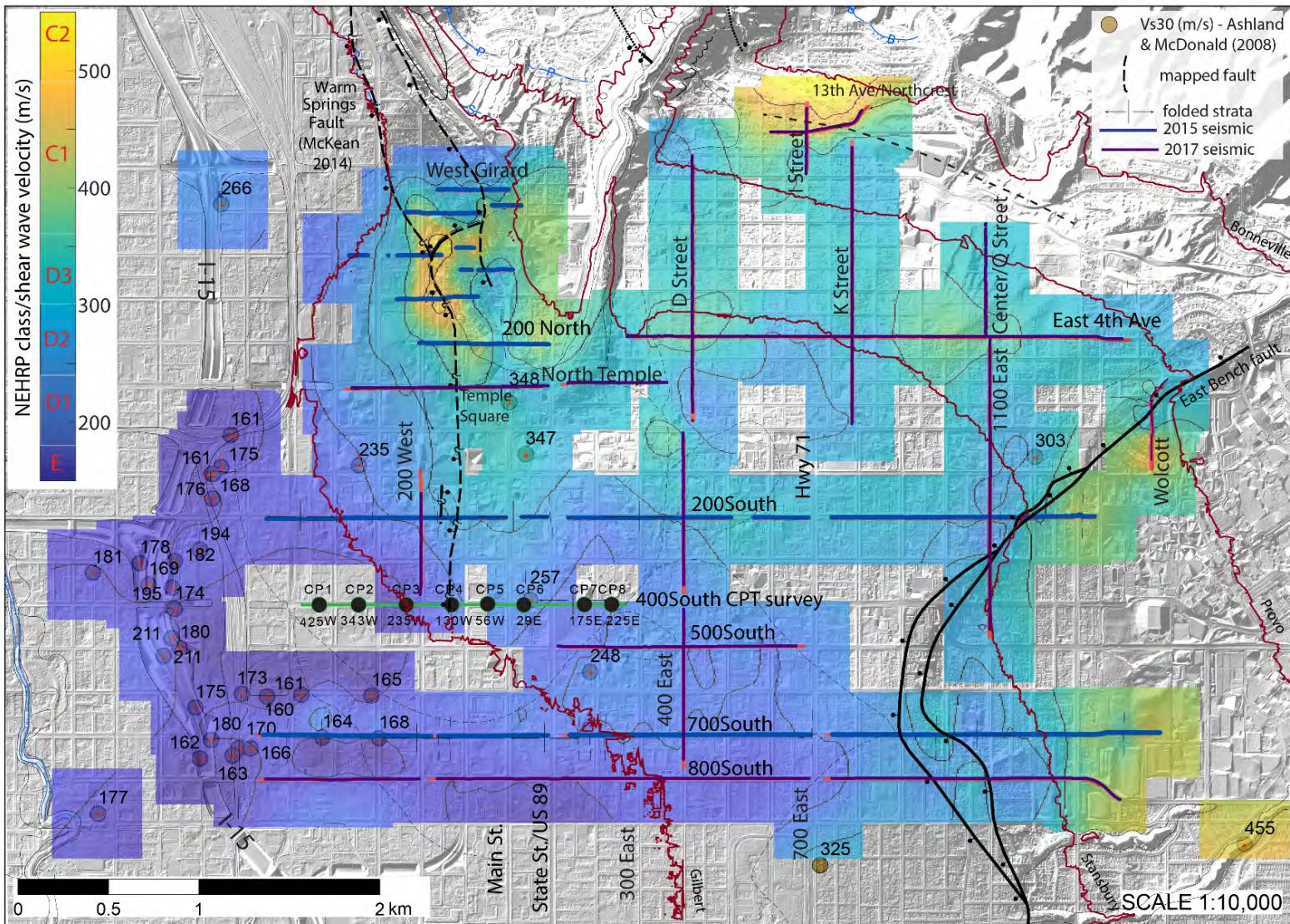
USUALLY NO – BUT CONCRETE ROADS AND TUNNELS ARE BAD



VS₃₀ MAP FOR DOWNTOWN SALT LAKE CITY

36 Vs measurements
McDonald and Ashland (2008)

15,000 additional Vs
measurements
via seismic land streamer

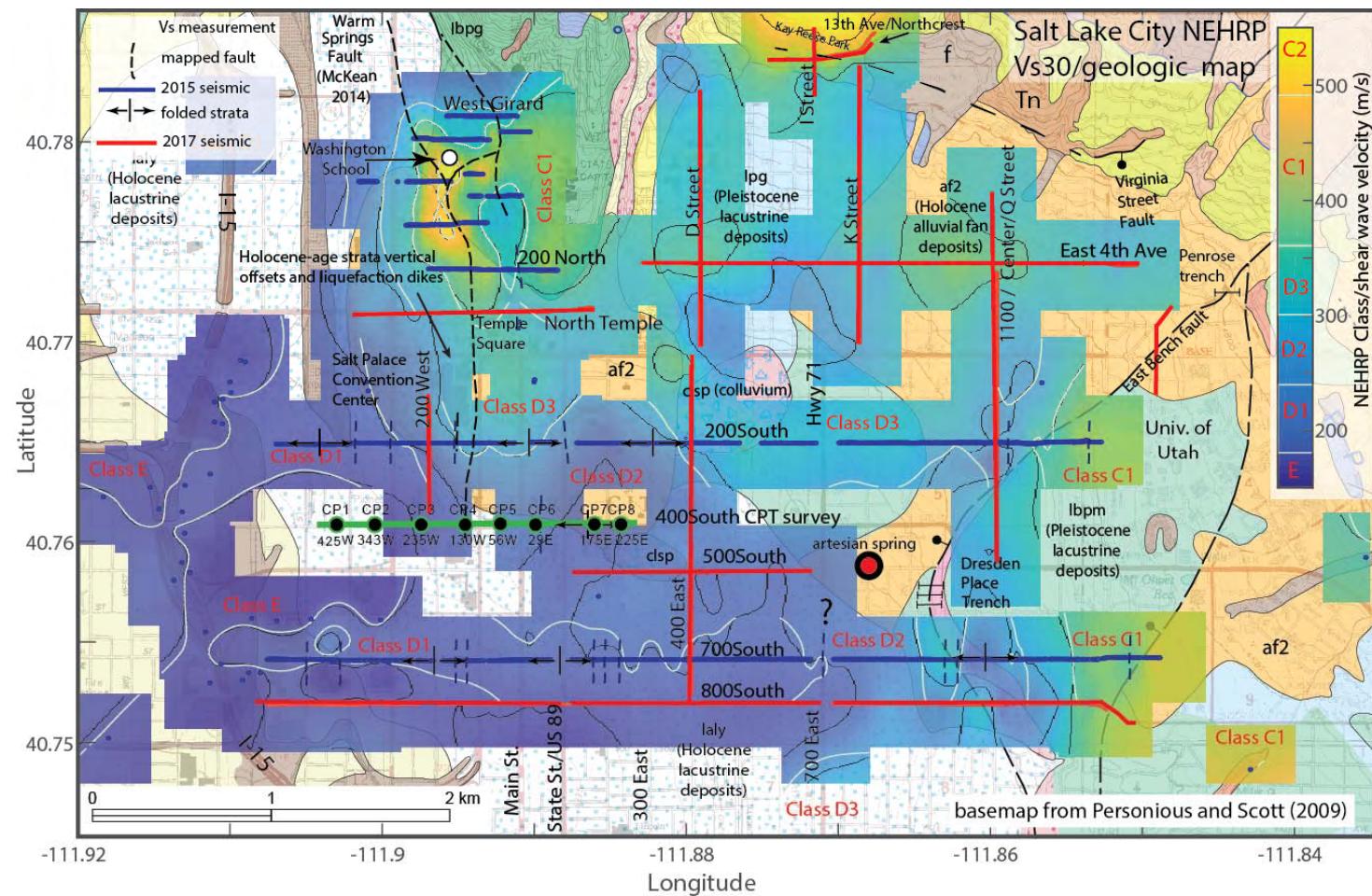


SALT LAKE CITY VS₃₀ LAND STREAMER RESULTS WITH GEOLOGIC MAP

Low Vs for Bonneville deposits beneath western portions of downtown Salt Lake City

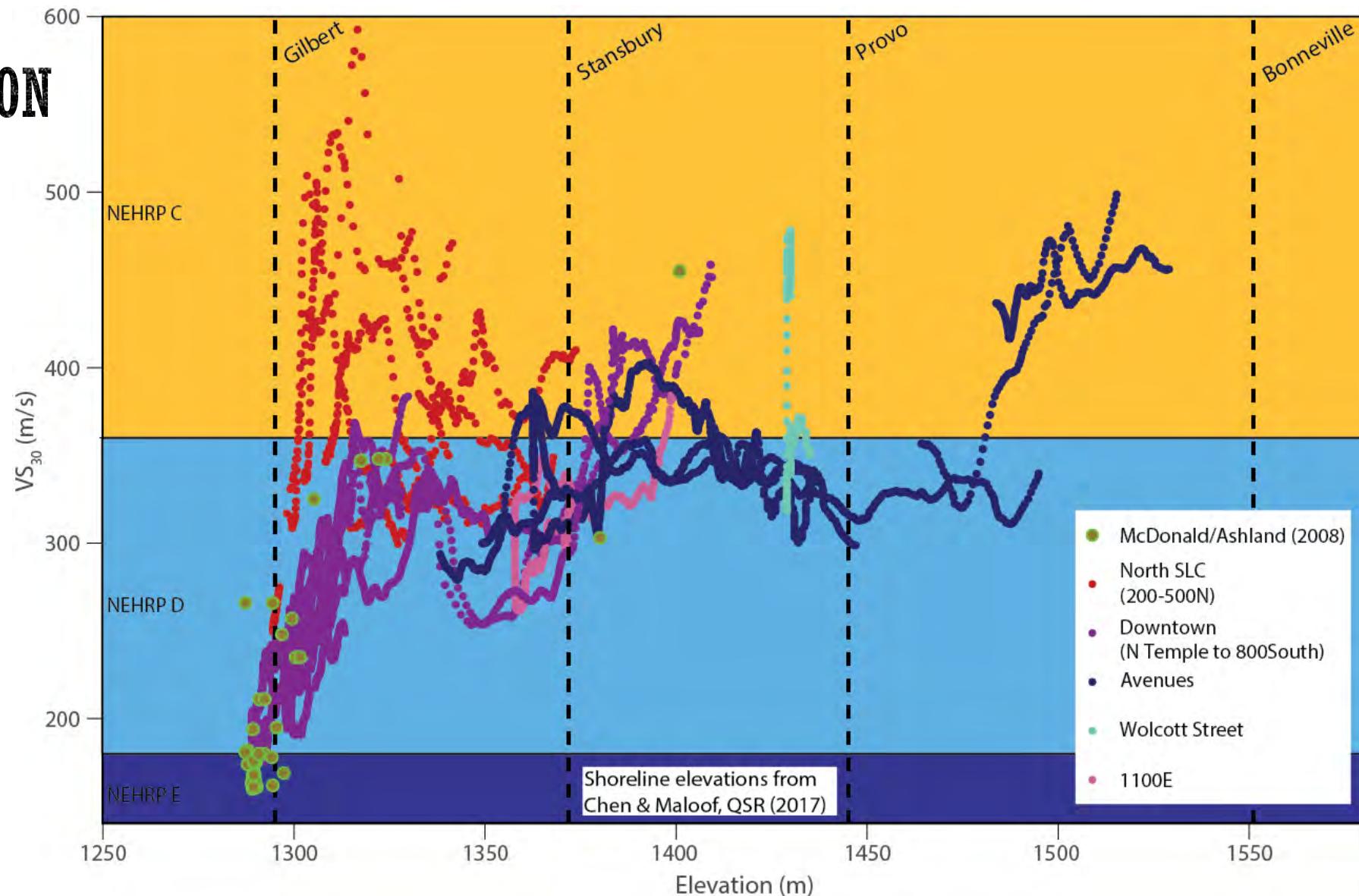
Increase in Vs30 from west to east

High Vs in the footwall or in fault zones



EL ELEVATION VS. VS₃₀

Linear
Vs/elevation
relationship at
low elevations



SUMMARY OF VS

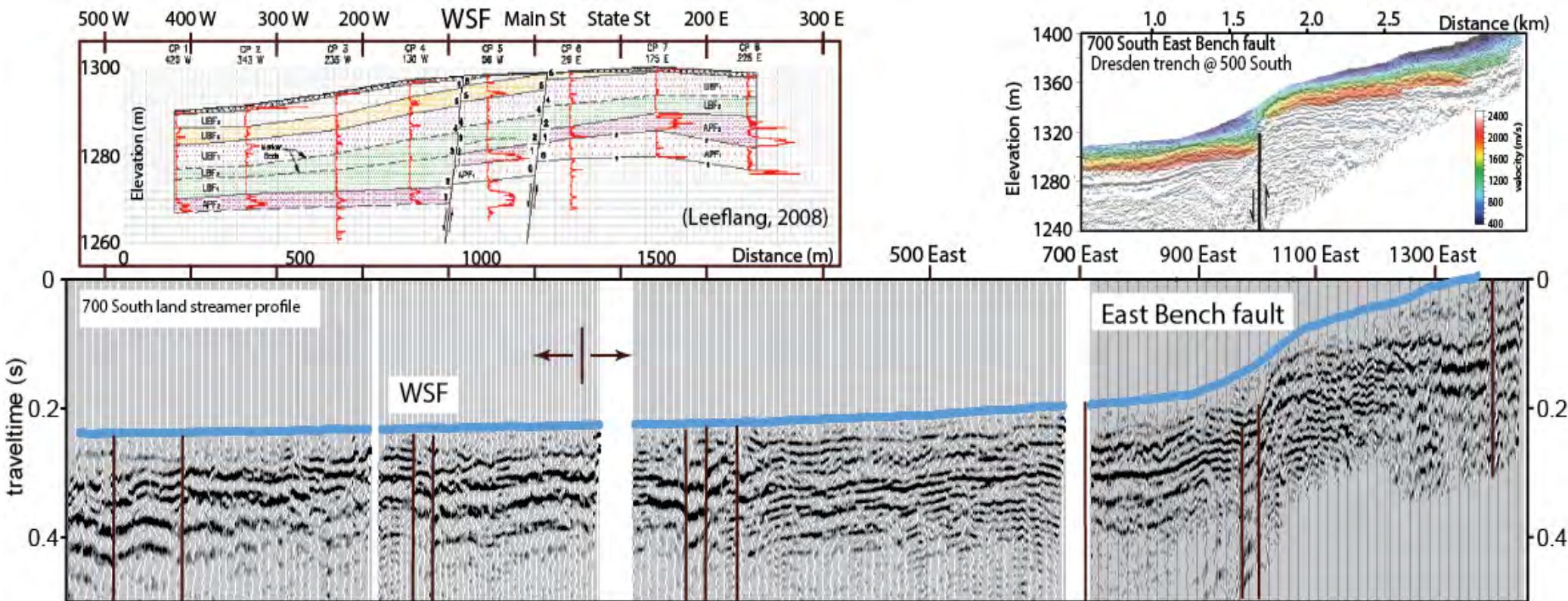
- Vs generally increases from west to east
- Vs generally follows a linear trend with elevation, with resets by Lake Bonneville shoreline highstands
- Vs increases at or near Warm Springs/East Bench faults

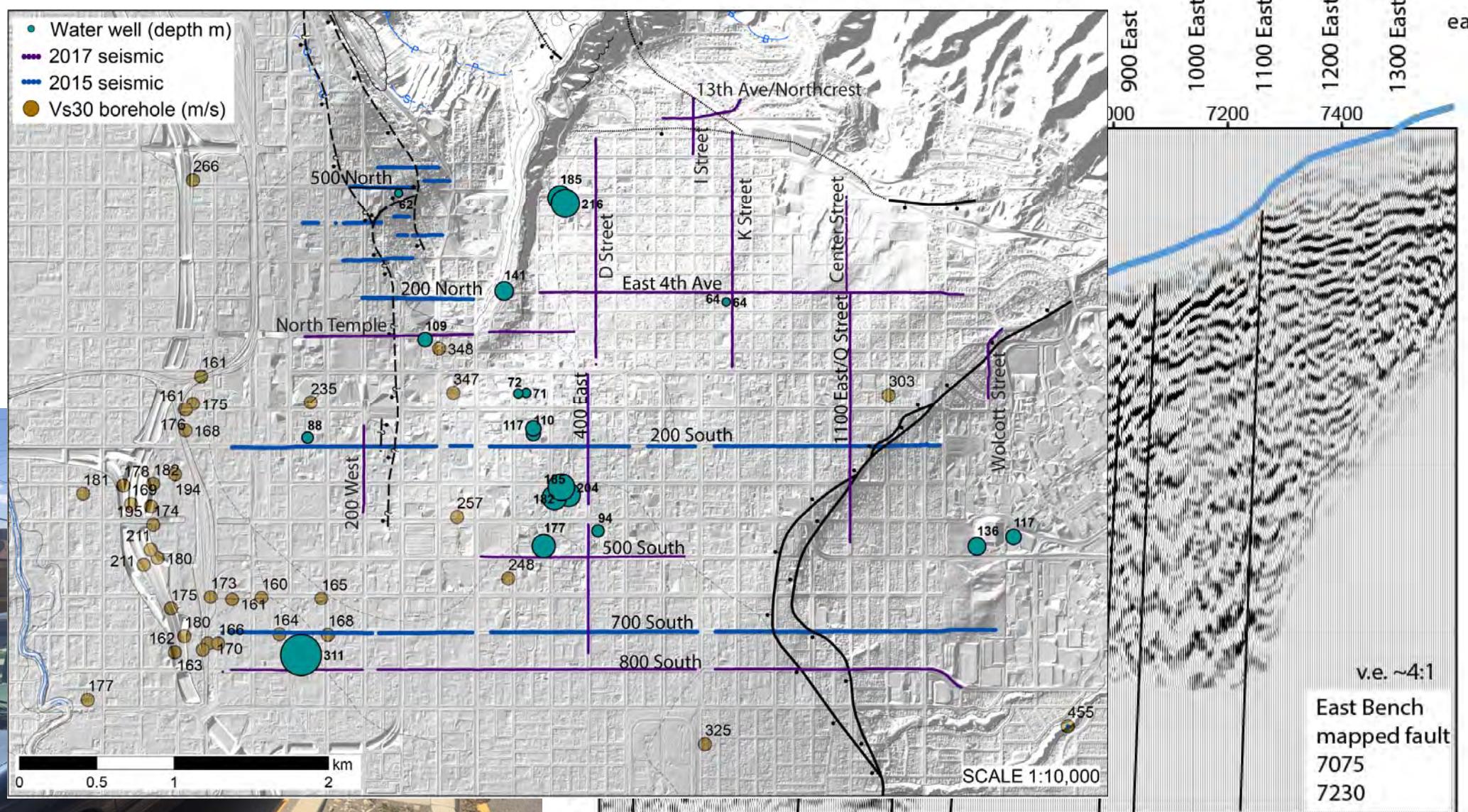
- To do:
 - Produce map of probing depth sensitivities – how deep can our streamer image with surface waves?
 - Produce “super gathers” to include lower frequency signals
 - Examine shallow Vs (Vs10) relationship to mapped geology



700 SOUTH REFLECTION PROFILE (COMPARED TO 400S)

- **Dresden Place Trenches (1986):**
- ≥7 m deformation
- 3 m monoclinal warping—latest Pleistocene
- ≥4 m brittle deformation (fault offset)—Holocene

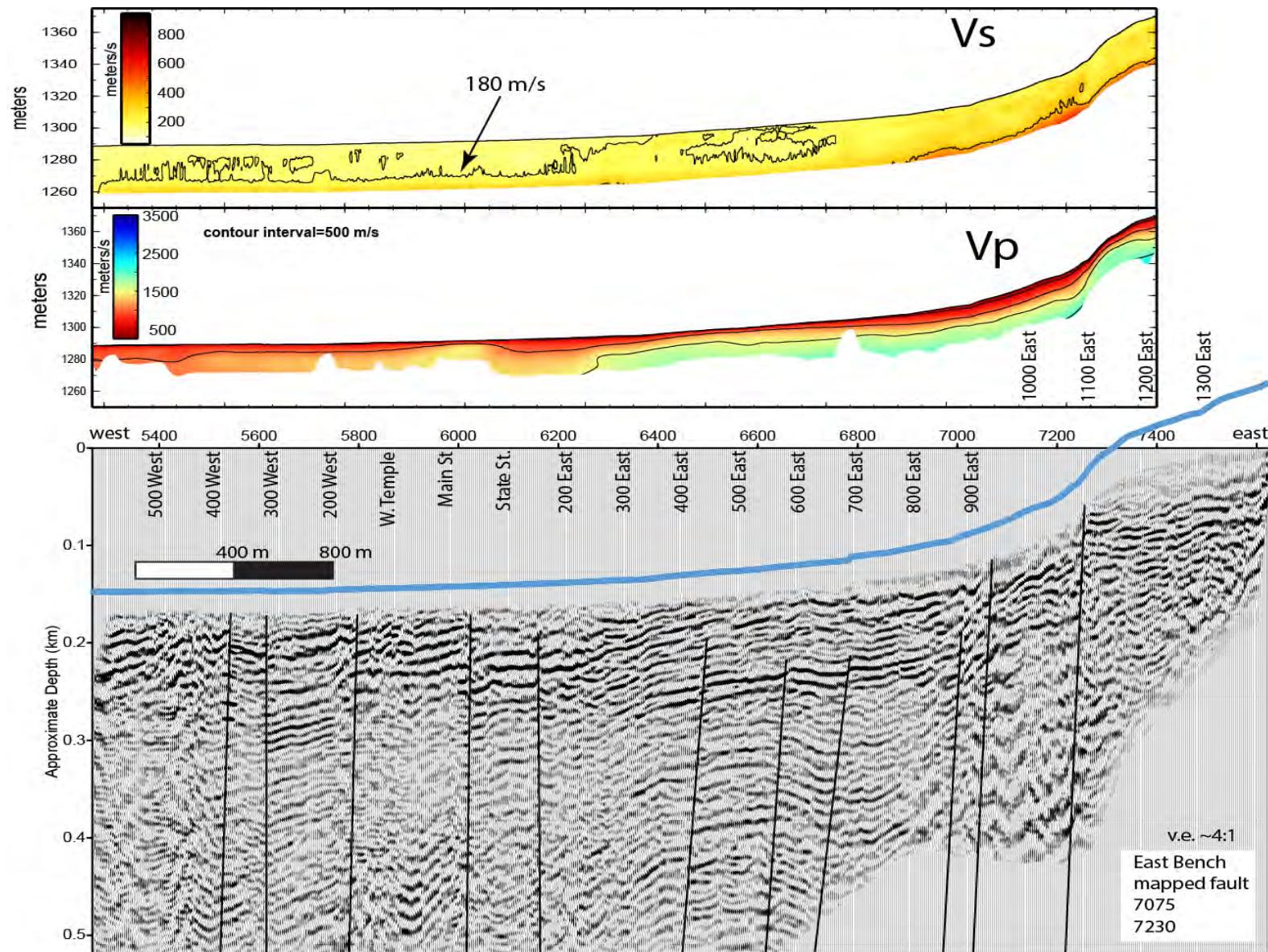




800 SOUTH

V_s and V_p velocities
slow to the west

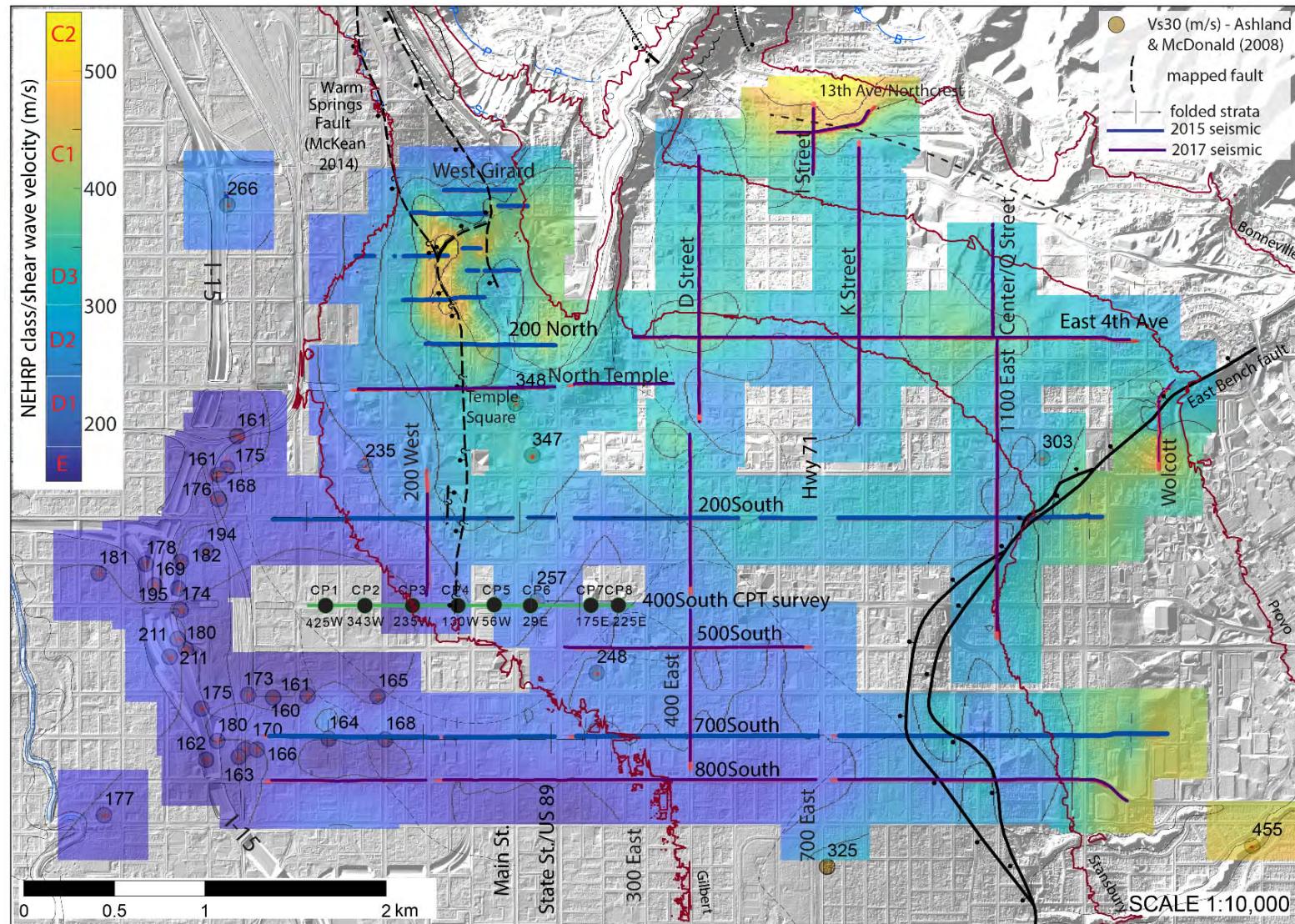
Seismic character is
more chaotic to the west



VS₃₀ MAP FOR DOWNTOWN SLC

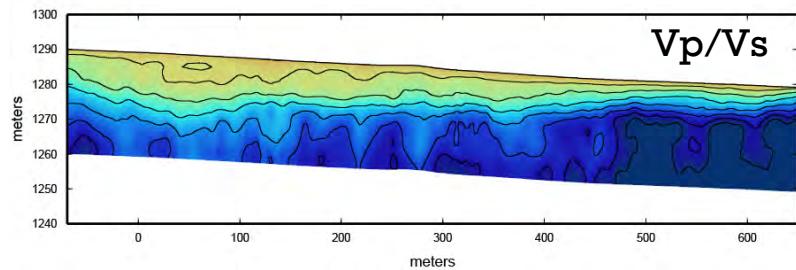
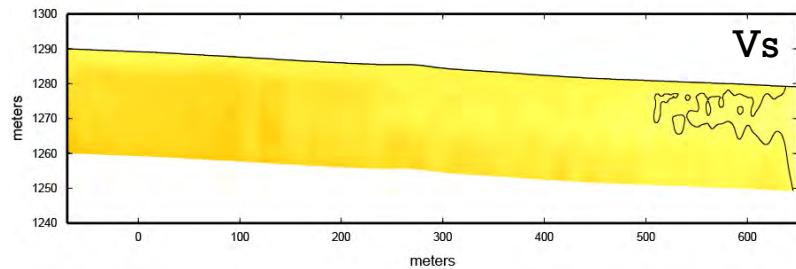
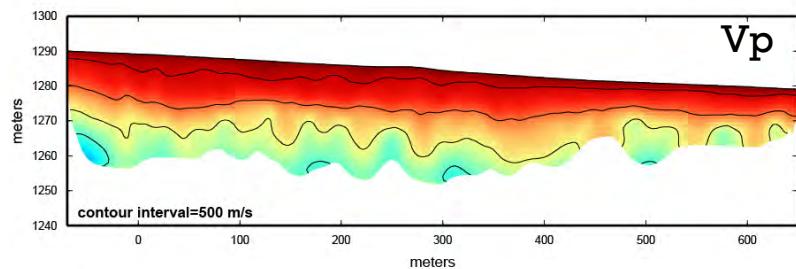
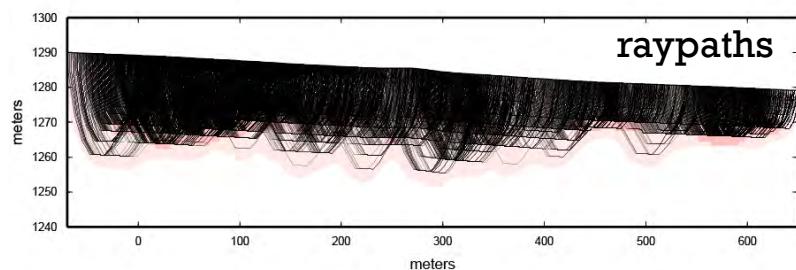
36 Vs measurements
McDonald and Ashland (2008)

15,000 additional Vs measurements
via seismic land streamer

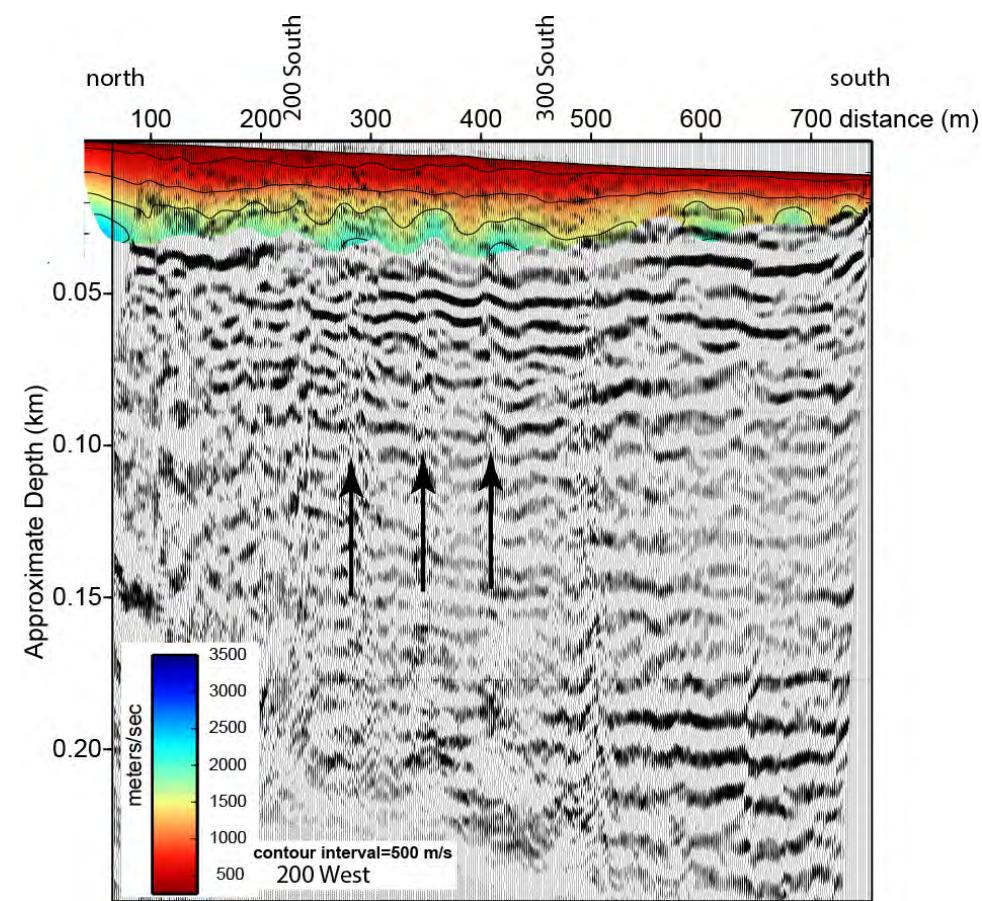
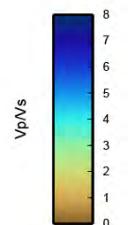
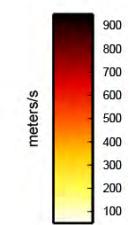
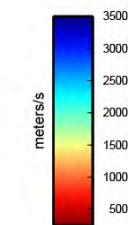
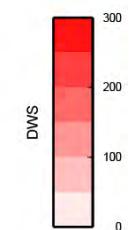


North

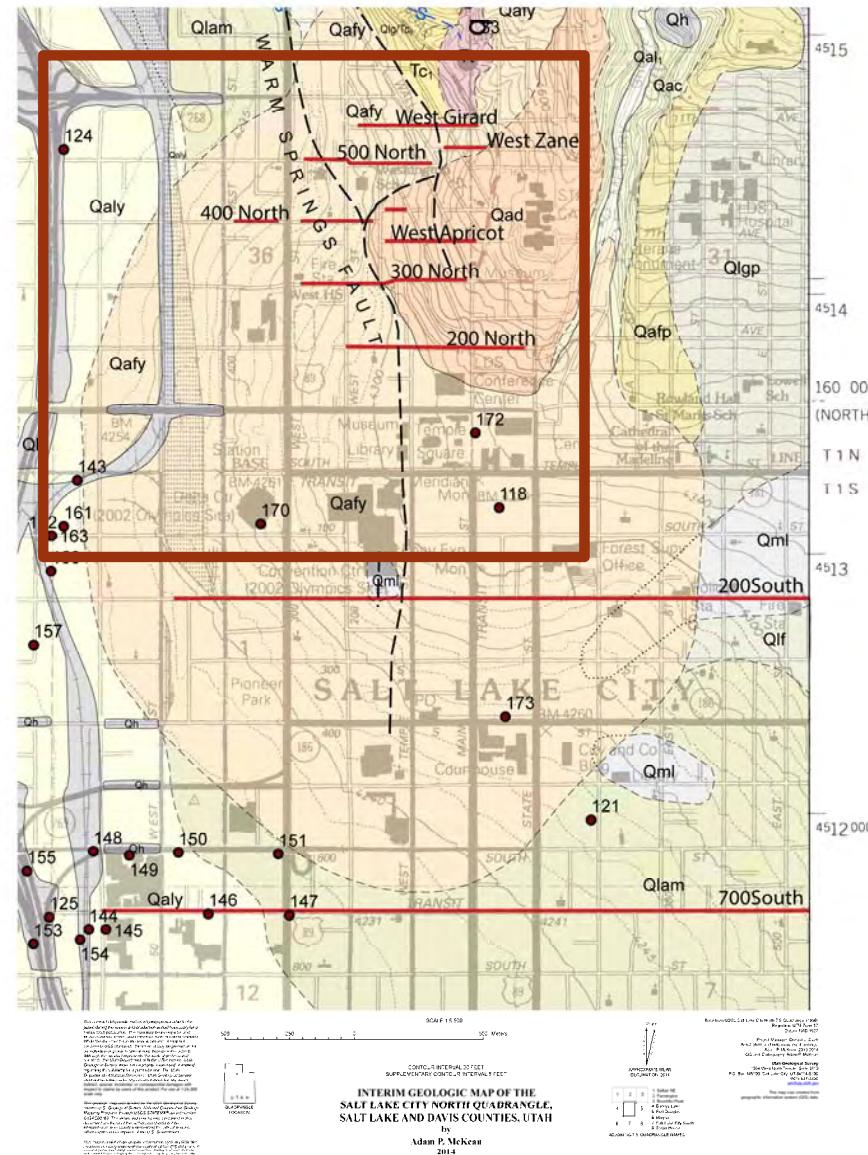
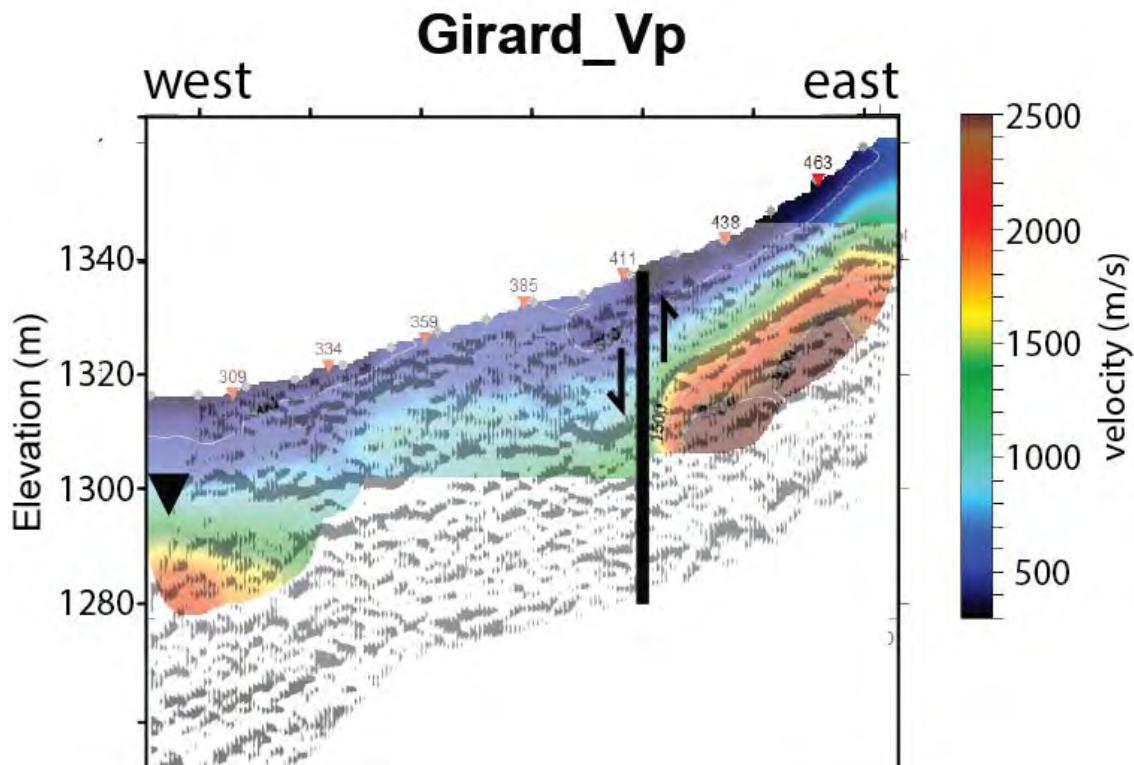
South

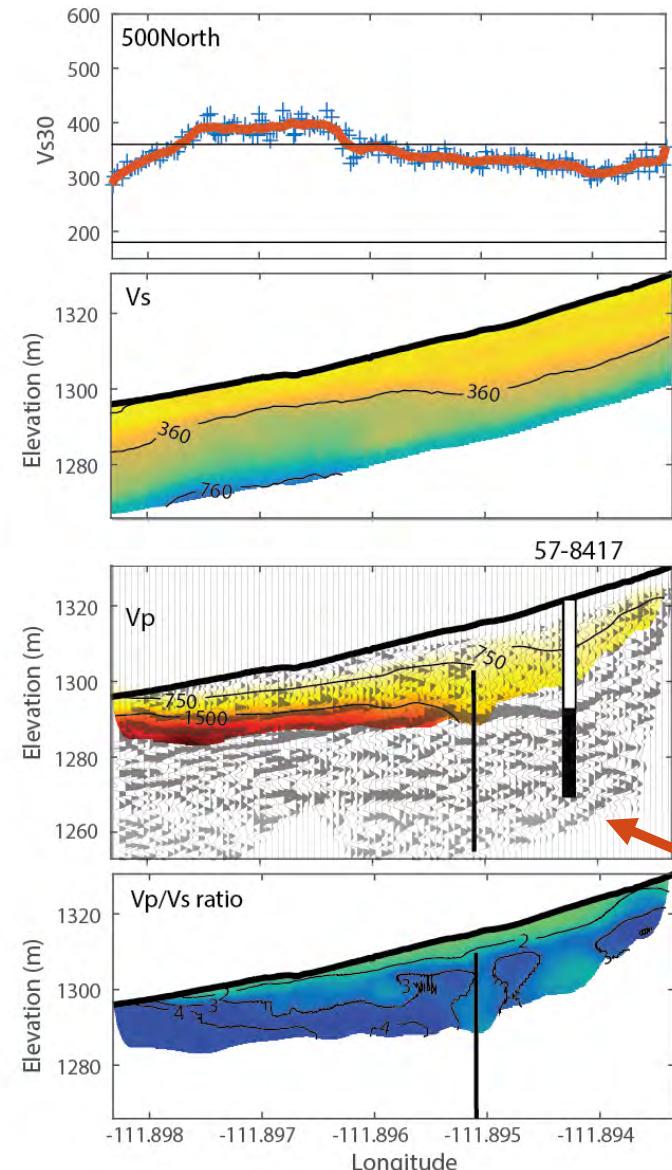


200 WEST SEISMIC REFLECTION/REFRACTION

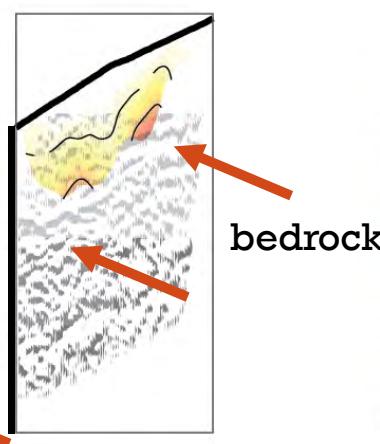


WEST GIRARD (20 M DEEP BEDROCK)

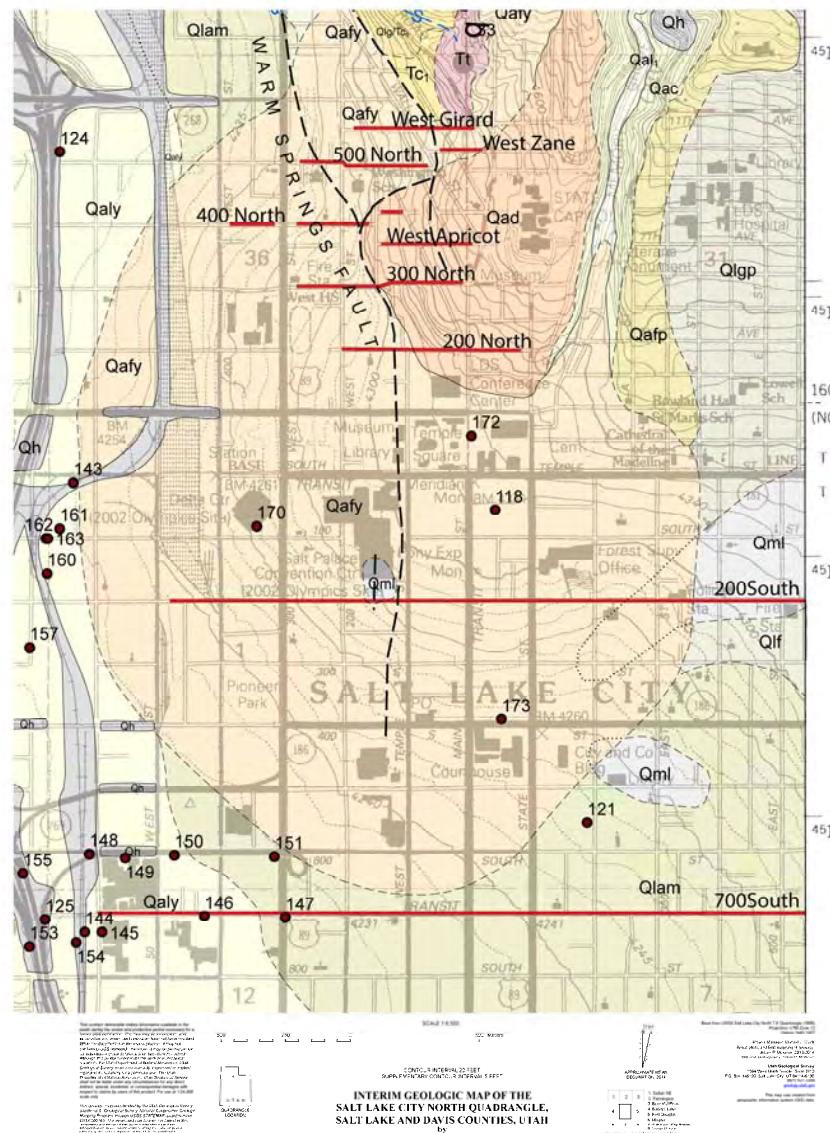


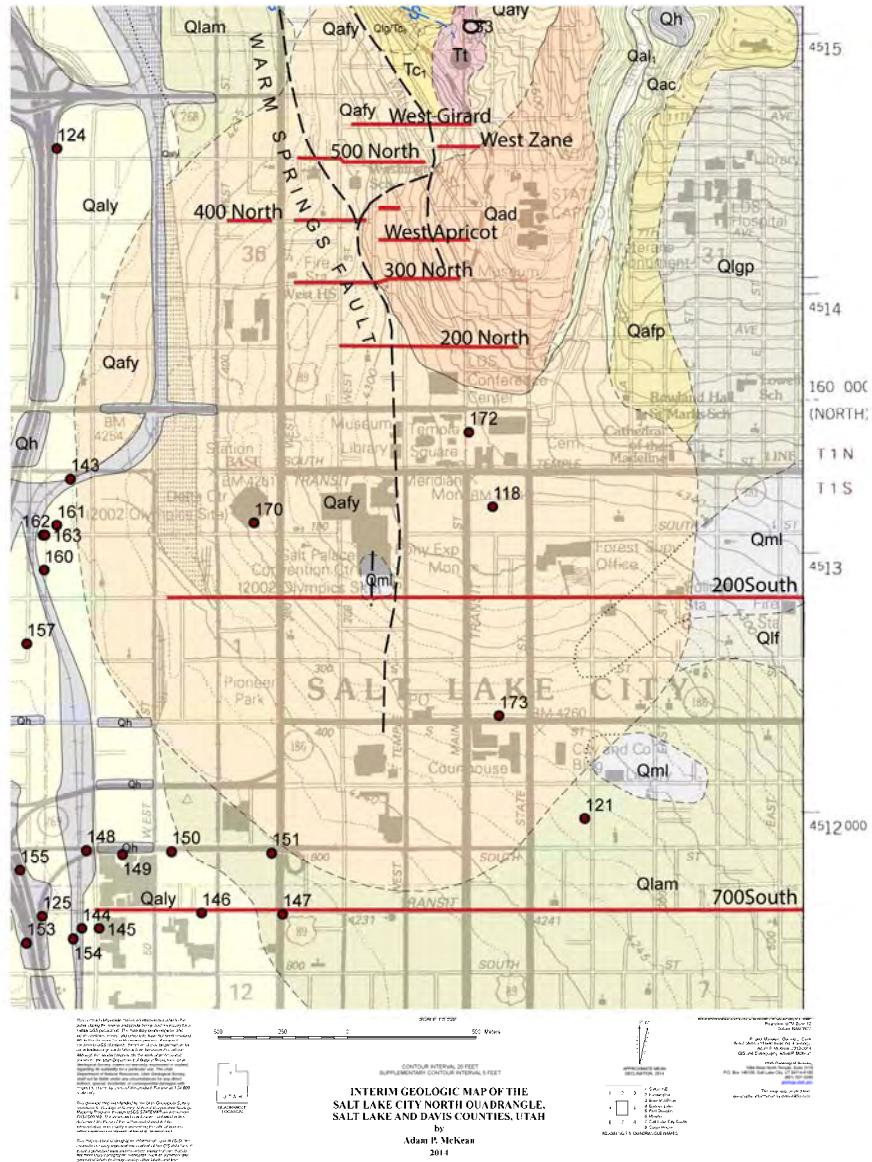


500 NORTH ZANE PROFILES

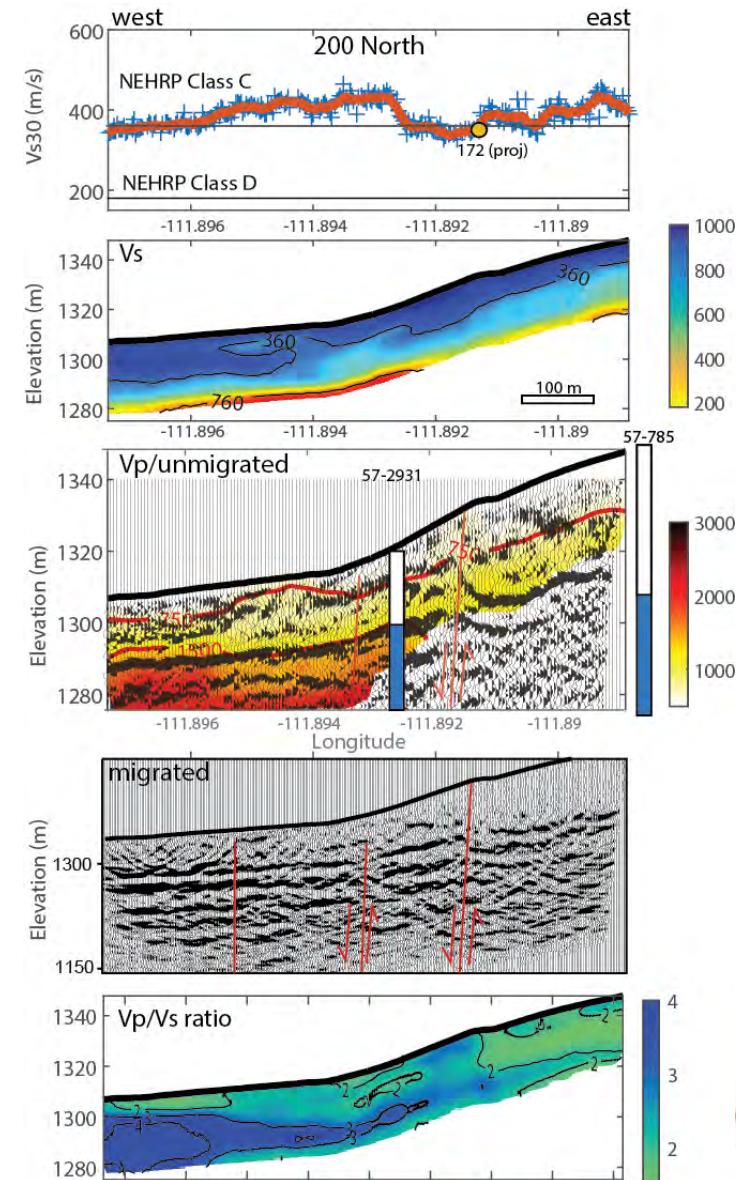


bedrock





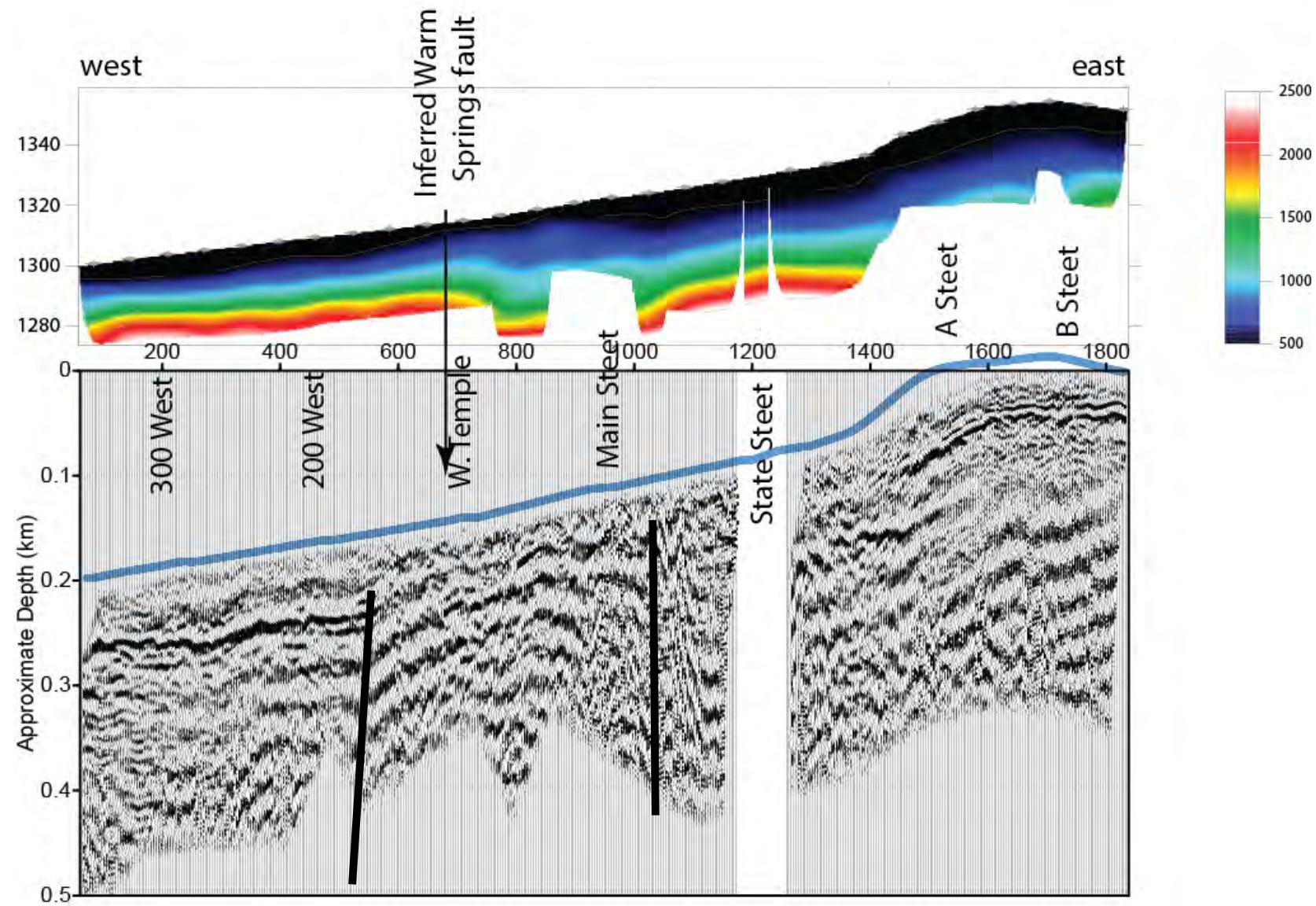
200 NORTH PROFILE

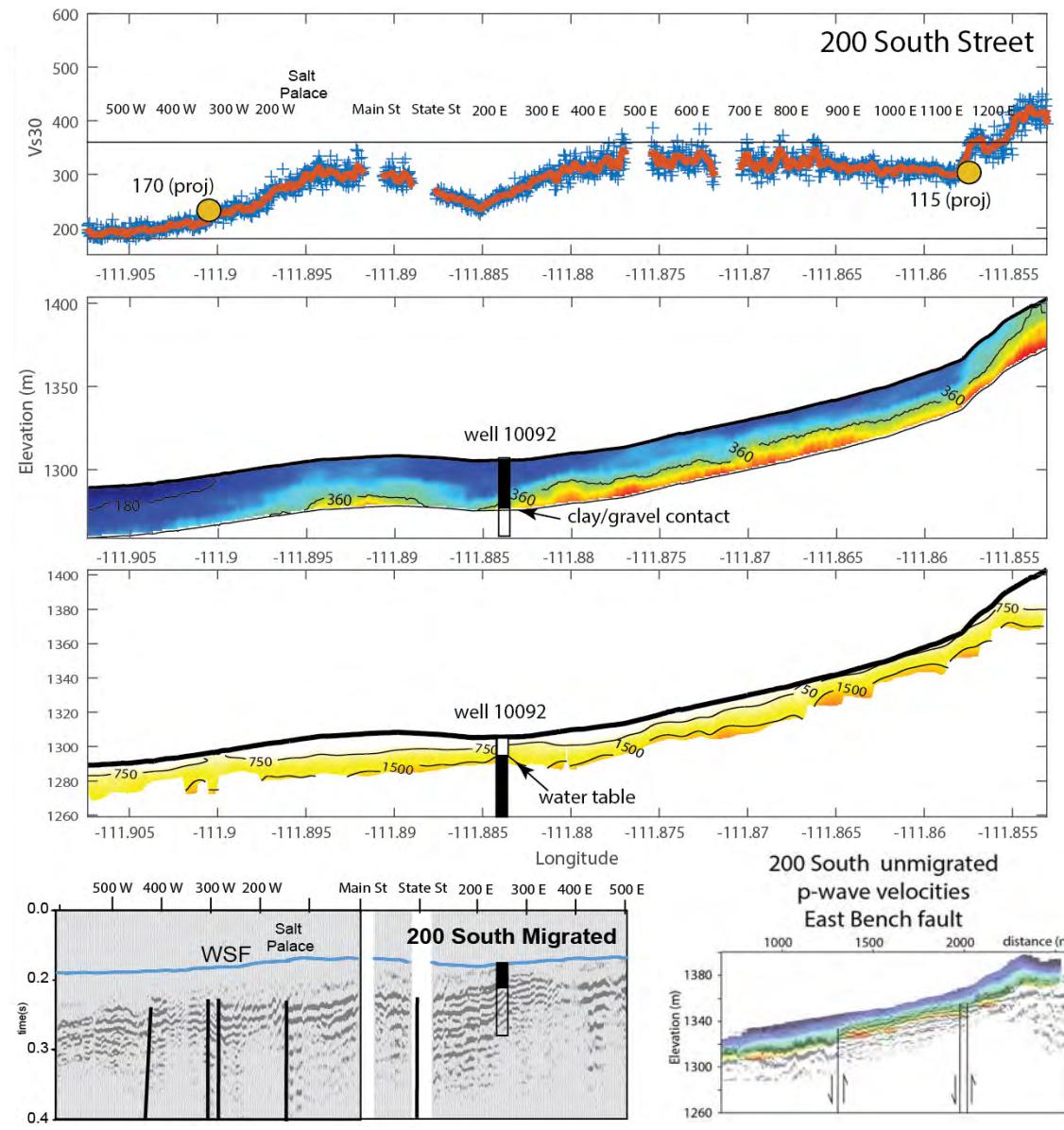
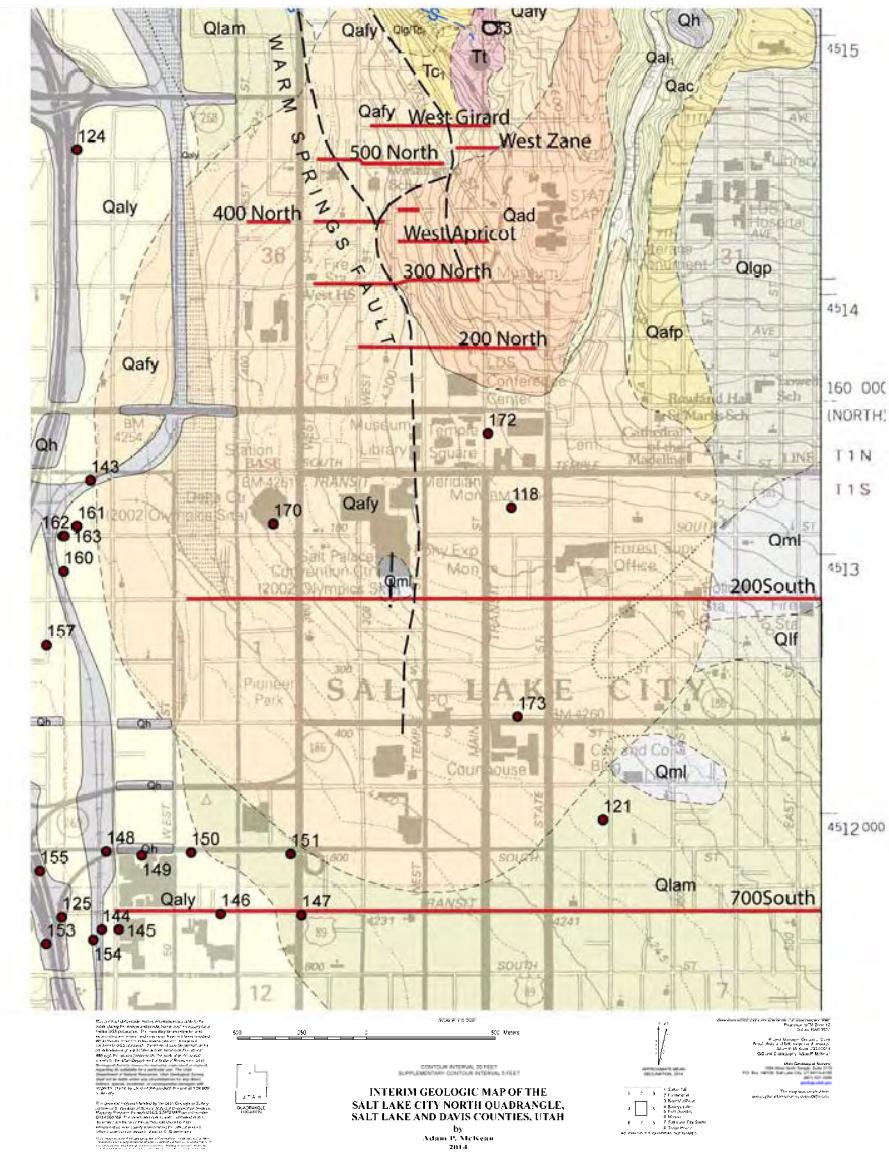


NORTH TEMPLE

Step in water table beneath West Temple

Fault beneath Main Street

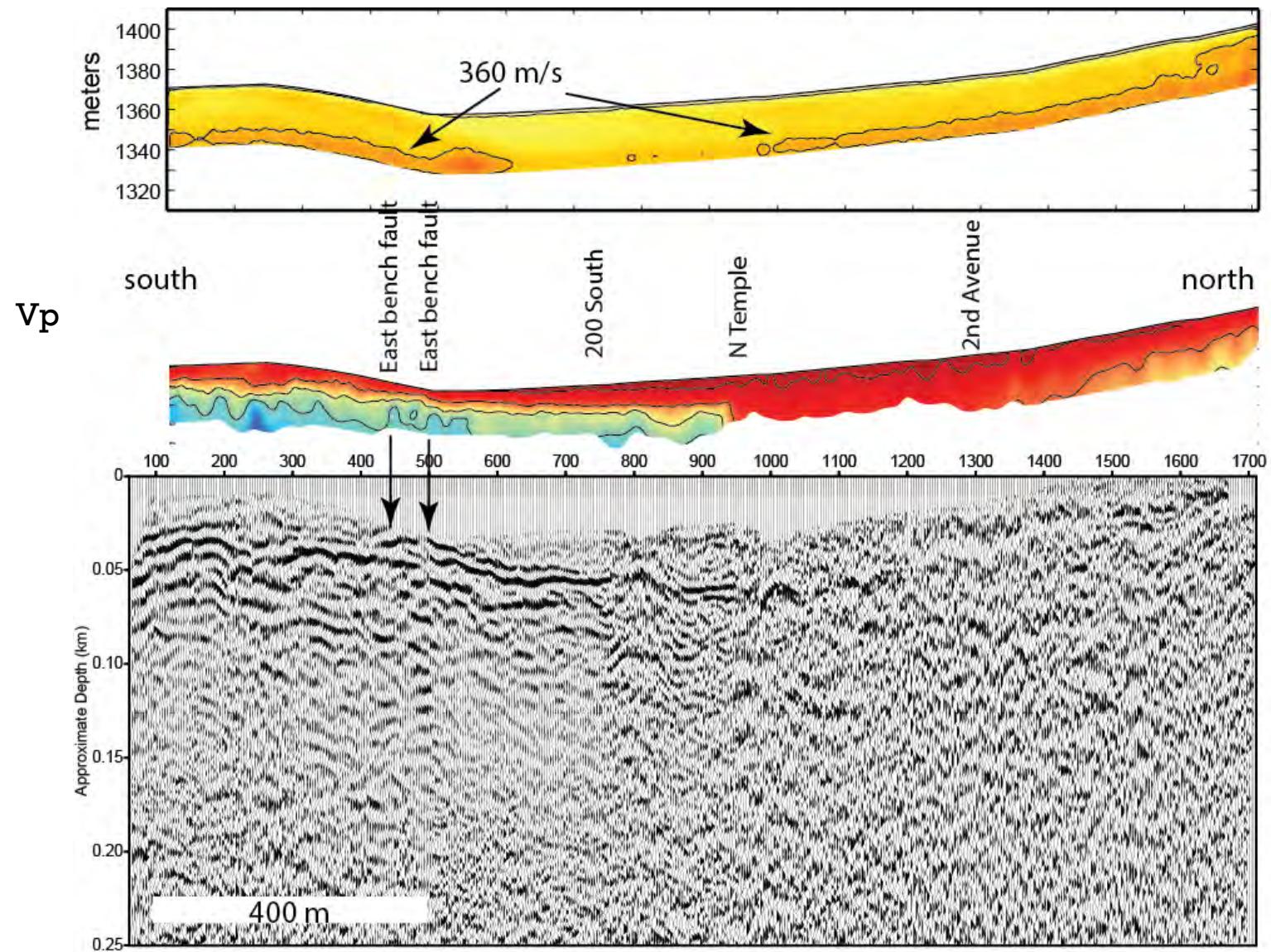


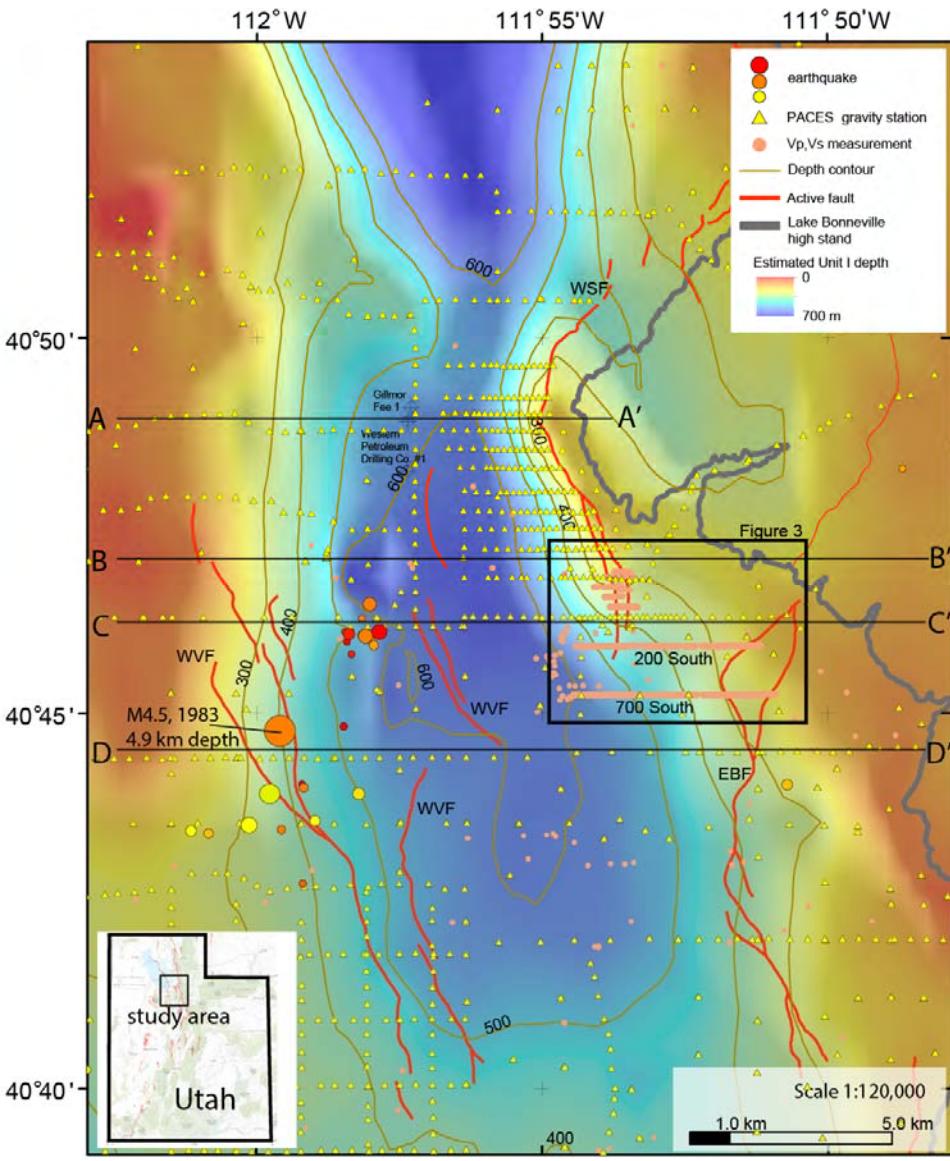


1100 EAST

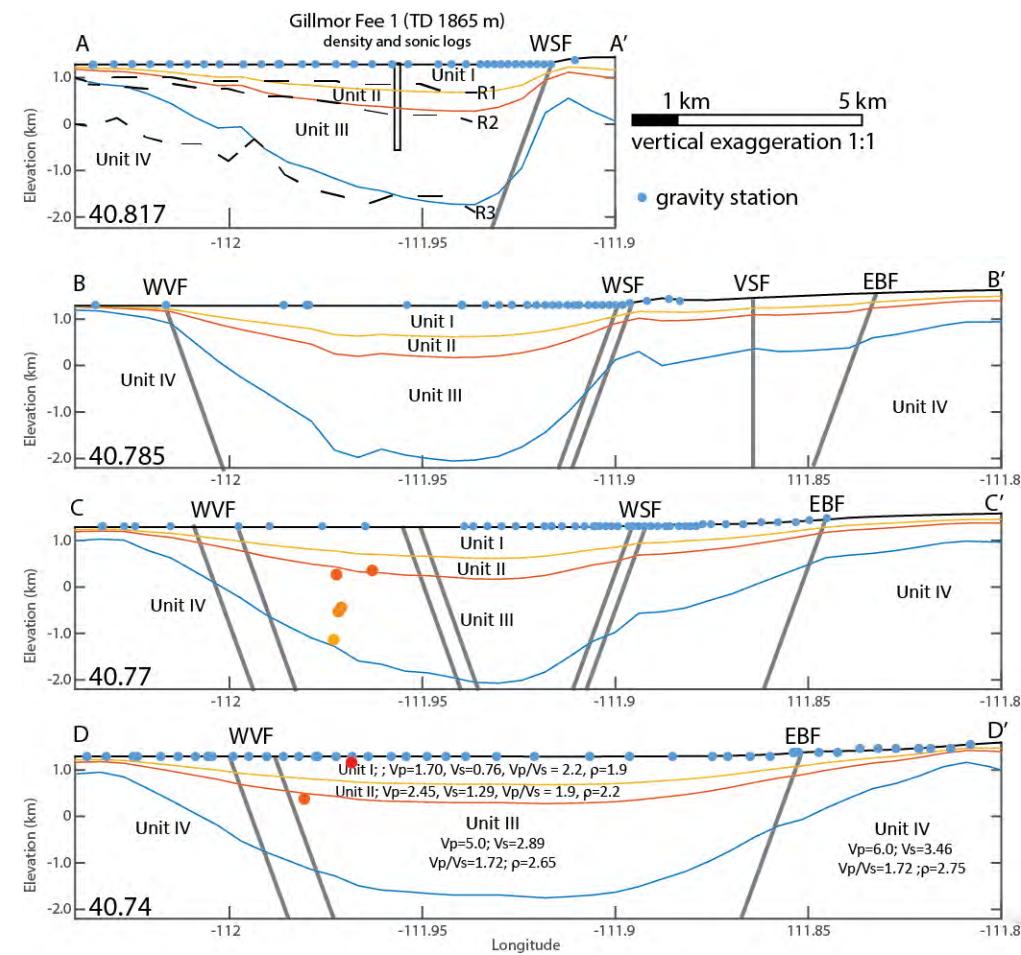
Seismic character changes beneath North Temple (fault?)

Shallow water table to the south
Deeper water table to the north

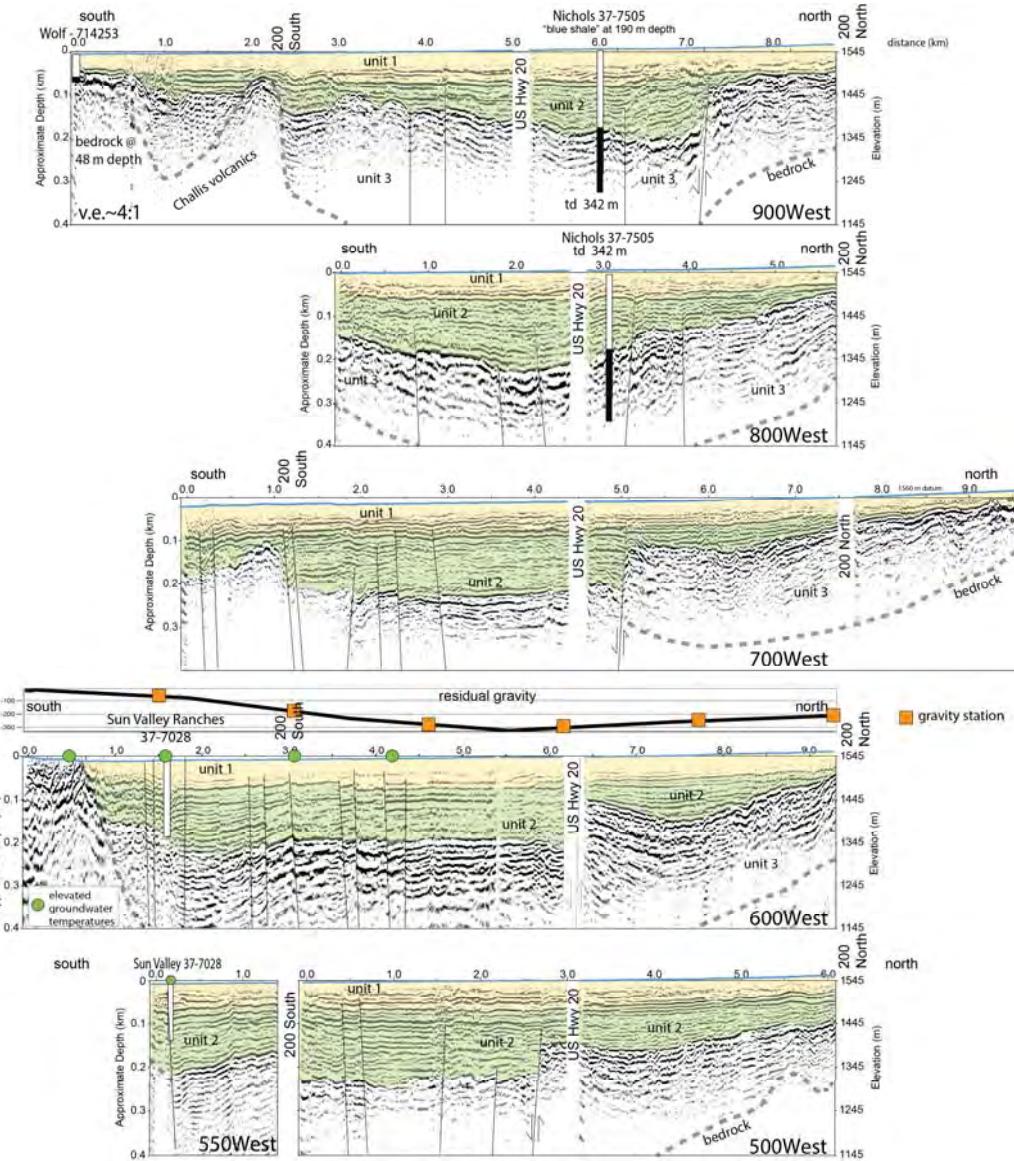




GRAVITY MODELS FOR WASATCH FRONT



LAND STREAMER RESULTS FROM IDAHO – CAMAS PRAIRIE





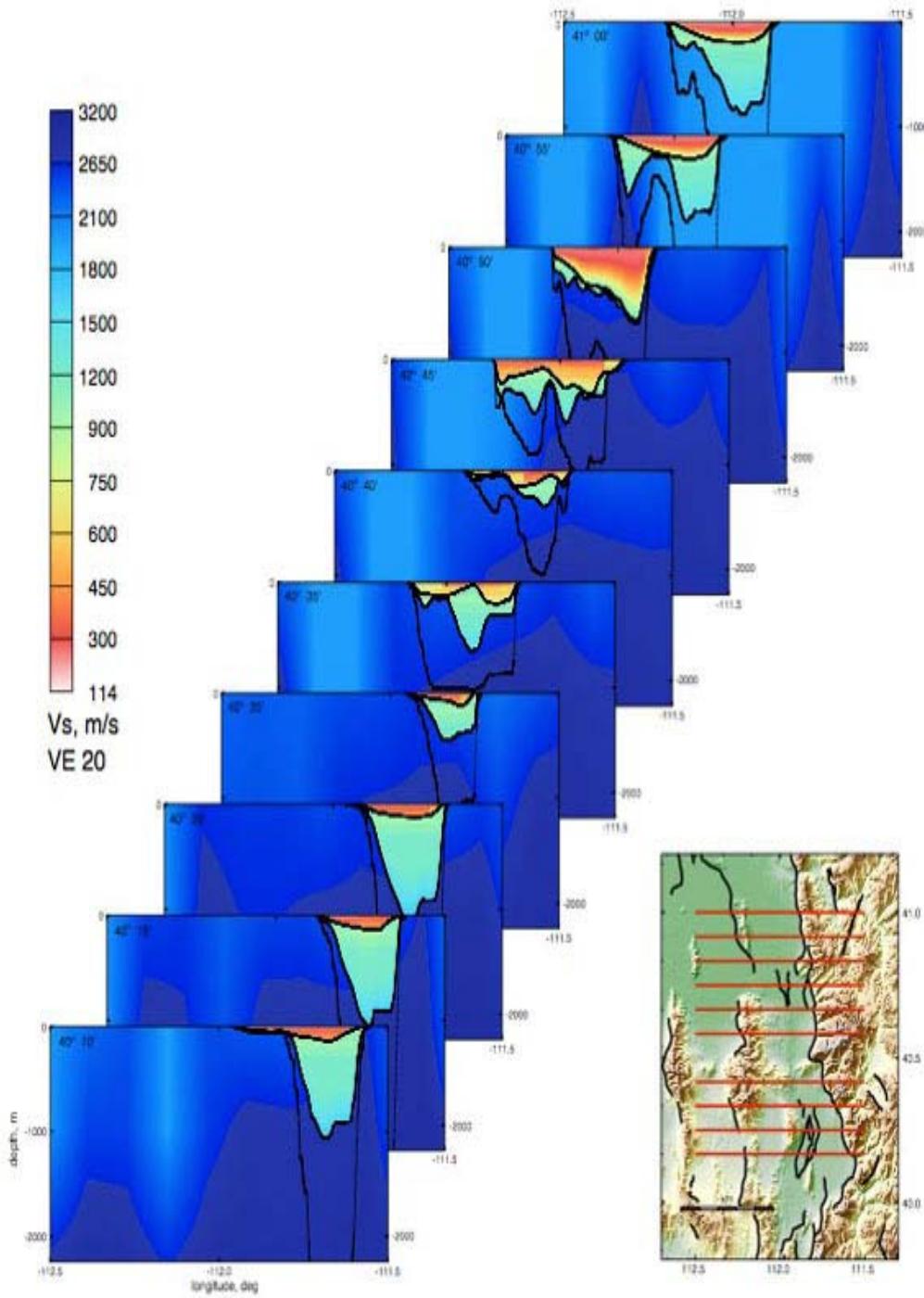
Wasatch Front Community Velocity Model

Greg McDonald, Utah Geological Survey

Harold Magistrale, FM Global

Kim Olsen, San Diego State University

James Pechmann, University of Utah



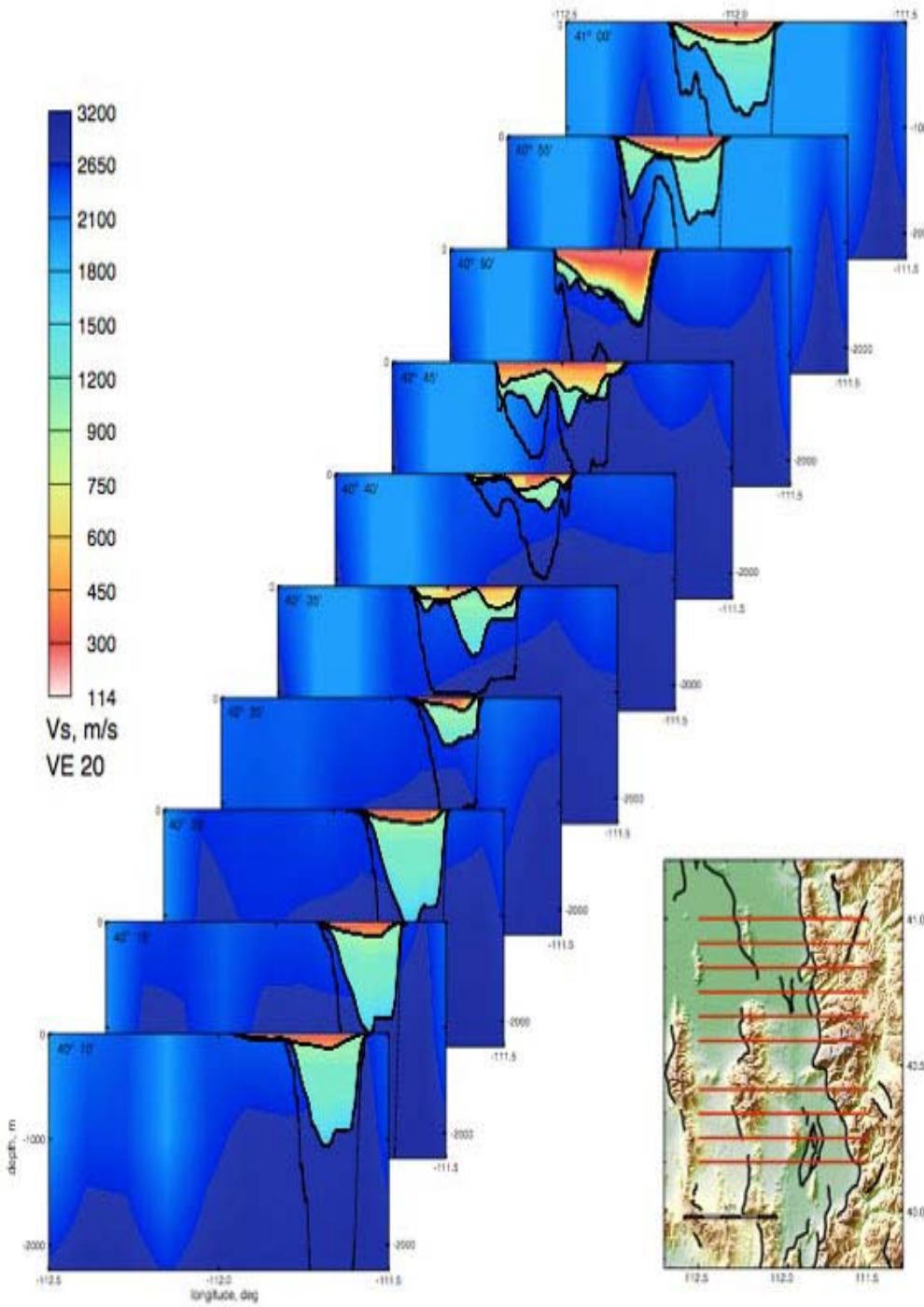
WFCVM development began
in 2004-05

Harold Magistrale, Kim Olsen, Jim
Pechmann

Based on SCEC models

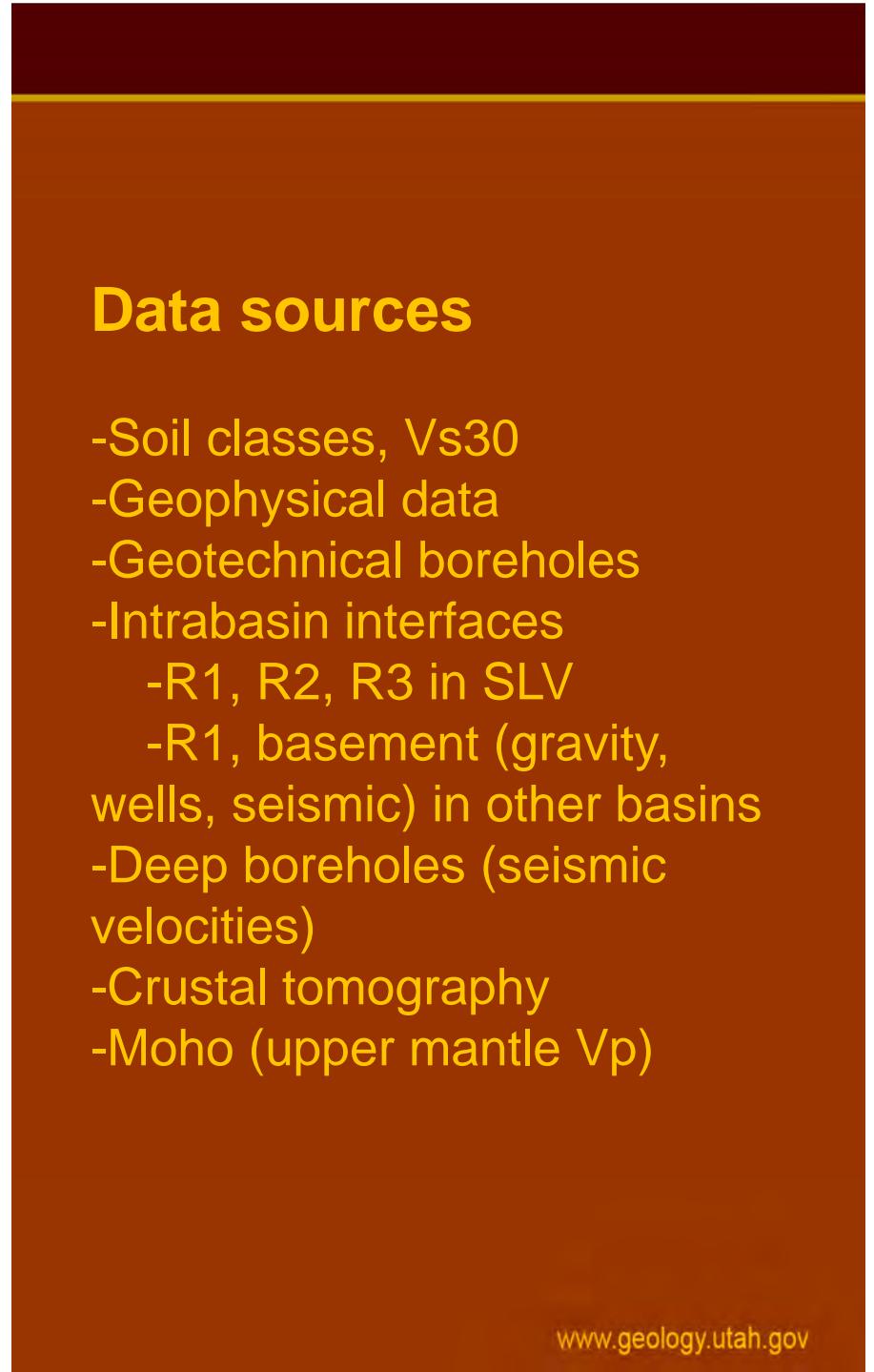
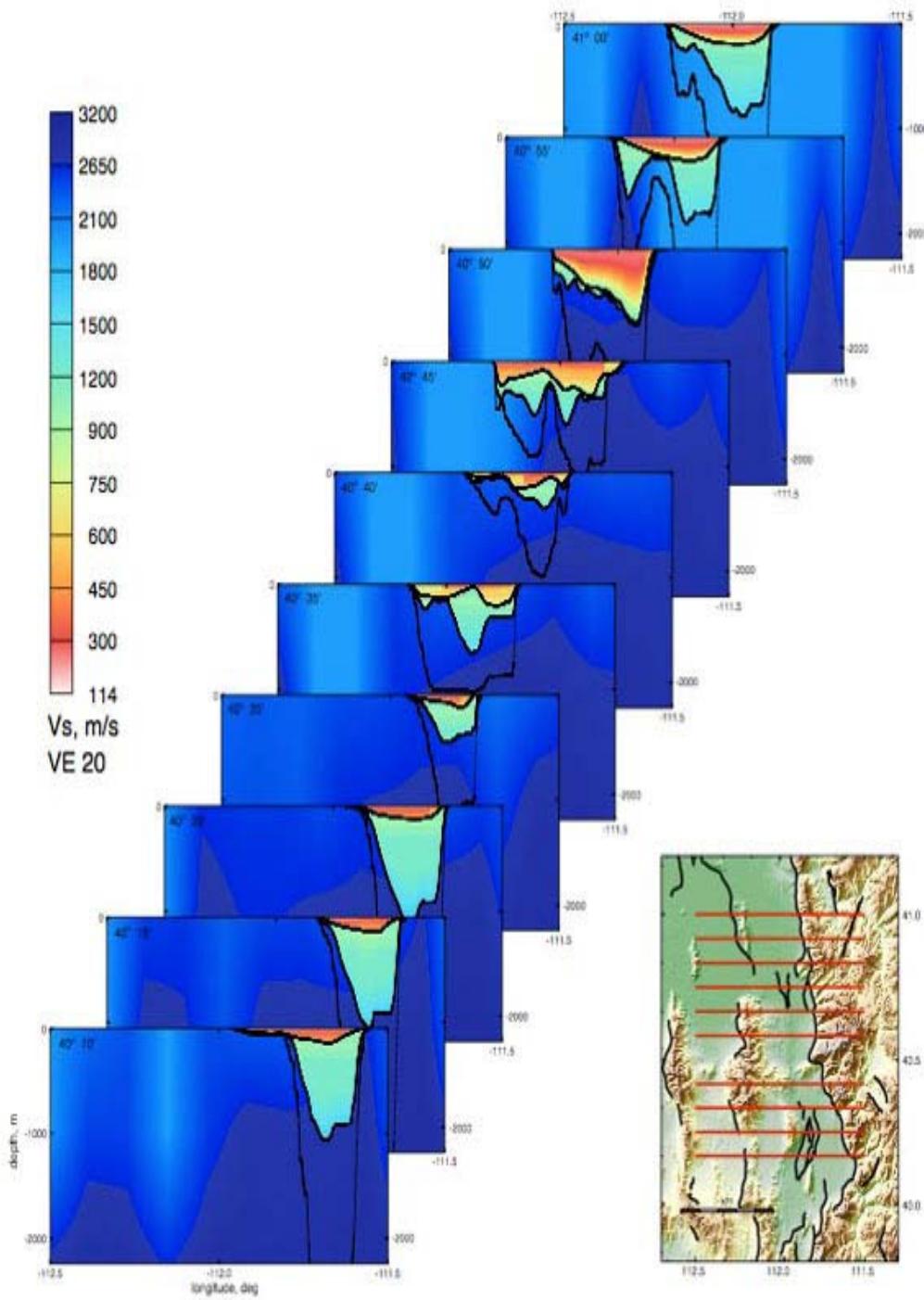
First draft submitted mid-2006
Most up-to-date version 3d
(2010~14)

Validation by Olsen, Roten,
and Pechmann
USGS



What is the WFCVM?

- A 3-D velocity structure model for basins along the Wasatch Front
- Used for ground-motion modeling
- Main components
 - Surfaces
geologic contacts
gravity inversion
seismic refraction
boreholes
 - Seismic velocities
Boreholes
SASW
Empirical relations





Rule Based Seismic Velocity Model

-Compile geologic and geophysical information

examples: stratigraphy, surficial geology
oil well sonic logs
tomography results

-Define reference surfaces

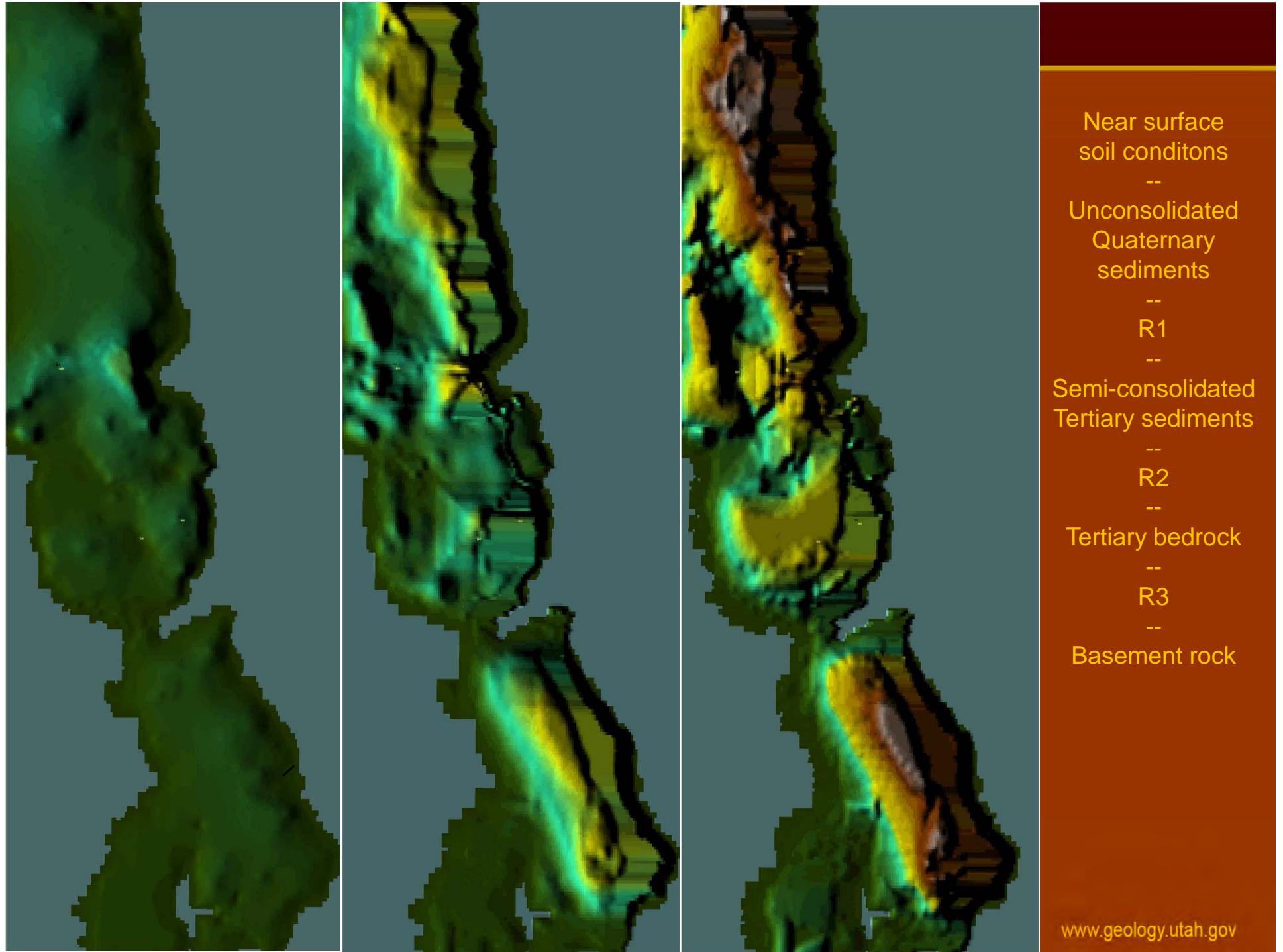
examples: lithologic contacts (isogage surface)
isovelocity surface
tomography model nodes

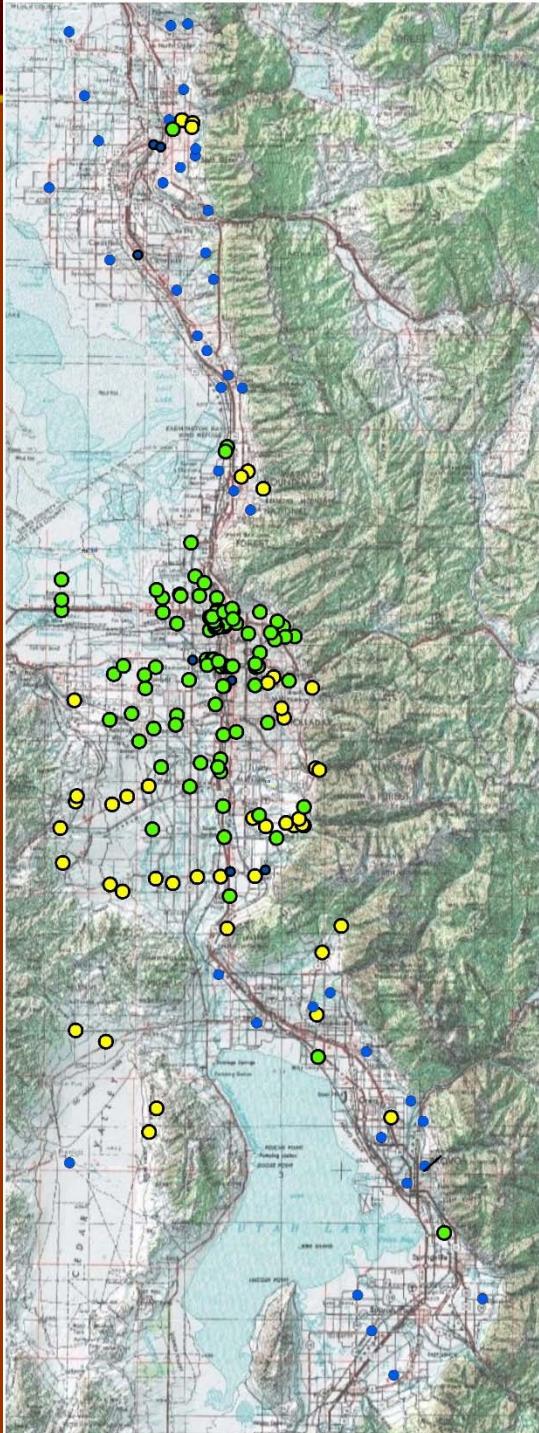
-Compare point of interest to objects and interpolate properties

examples: interpolation of age between surfaces
interpolation of velocity between tomography nodes

-Apply rule to get velocity (or other property) at point of interest

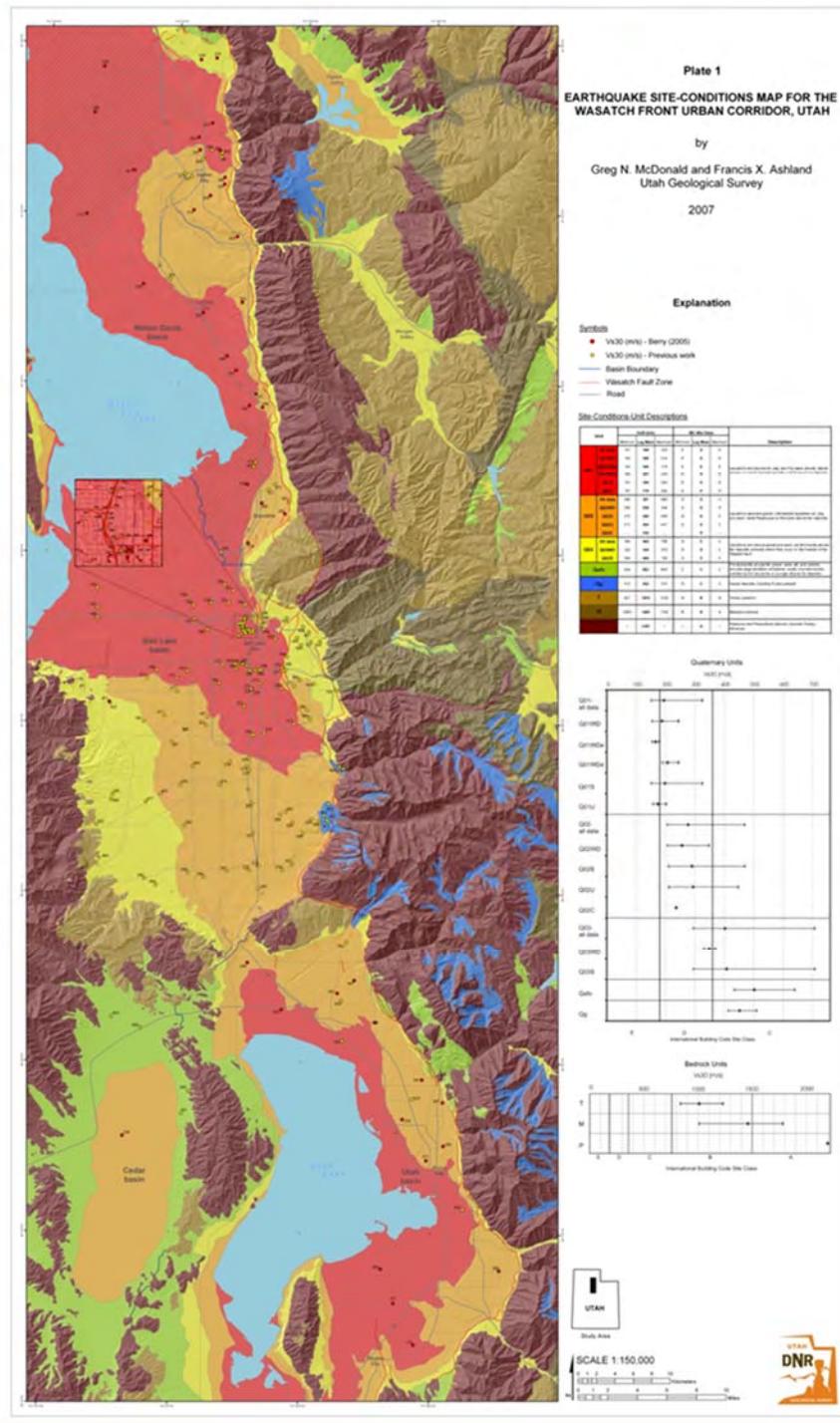
examples: Linear gradient between isovelocity surfaces
Faust's rule (velocity-age-depth relation)
 $V_p=k(da)^{1/6}$



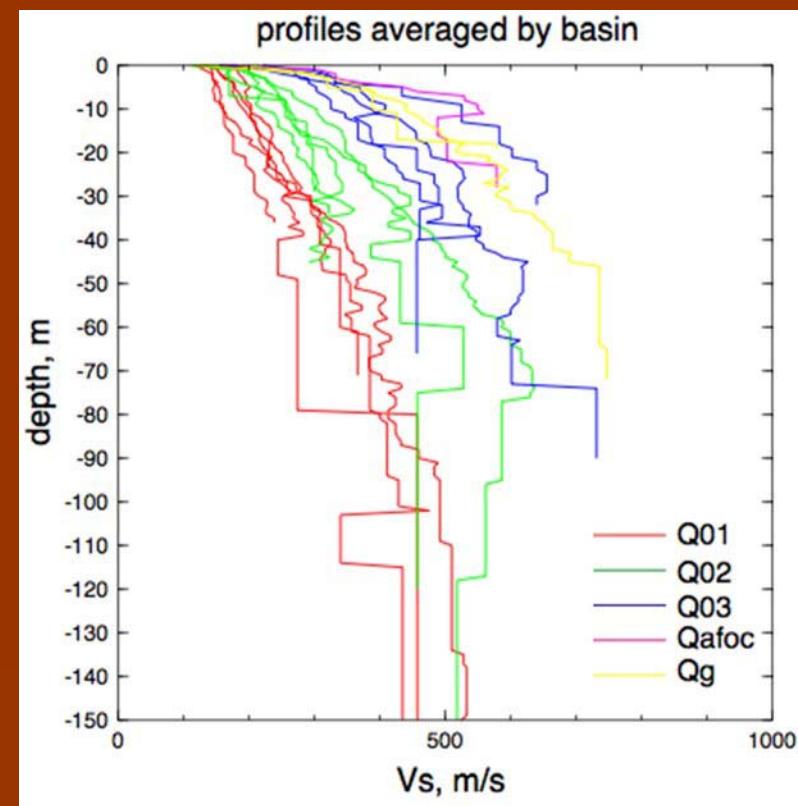


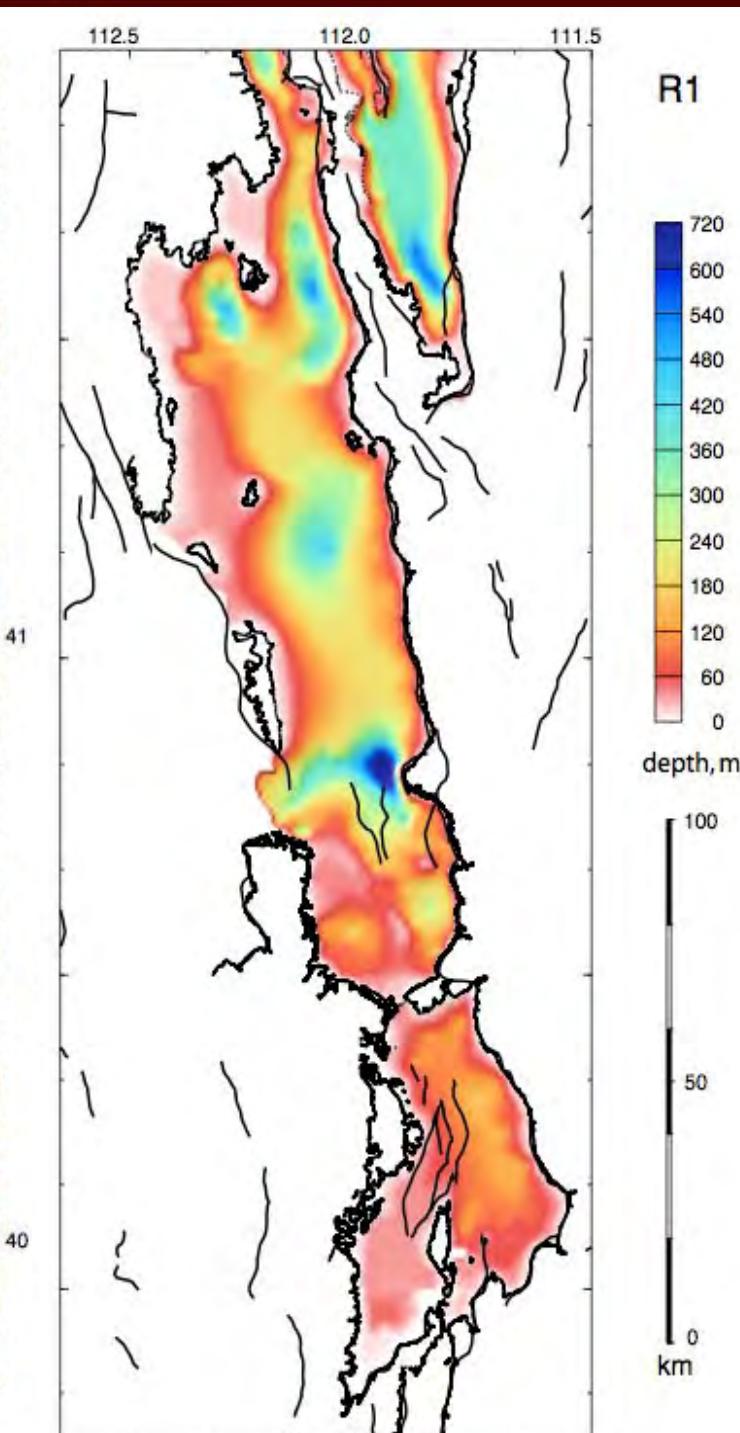
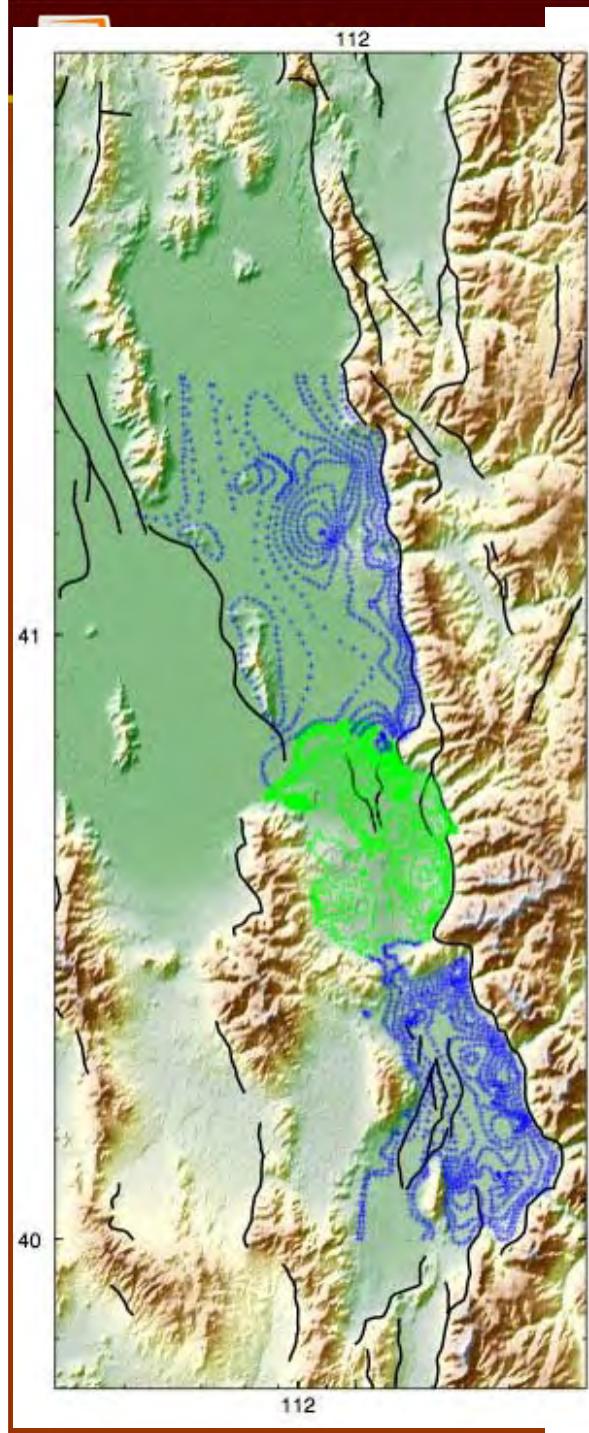
Soil conditions

- Surficial geology
- Vs30
 - Compiled from literature and consultant's reports
 - Crosshole/Downhole
 - CPT
 - SASW
 - Vs collection campaigns
 - SASW – USU Jim Bay and students
 - USGS seismic
- 204 sites total
 - 139 - Salt Lake basin
 - 24 - Weber basin
 - 16 - Davis basin
 - 20 - Utah basin
 - 5 - Cedar Valley

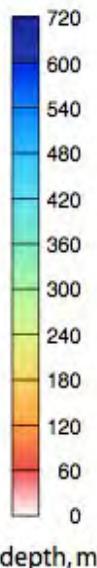


Mapped site-conditions units
 Unit extents from surficial
 geology
 Mean Vs30 to relate to IBC
 site classes



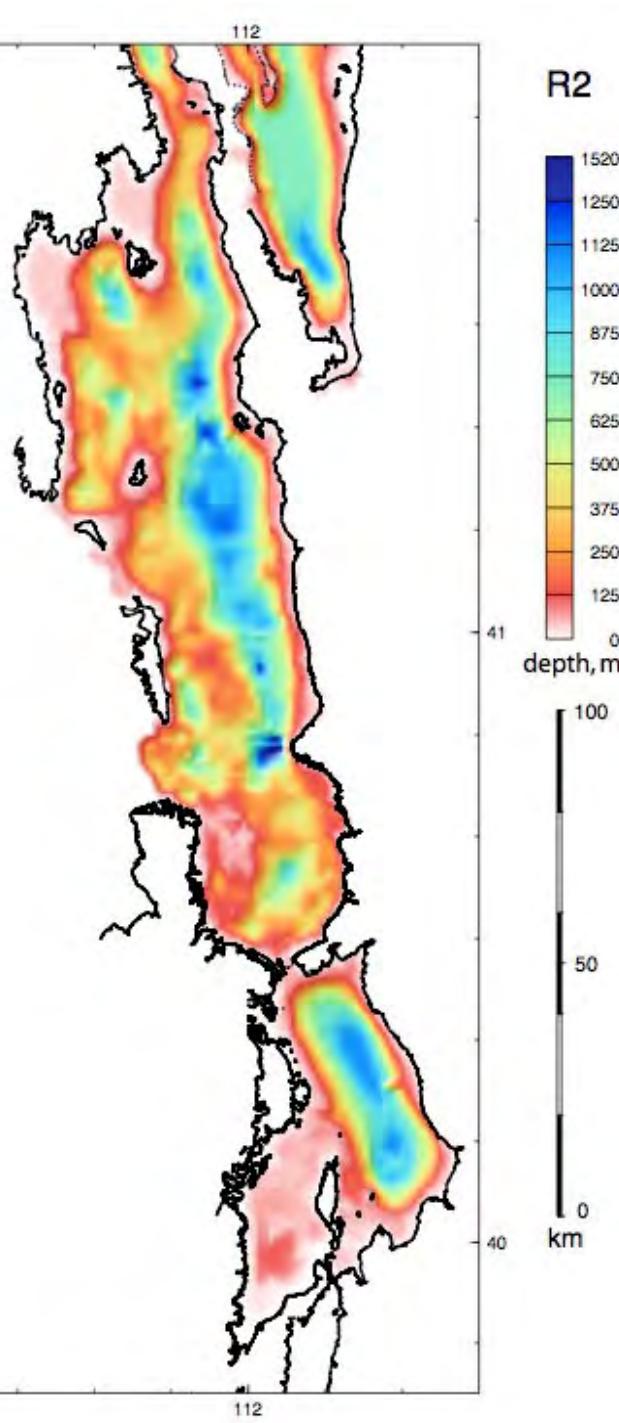
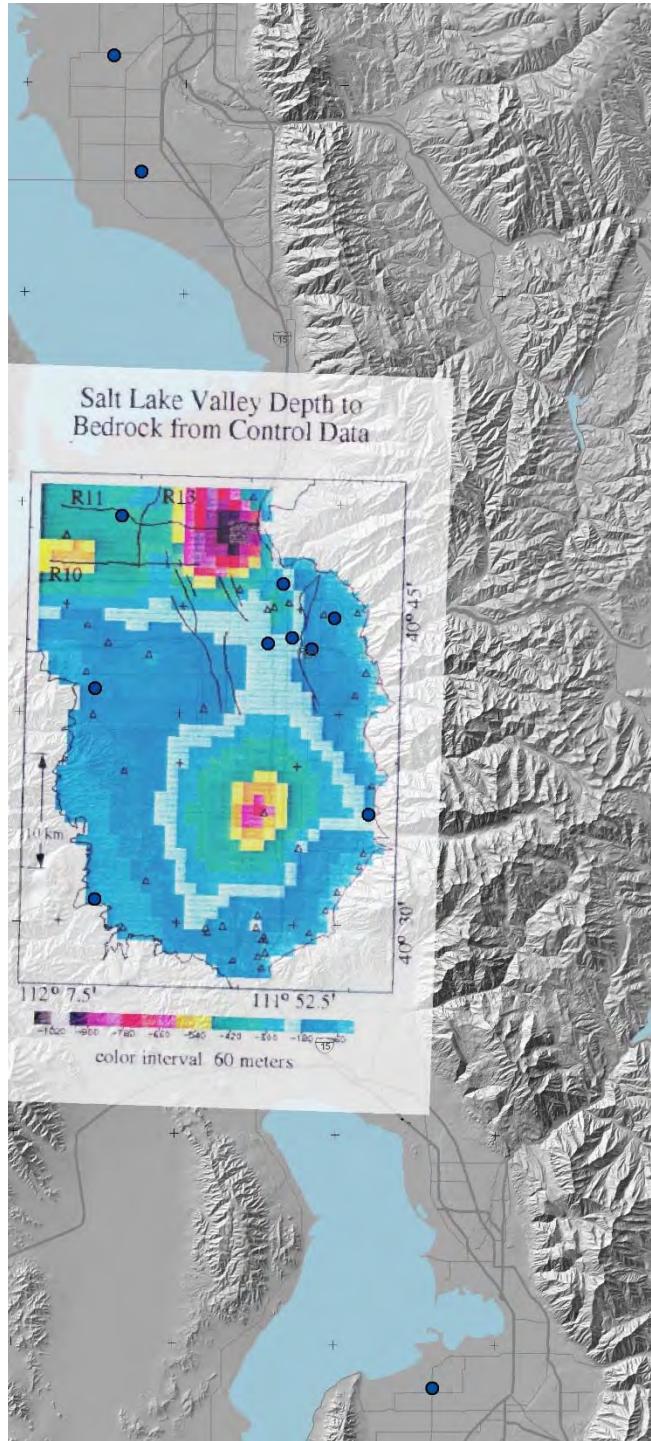


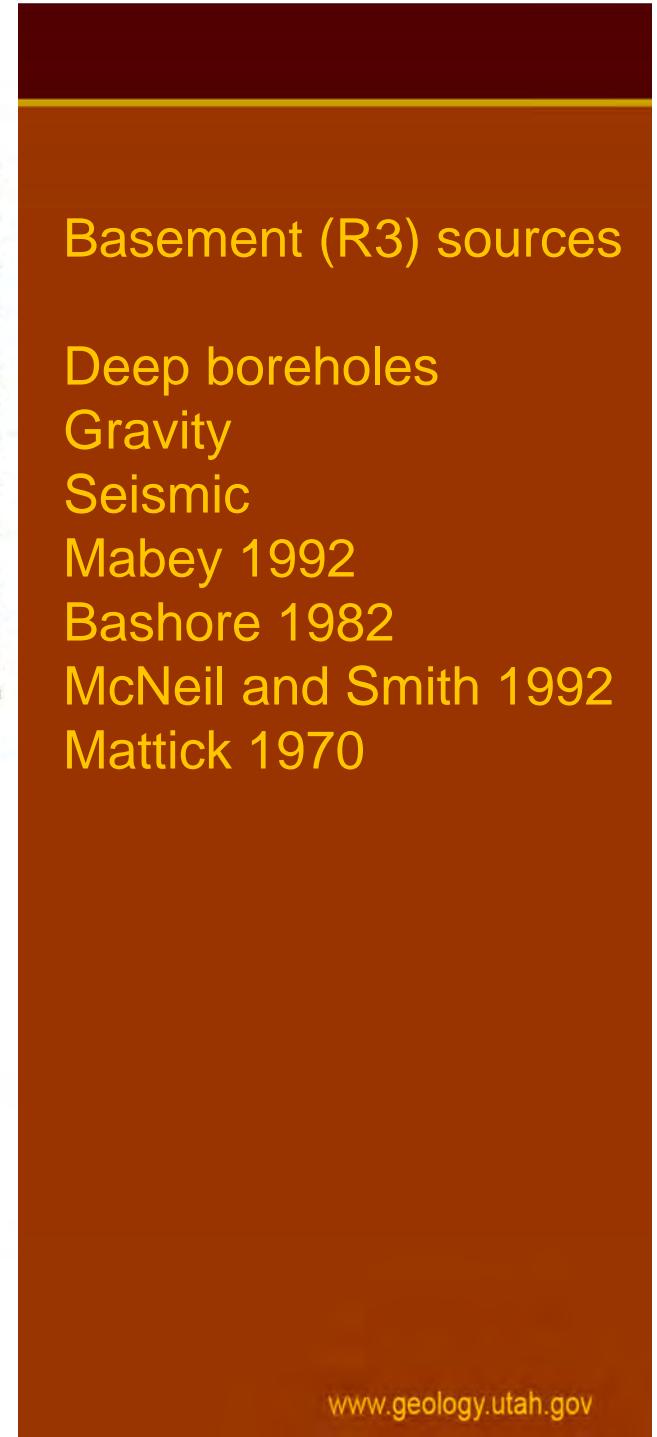
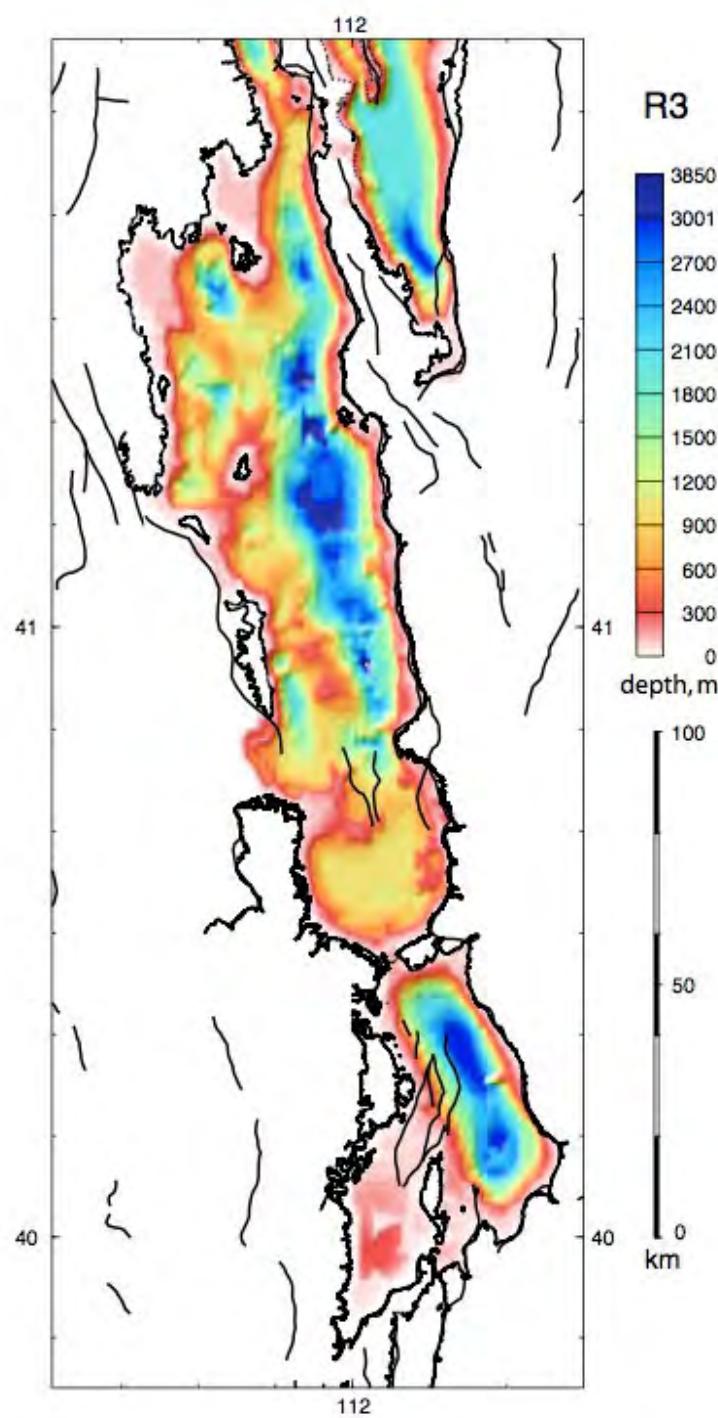
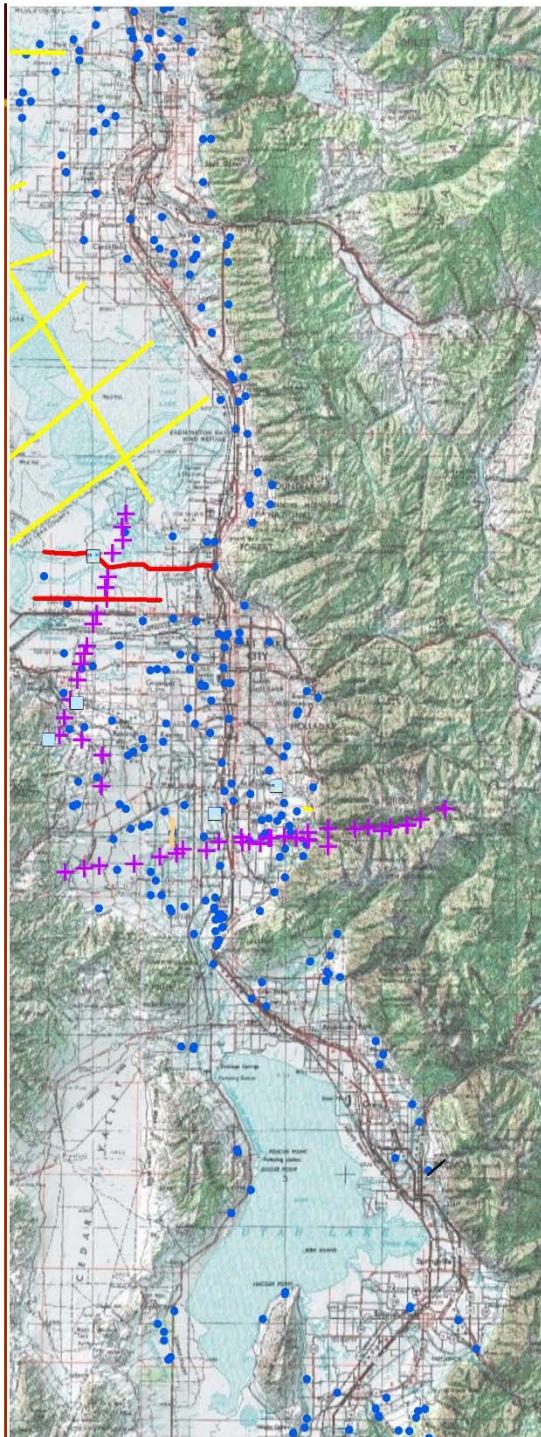
R1



R1 sources

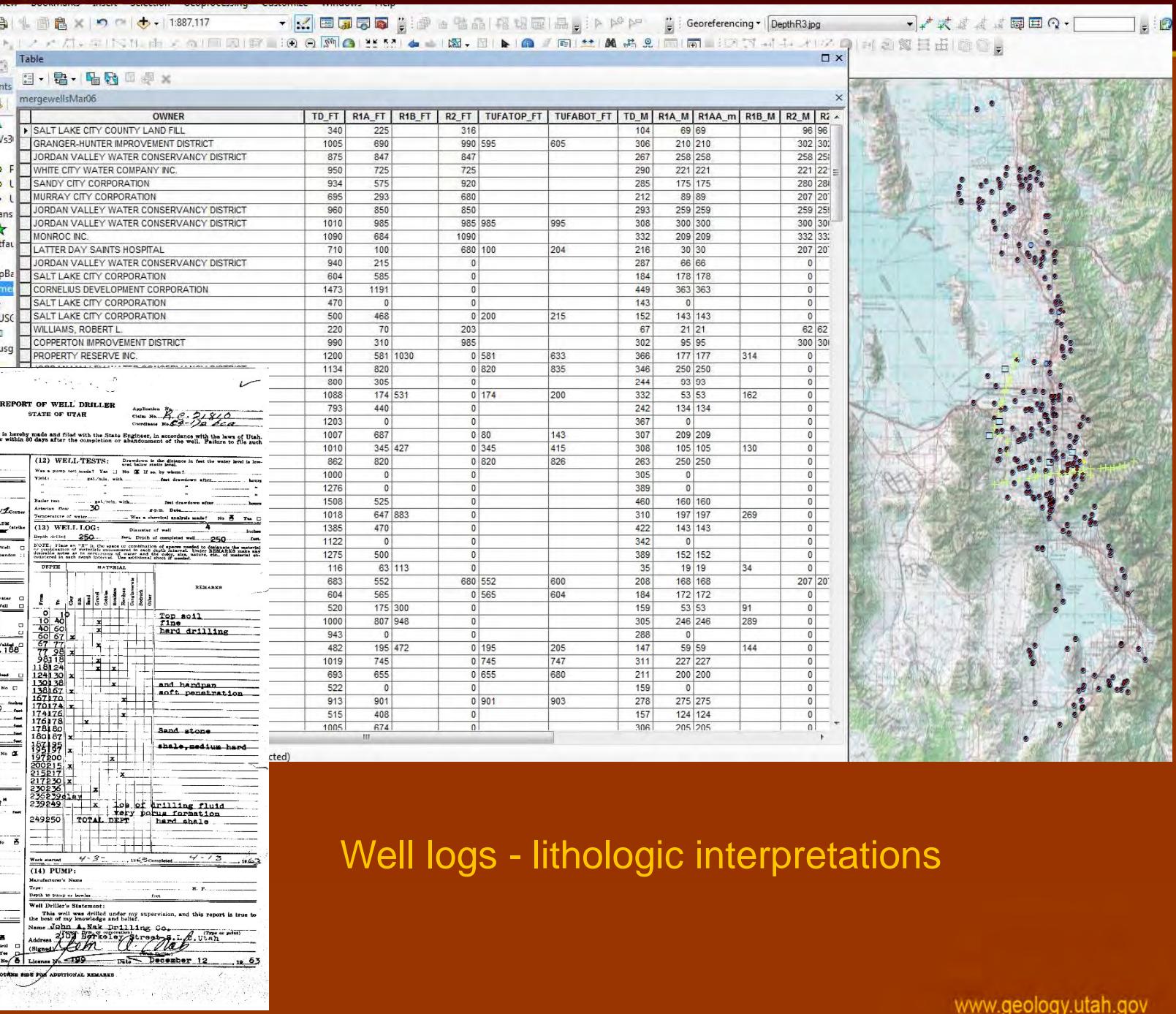
Deep boreholes/water rights wells
Seismic Vs profiles
(Solomon et al 2004
Wong et al 2002)





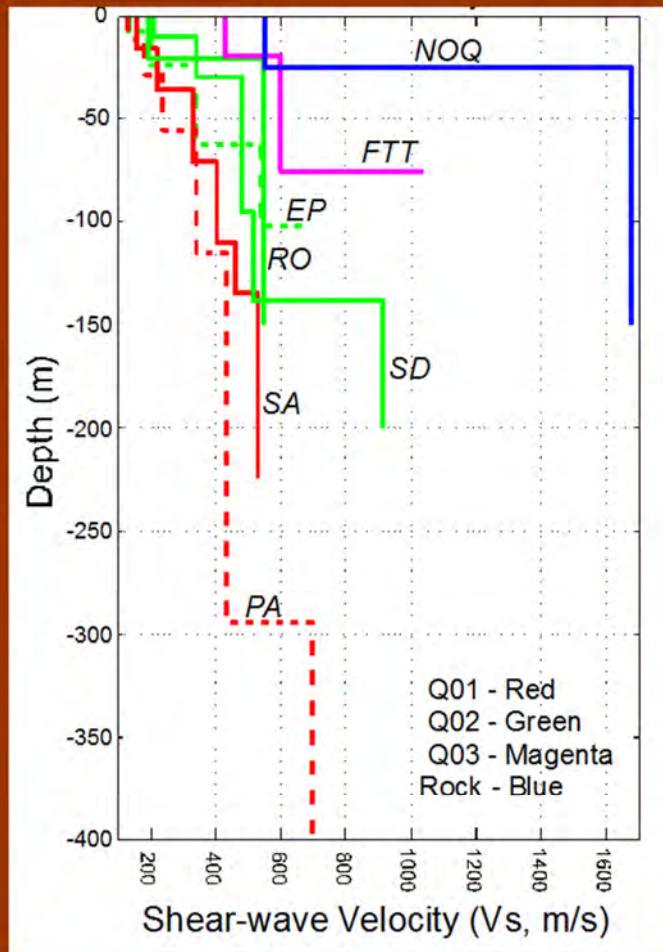


UTAH



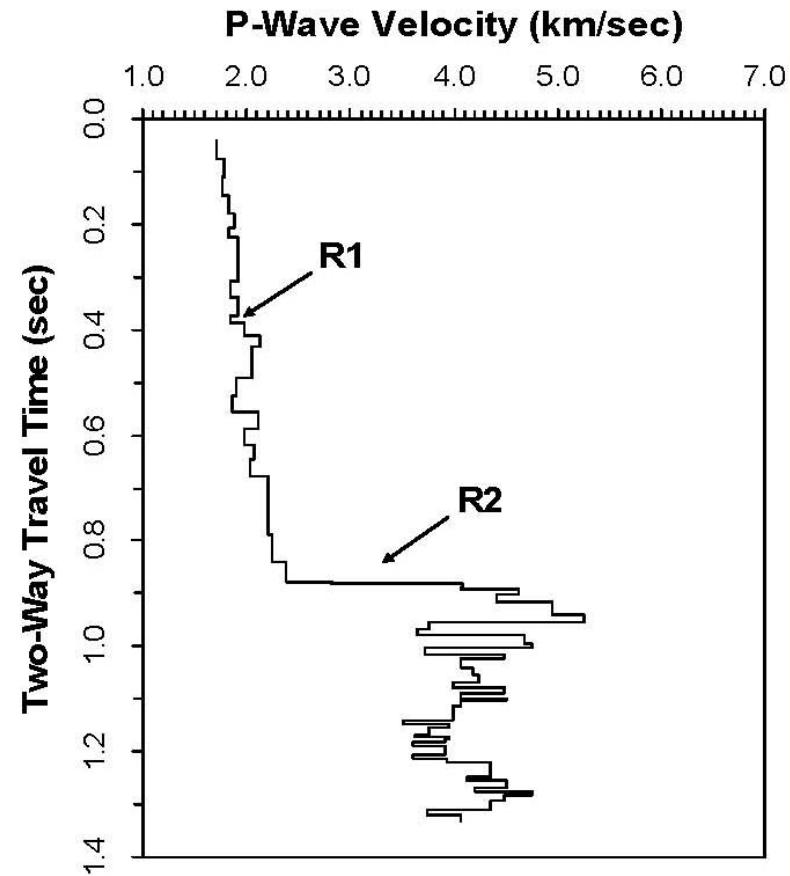


UTAH GEOLOGICAL SURVEY



S-wave minivibe soundings
W. Stephenson, R. Williams, J. Odum, D. Worley,
R. Dart (USGS) J. McBride (BYU)

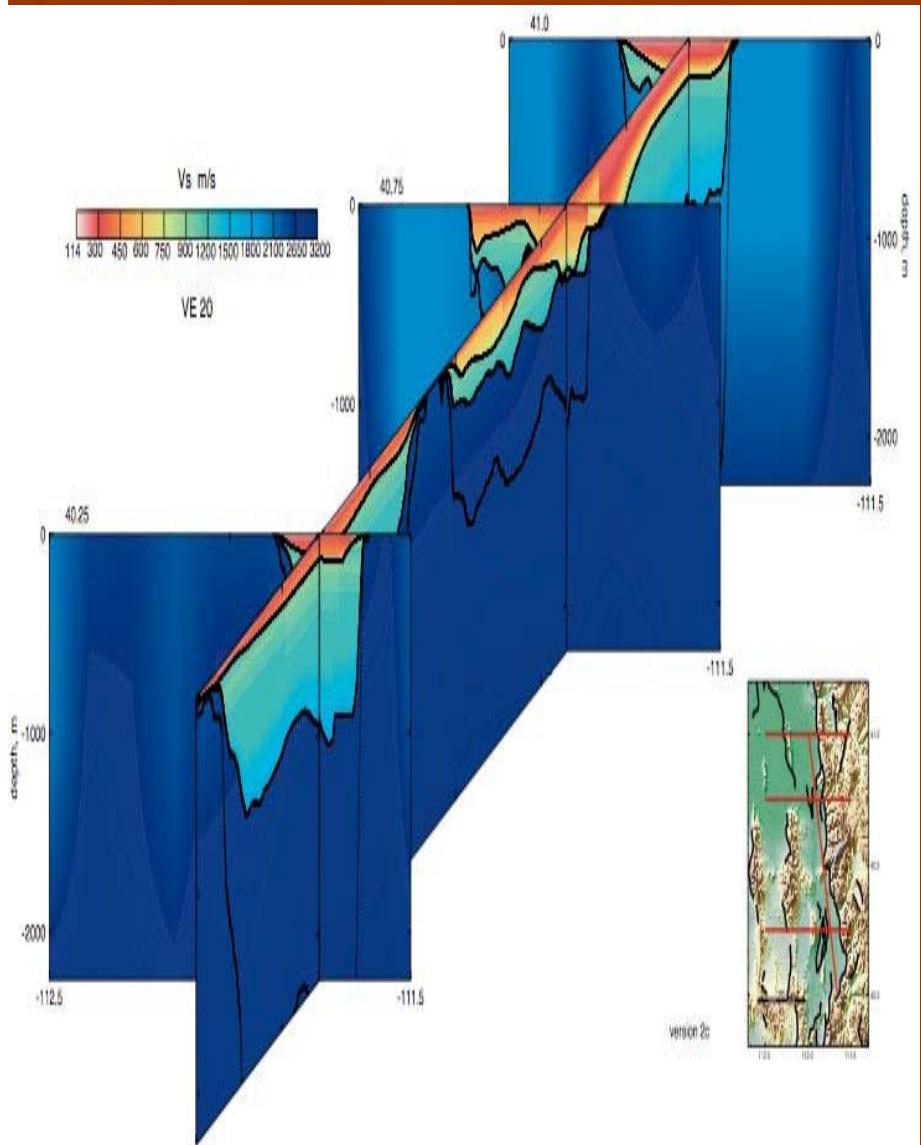
GILLMAR FEE 1: API No. 4303530001



Sonic Logs
J. Pechmann, K. Jensen (UofU), H. Magistrale (FM Global)



UTAH GEOLOGICAL SURVEY



Above R1

- soil classes, Vs
- Vp from piecewise linear fits to geometric mean sonic log profiles
- If Vs geotech, Vp from modified mudline

R1-R2

- Vp from piecewise linear fits to geometric mean sonic log profiles
- If Vs geotech, get Vp from original sigma

R2-R3

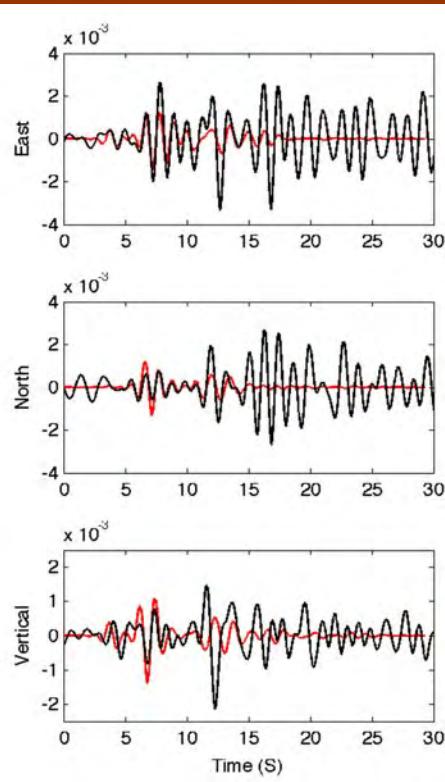
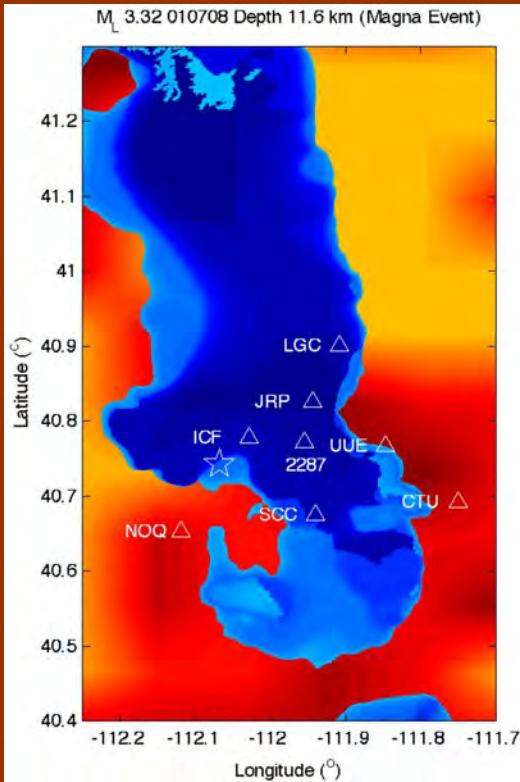
- Sonic logs R2-R3 gradient
- R2 to R3 Vp from Faust's rule (velocity-age-depth relation)

Basement:

- Use Vp from sonic logs 0 to 4 km depth, taper to tomographic Vp between 4 and 5 km depth
- Vp/Vs gradient 2.0 to 1.74 from 0 to 1 km depth



UTAH GEOLOGICAL SURVEY



WFCVM validation

Olsen, Roten, Pechmann
2006

Moschetti, Ramirez-Guzman



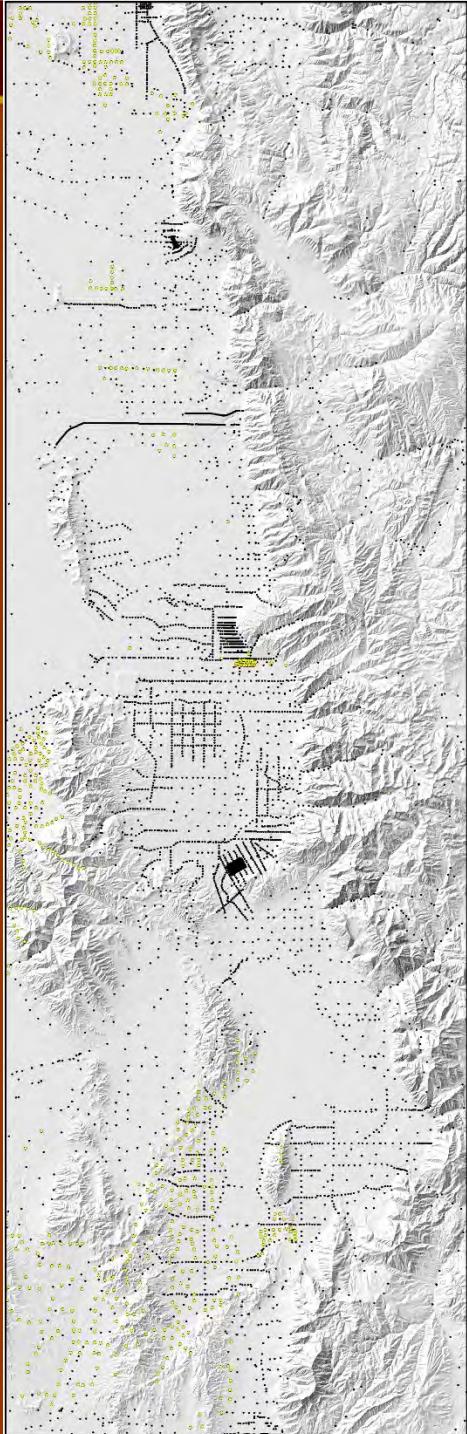
WFCVM has been used by several modeling groups:

Ground Motion Predictions from 0-10 Hz for M7 Earthquake on the Salt Lake City Segment, D. Roten, K. Olsen, H. Magistrale, J. Pechmann, V. Cruz-Atienza

3D Nonlinear Earthquake Ground Motion Simulation in the Salt Lake Basin, J. Bielak and R. Taborda

Ground Motions in the Salt Lake Basin from Dynamic Modeling of a M7 Earthquake on the Wasatch Fault, R. Archuleta, Q. Liu, R. Smith, and C. Puskas

Long period ($T > 1\text{-s}$) earthquake simulations
M. Moschetti, S. Hartzell, L. Ramirez-Guzman, A. Frankel, S. Angster, W. Stephenson



VEY

WFCVM potential updates/future work

- Collect data for Weber/Davis and Utah basins
- Expand model to include Wasatch-adjacent basins and back valleys
- Compile/update with Vs data collected since 2008
- Update basin geometries with more recent gravity data

Rupture Direction, Hanging Wall, Basin, and Distance Effects on Ground Motions from Large Normal-Faulting Earthquakes

Kim B. Olsen

Nan Wang, Daniel Roten and James C. Pechmann

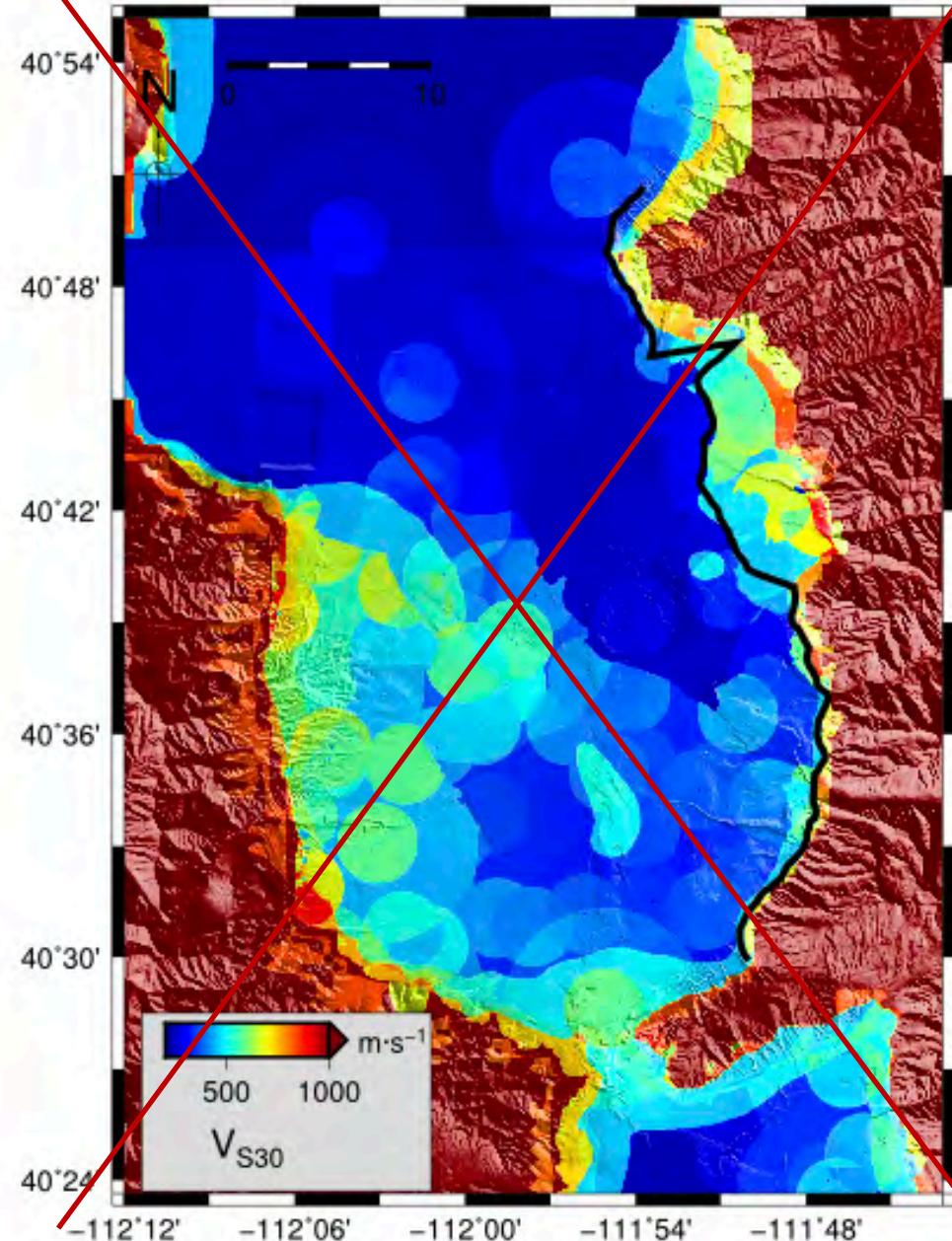
Based on NEHRP awards G14AP00044 & G14AP00045

UGS Meeting Feb 13, 2018

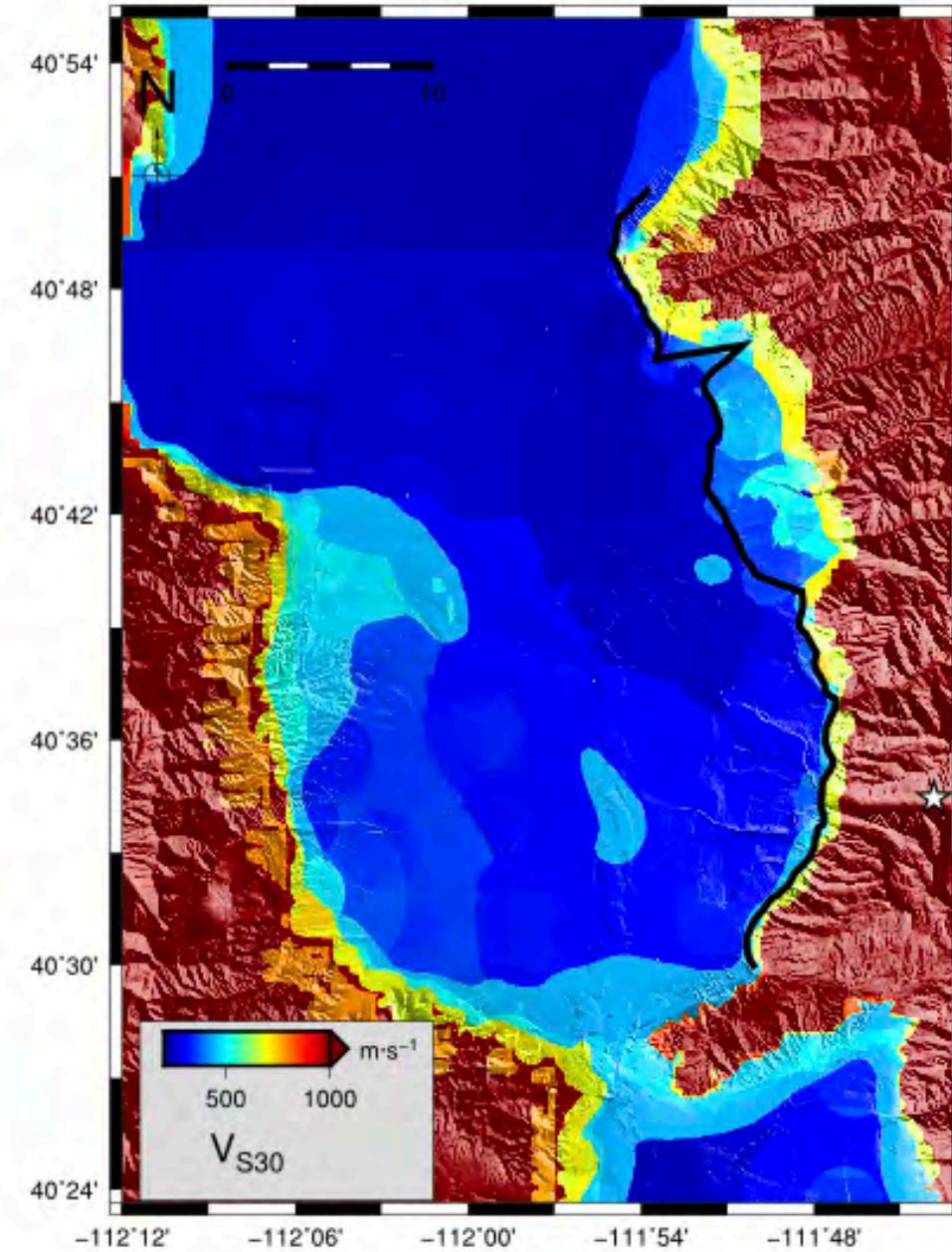
Outline

- Ground motion amplification from 3D simulations in the SLB
- Comparison of simulated amplification to NGA-West2 GMPEs
- What controls ground motion amplification in the SLB (source/path)?
- Can recent directivity model predict directional amplification effects?
- Causes of simulation versus GMPE bias at 0-1.5 km and 4-10 km
- Hanging-wall effects

Version 3c

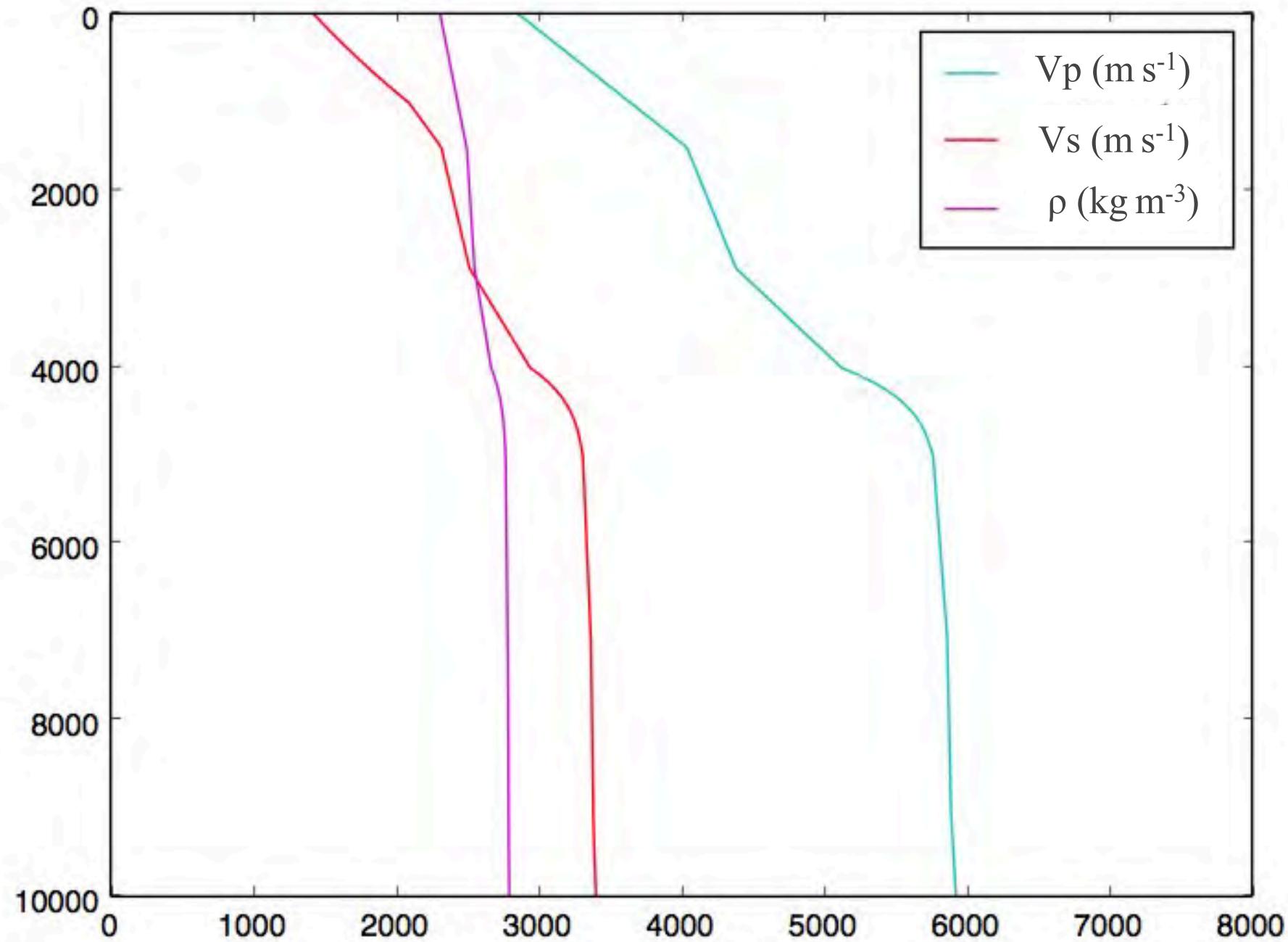


Version 3d

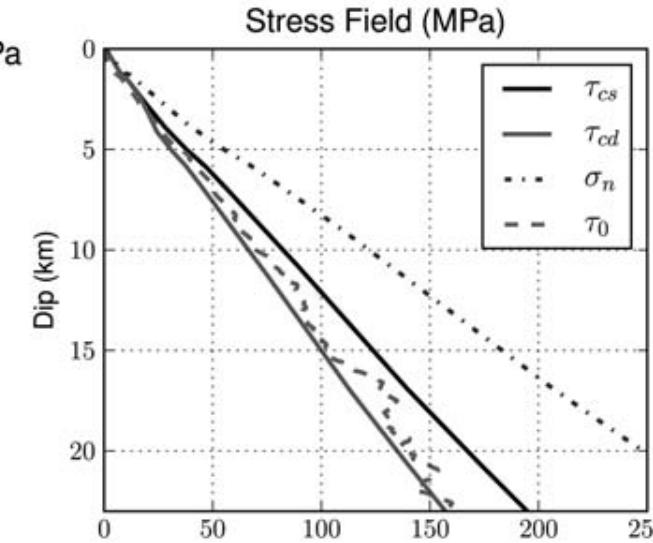
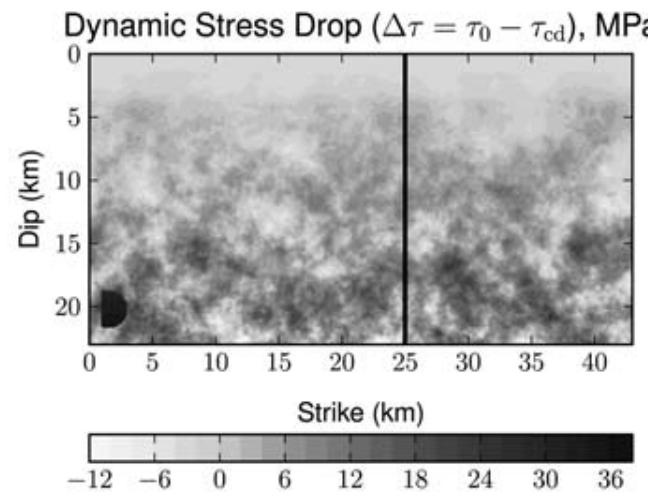
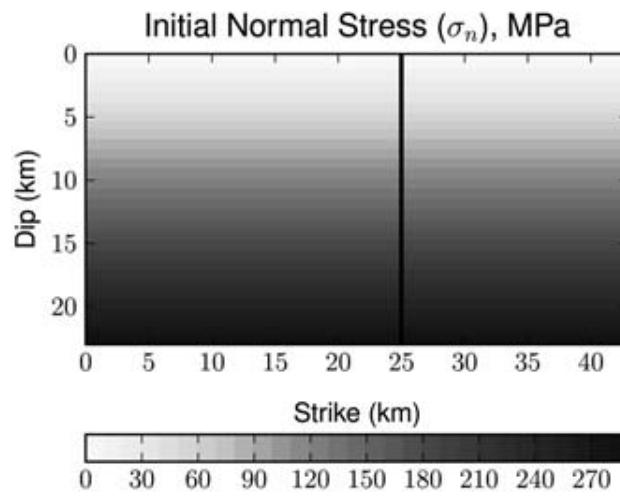
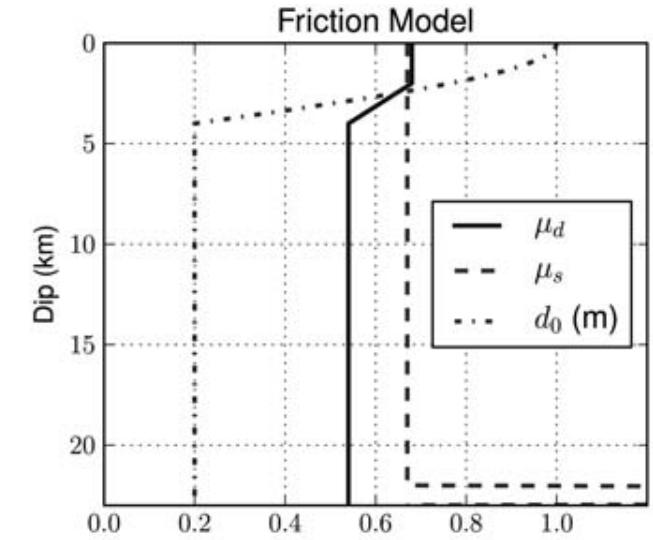
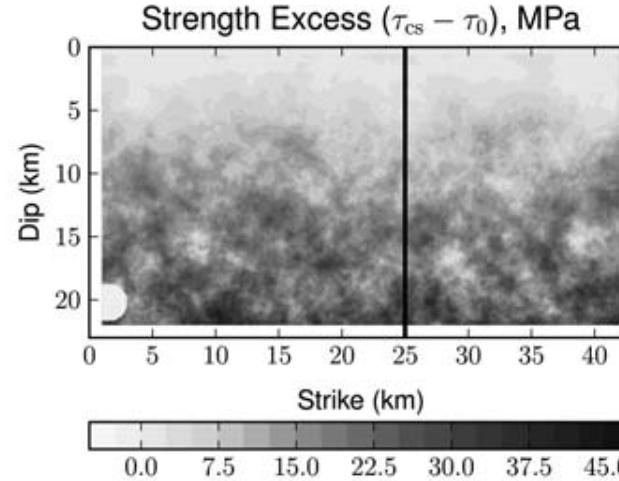
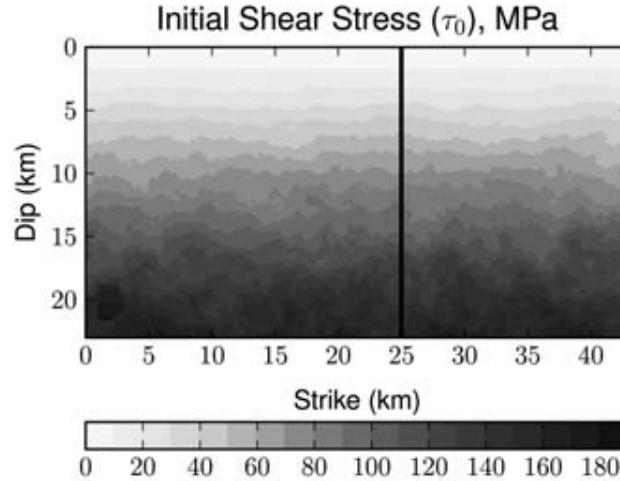


Roten et
al. (2011)
re-done
in fixed
CVM

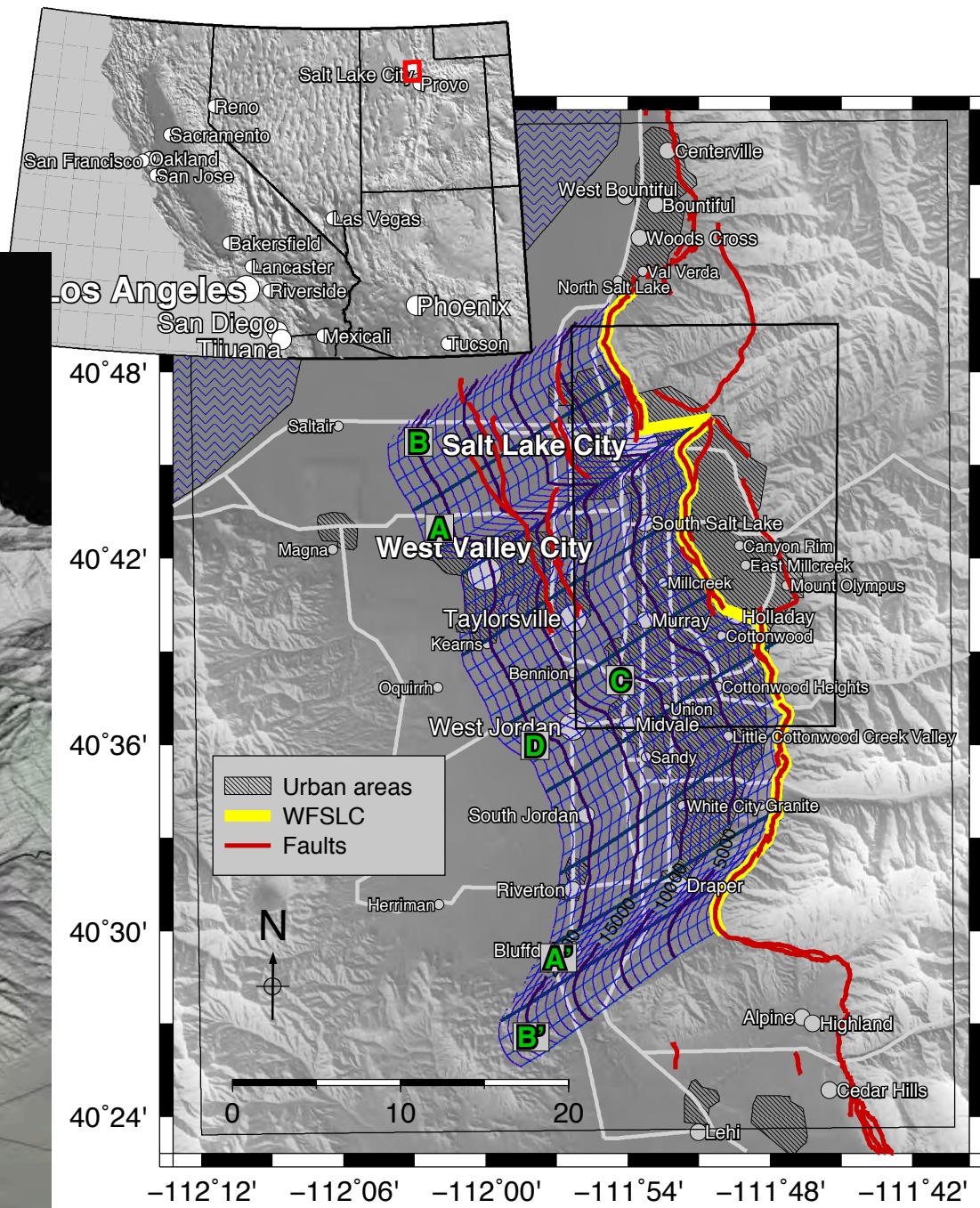
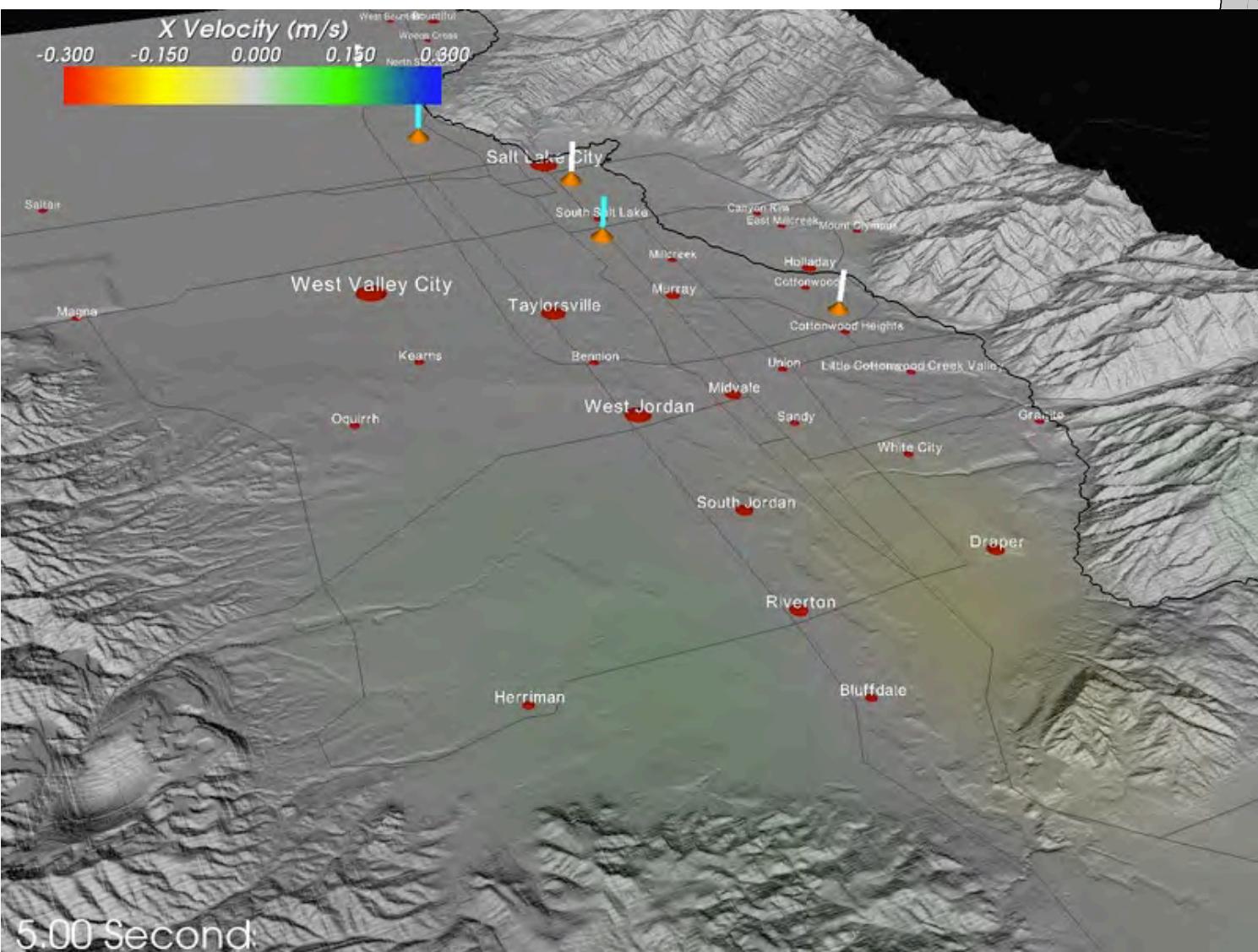
Additional set of
6-scenario
simulations with
1-D rock velocity
model



Source Descriptions from Dynamic Ruptures

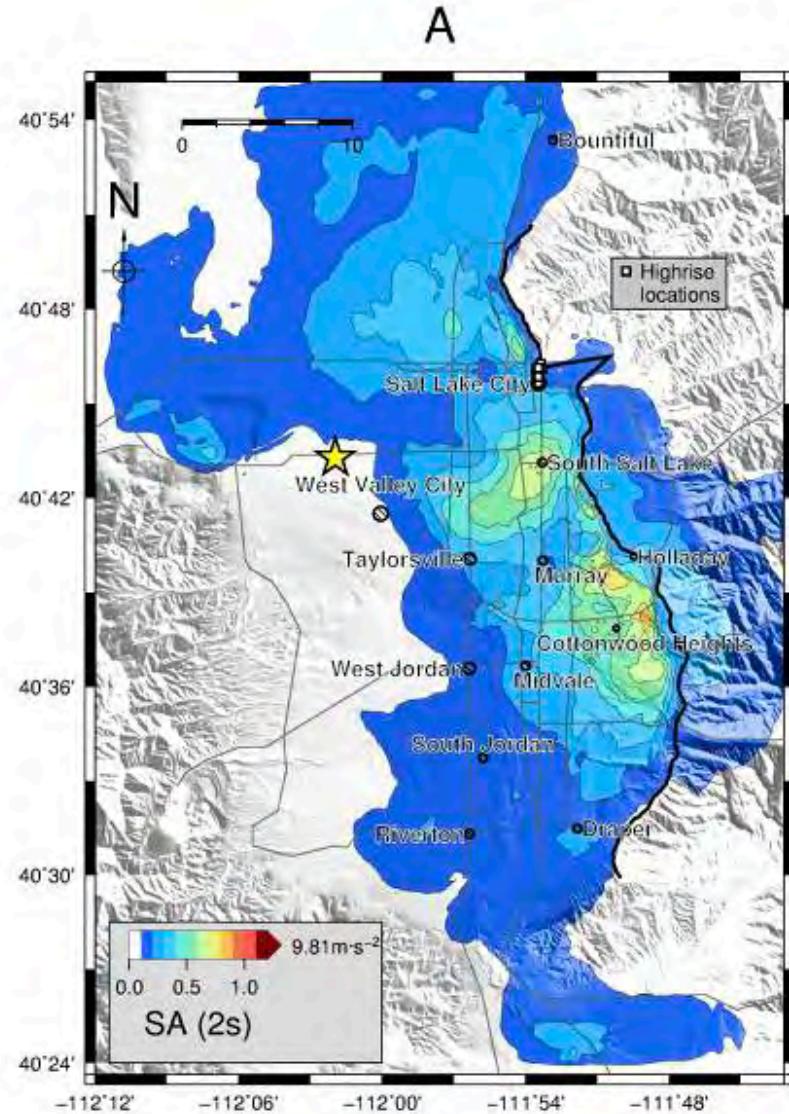


All simulations use Wasatch Fault model as in Roten et al. (2011).

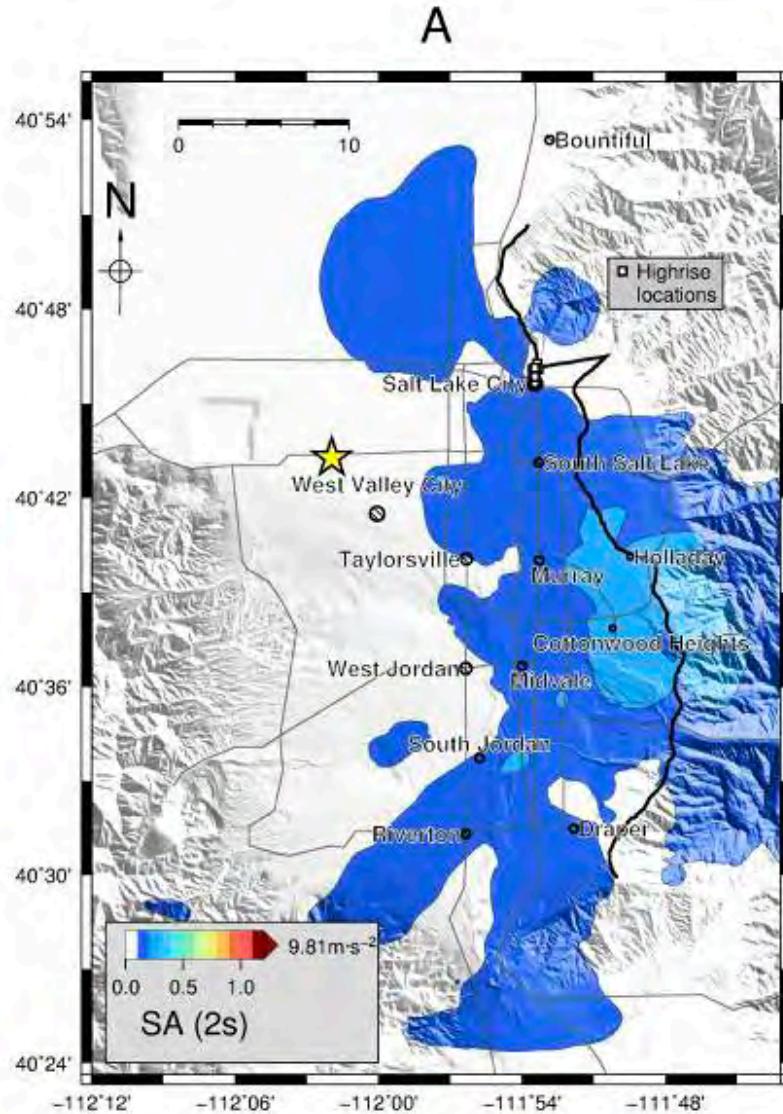


Basin Amplification

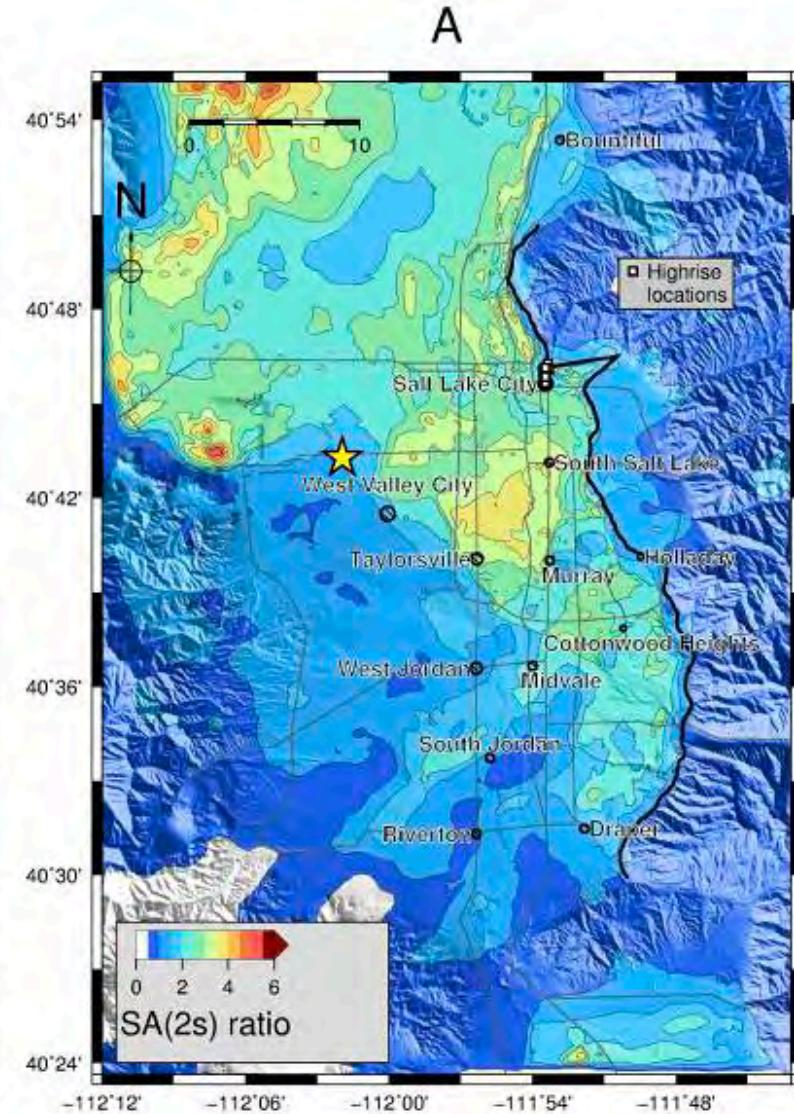
3D



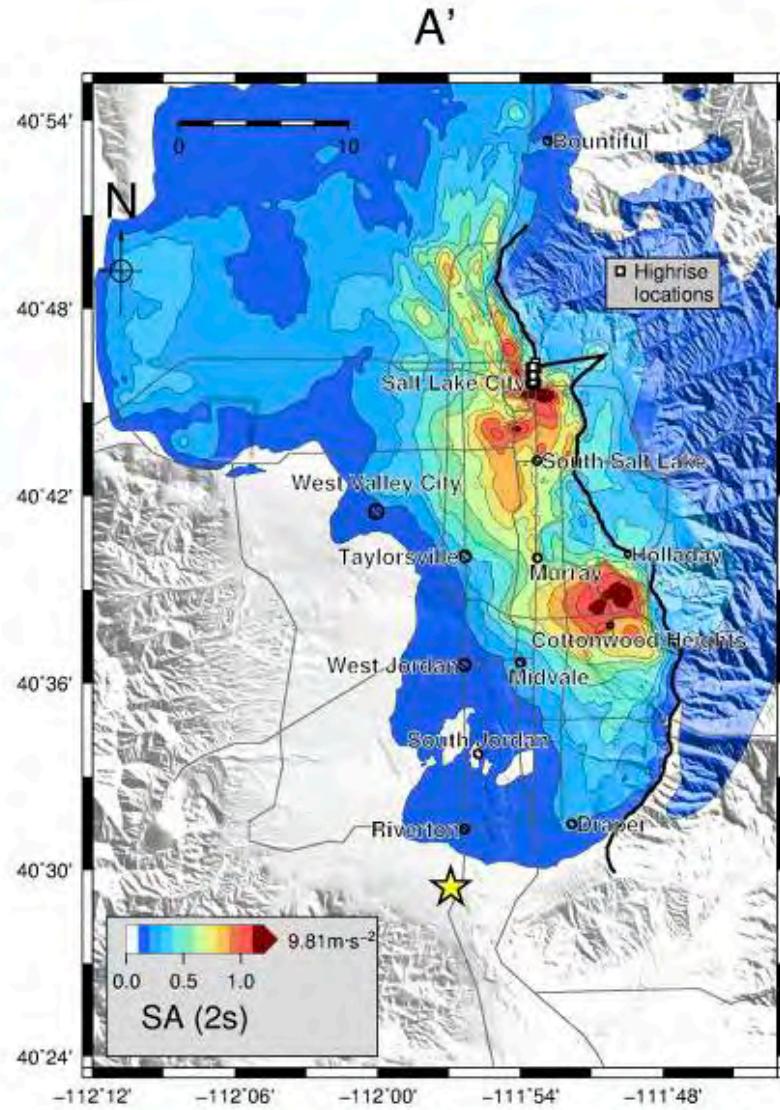
1D



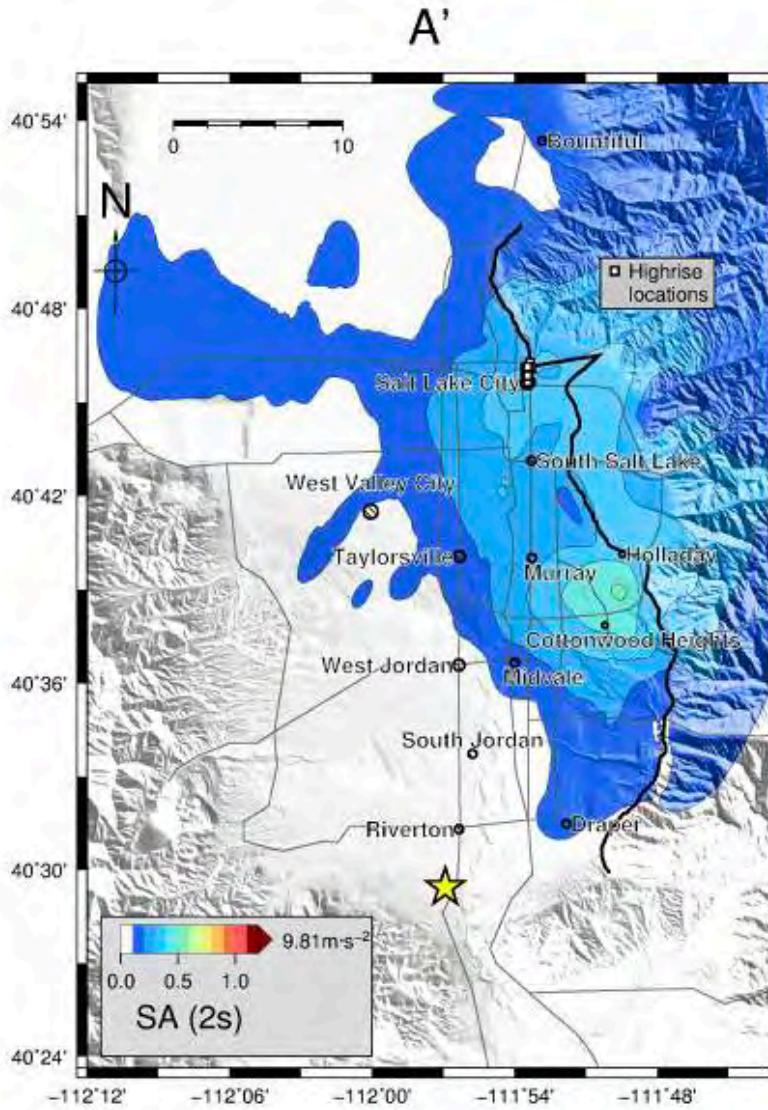
3D/1D



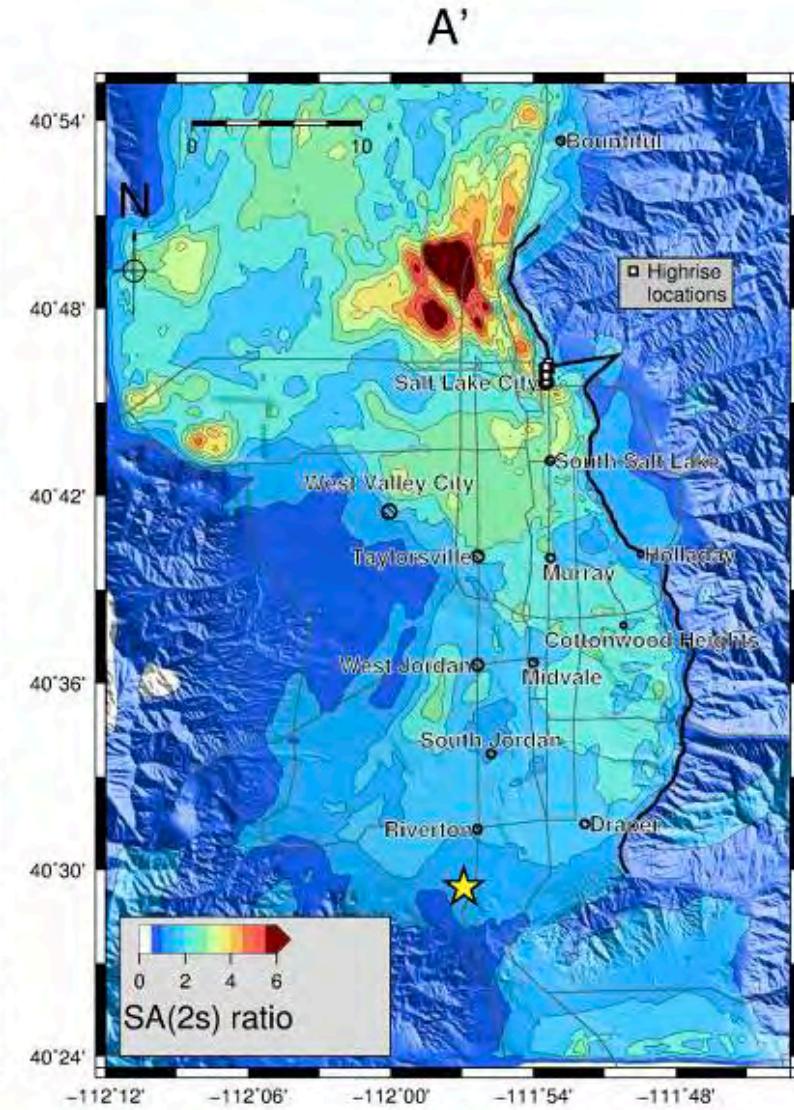
3D



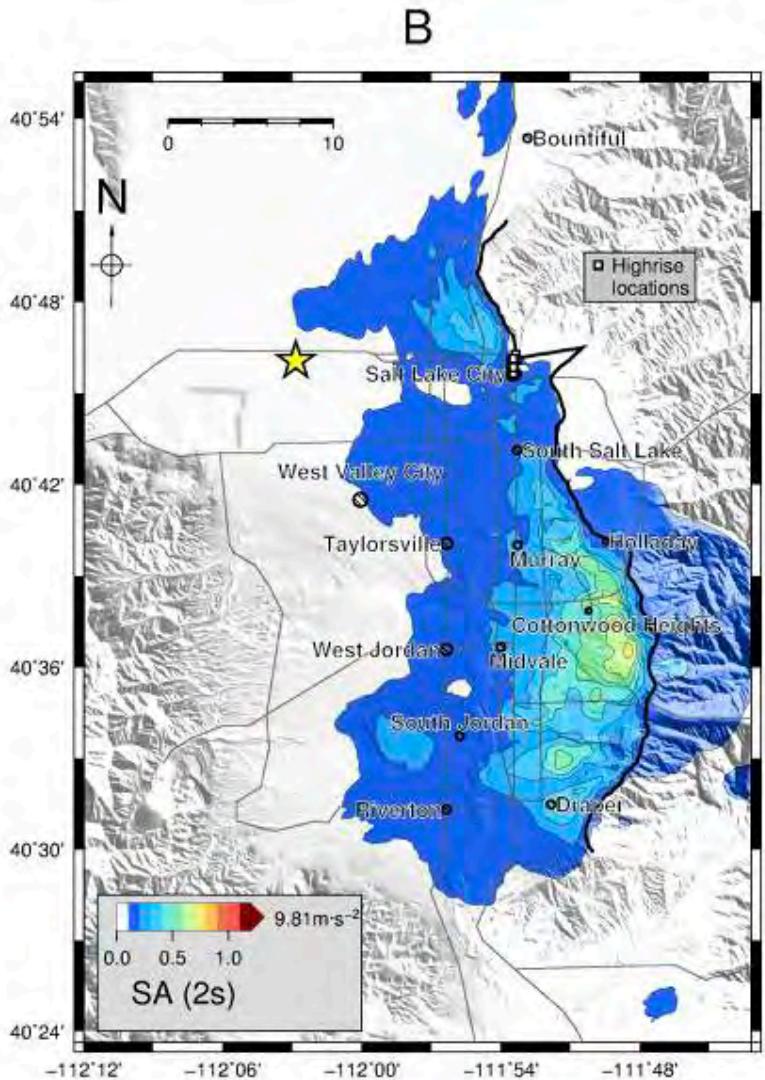
1D



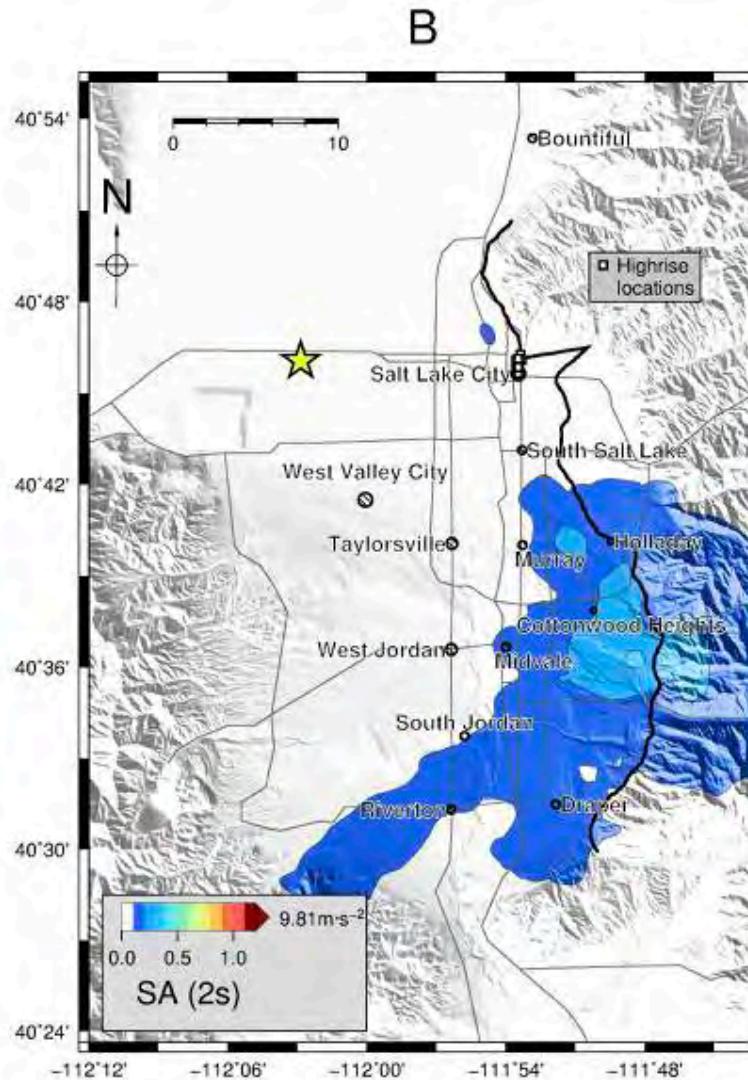
3D/1D



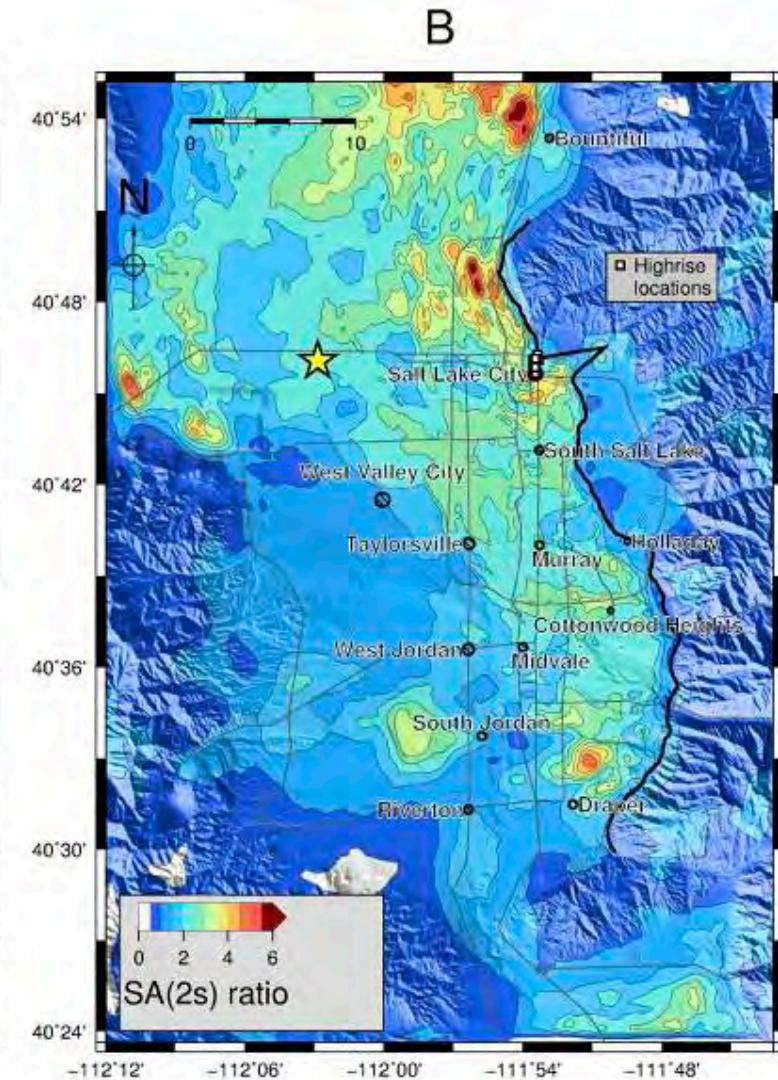
3D



1D

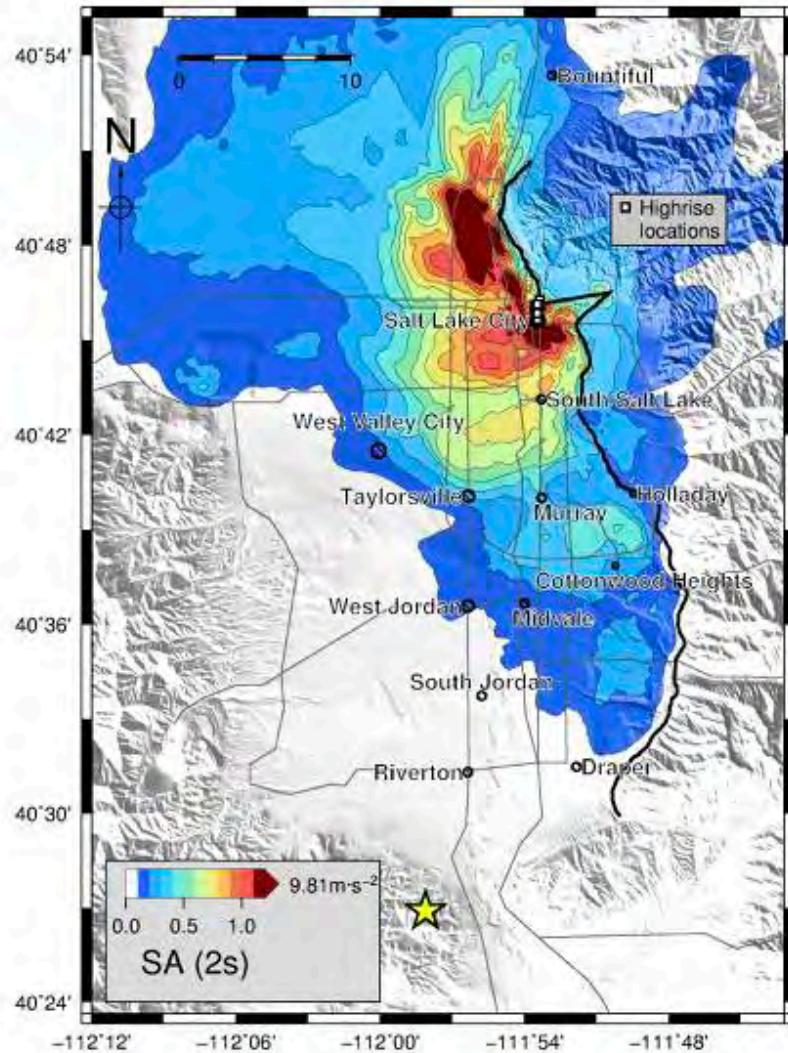


3D/1D



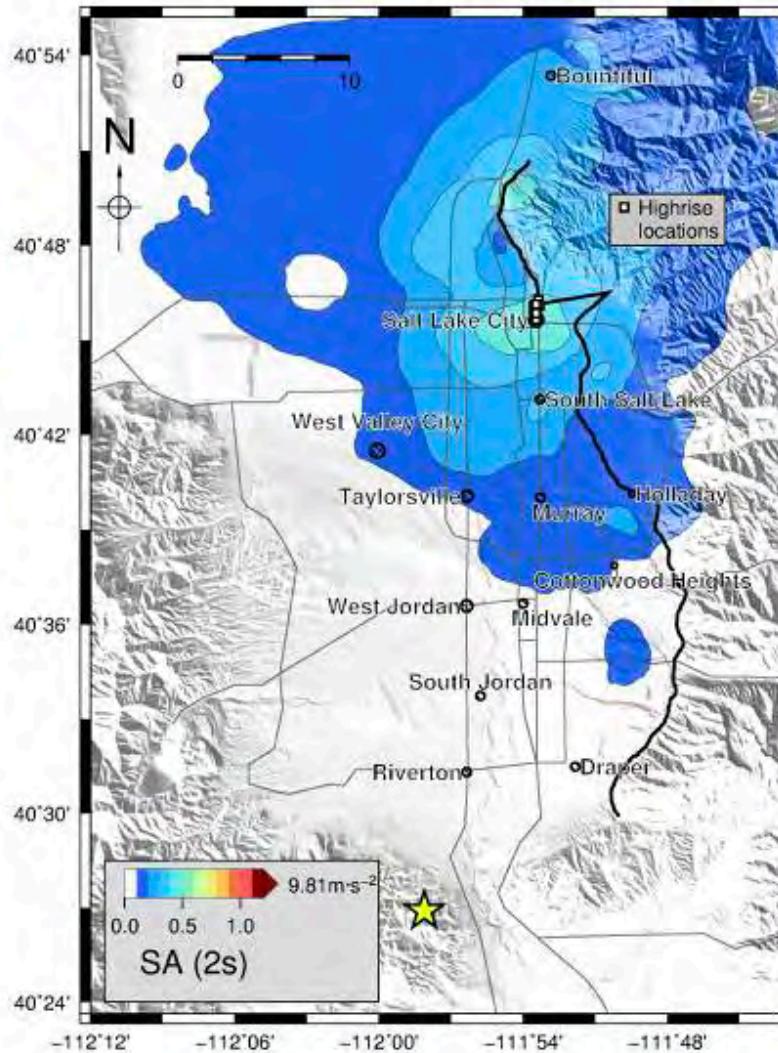
3D

B'



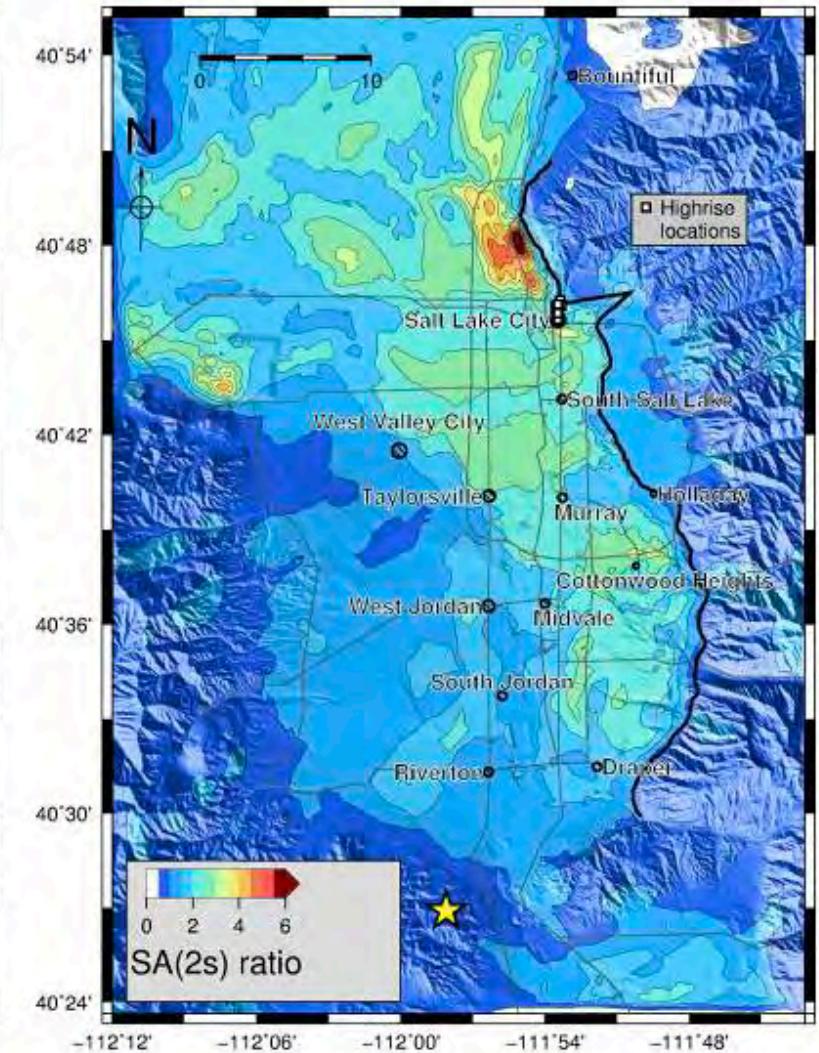
1D

B'

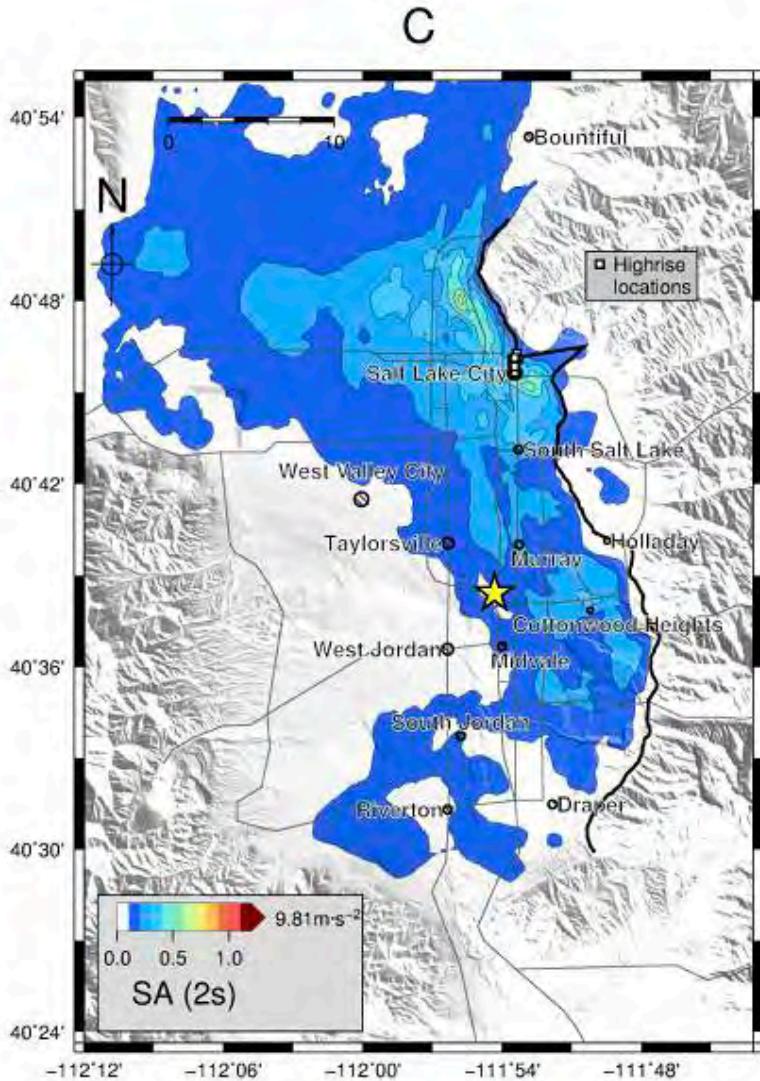


3D/1D

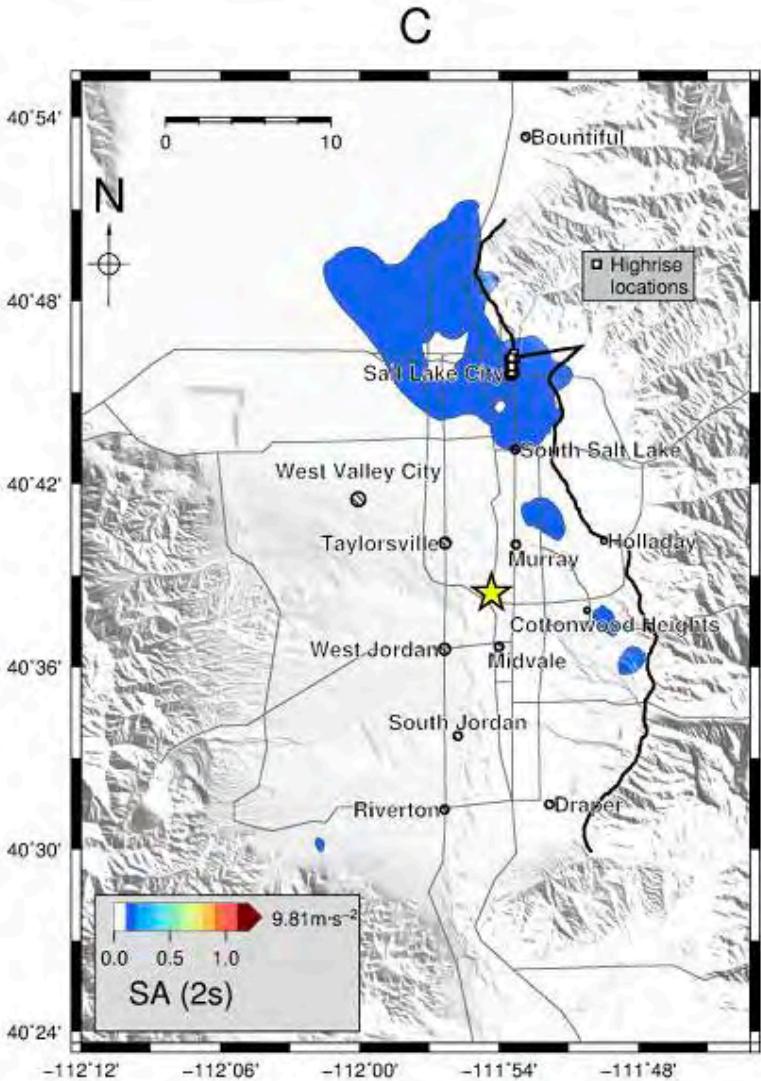
B'



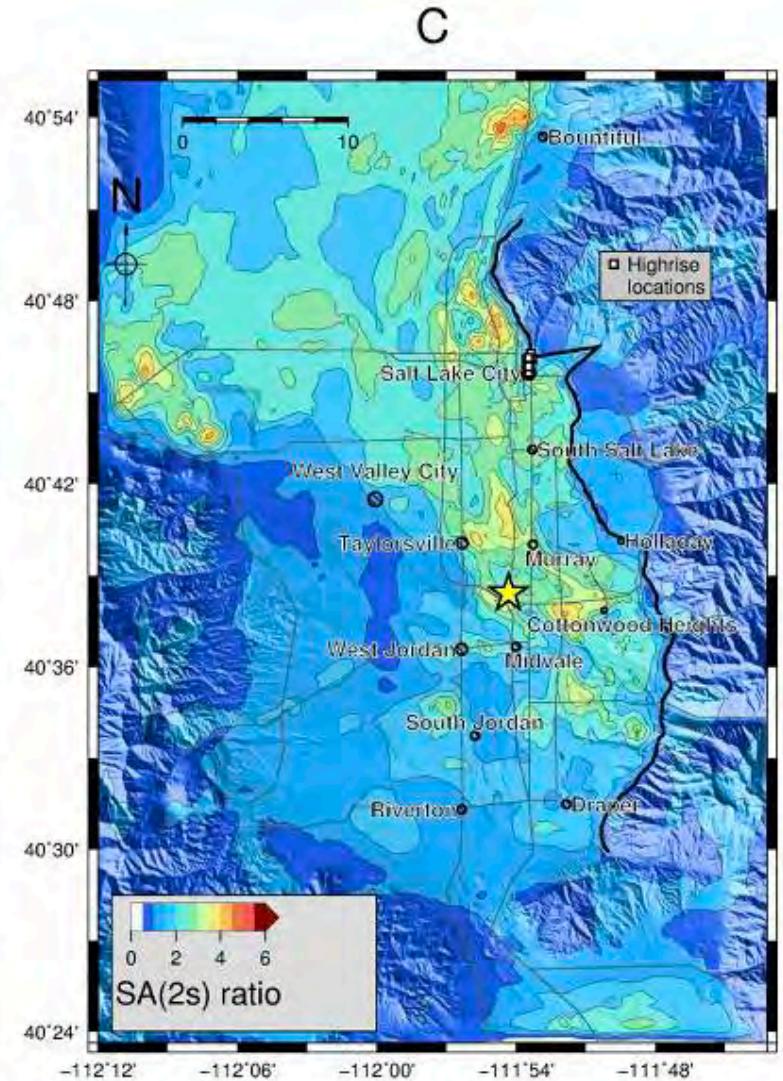
3D



1D



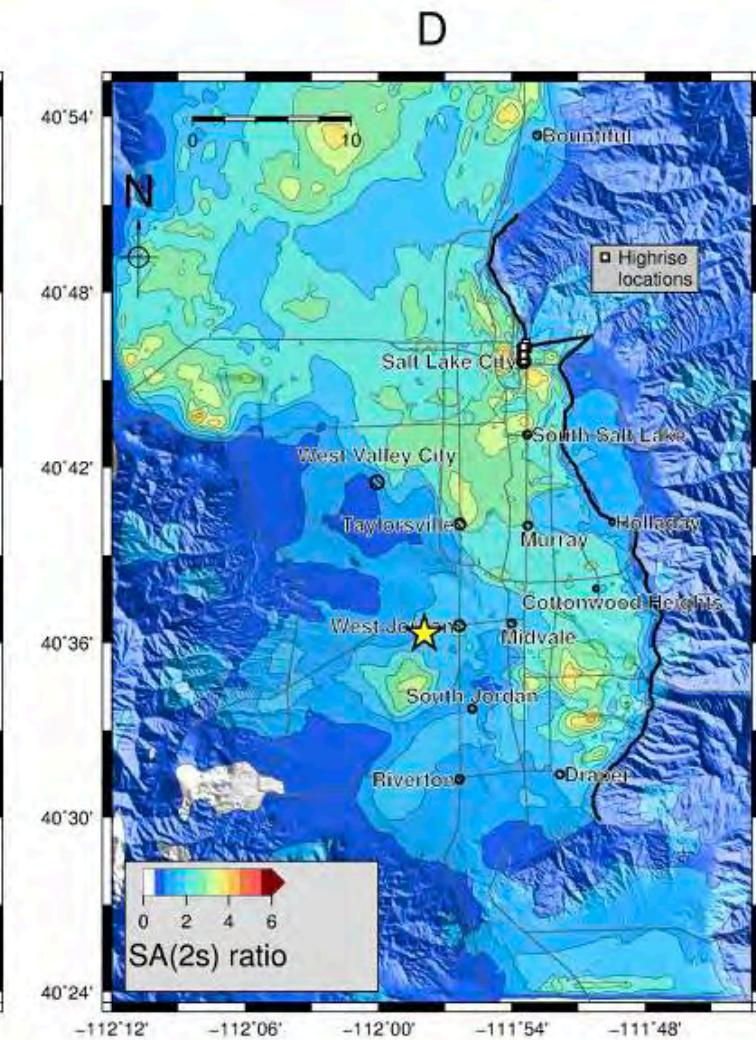
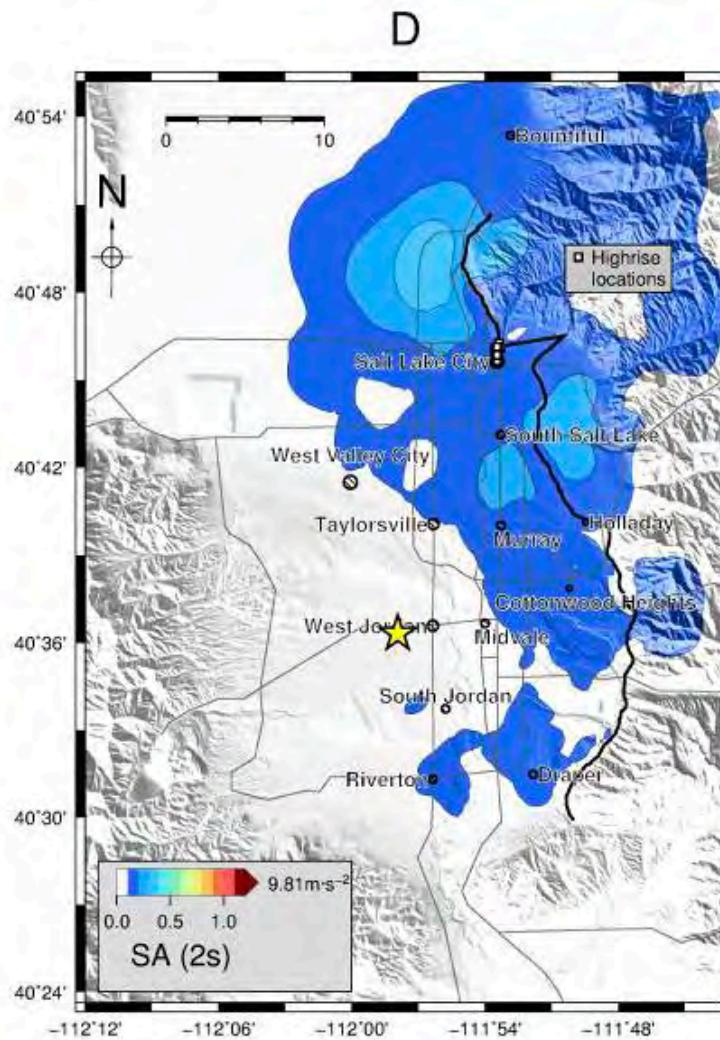
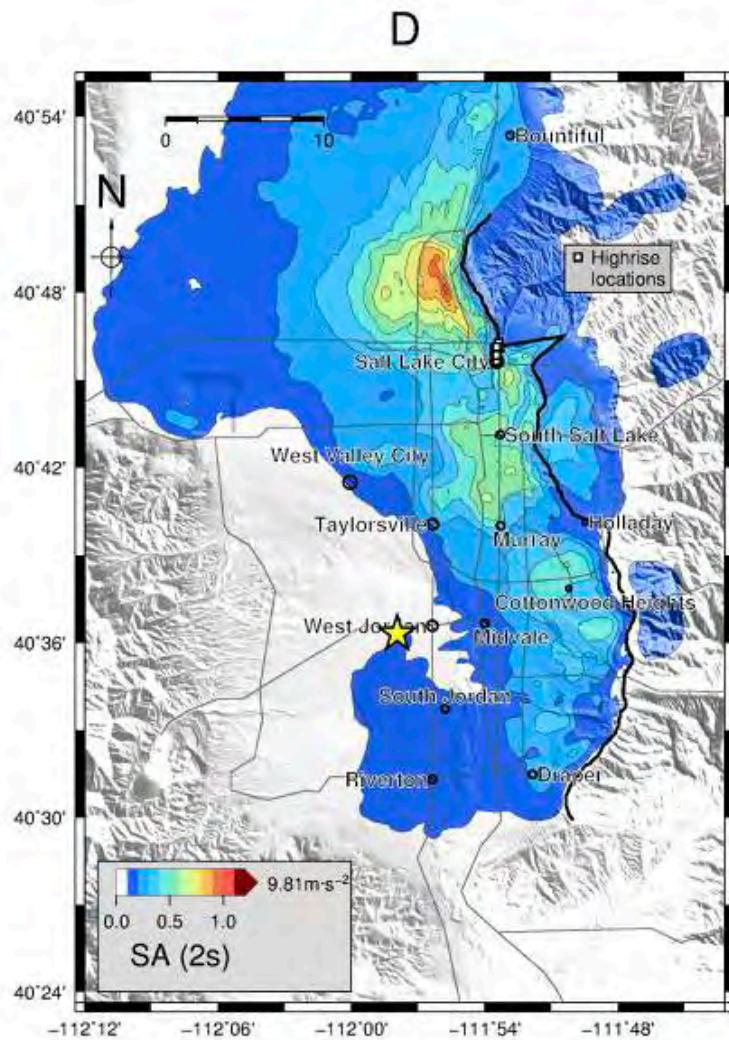
3D/1D



3D

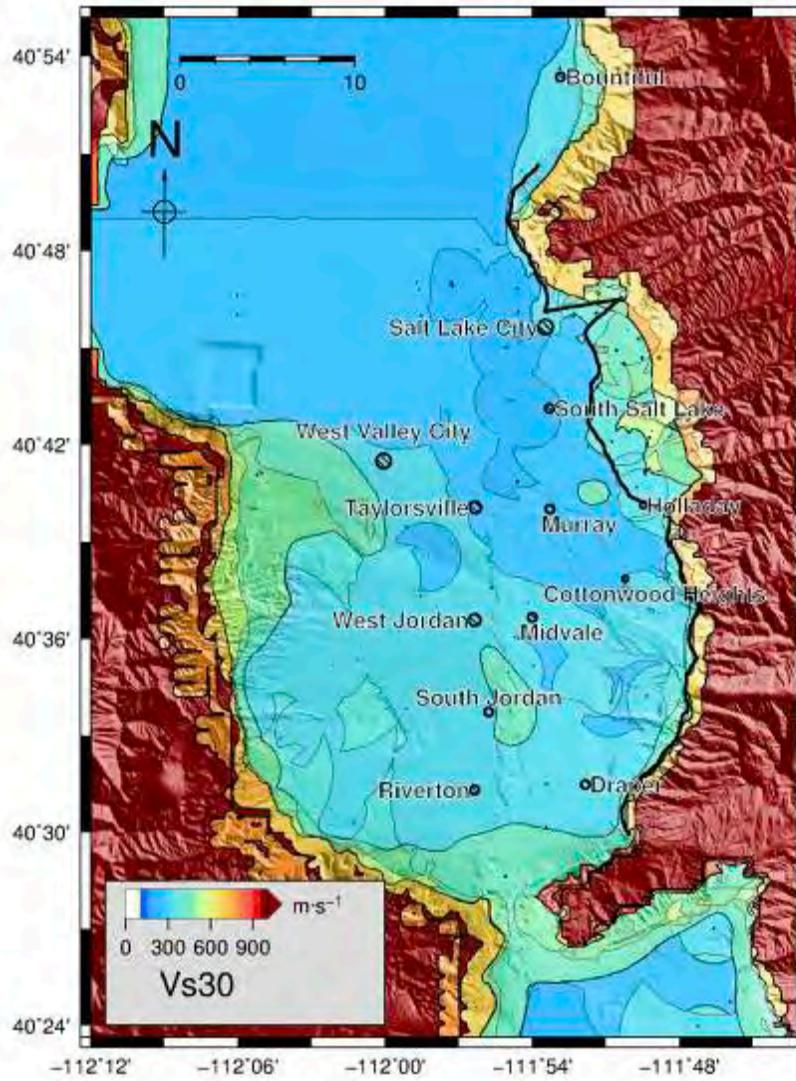
1D

3D/1D

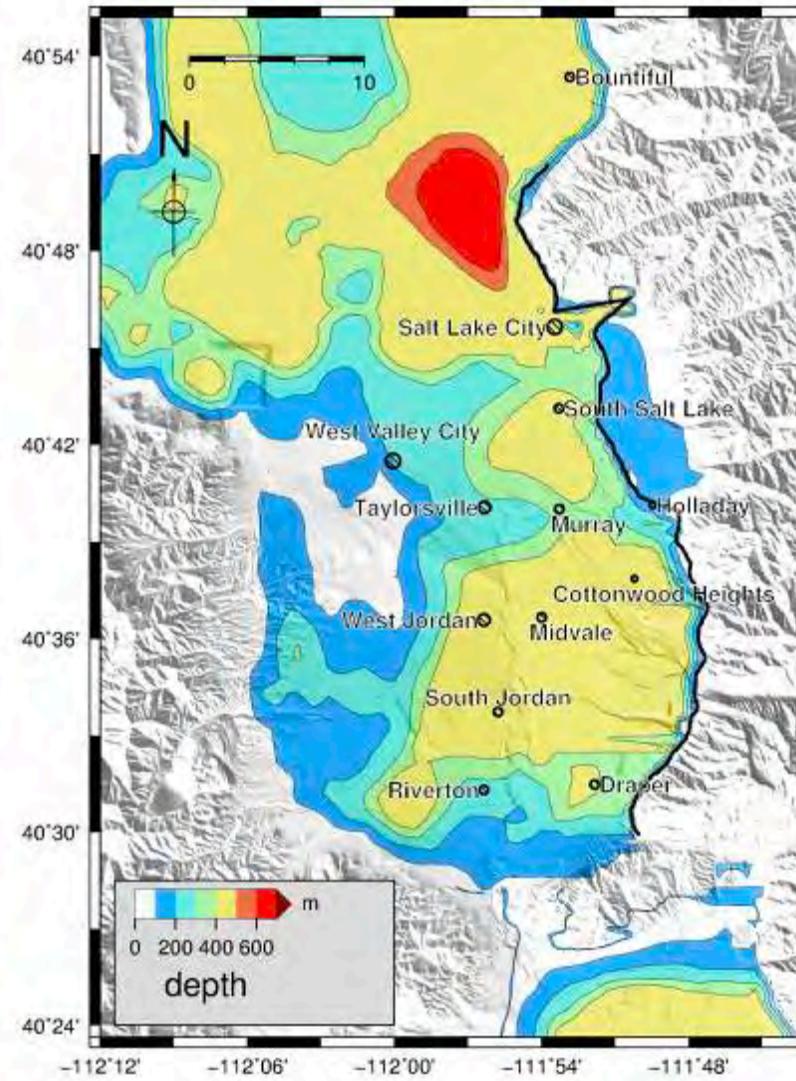


Basin Parameters

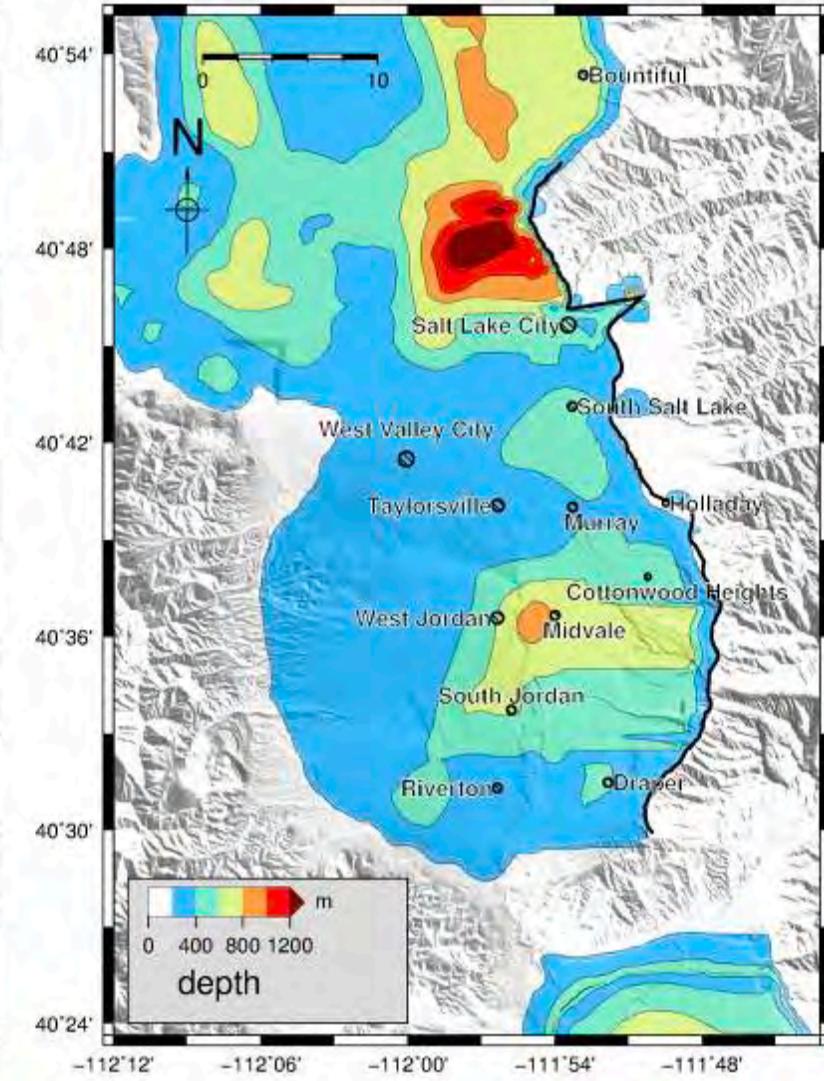
Vs30



Isosurface_Vs=1.0km/s

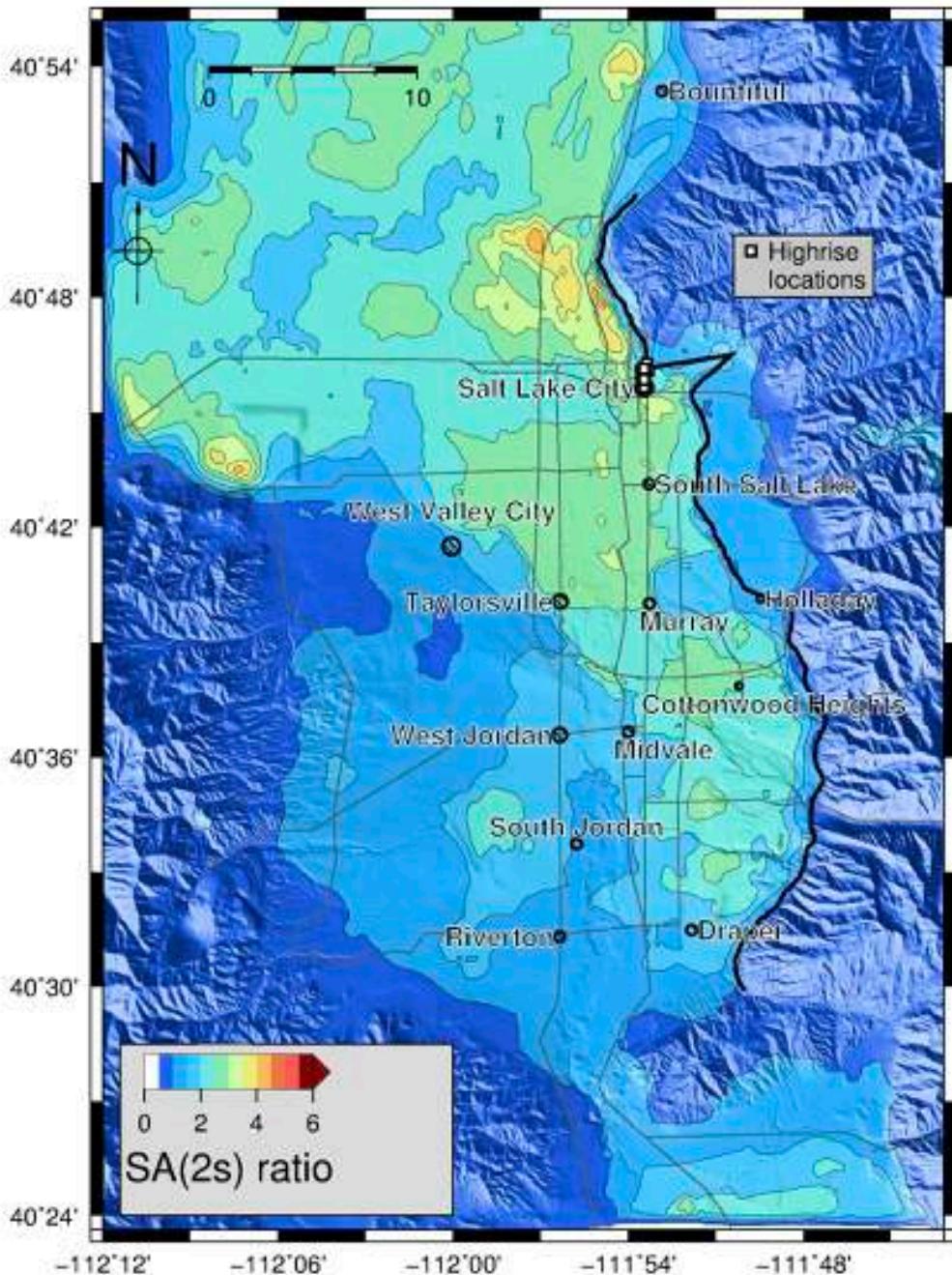


Isosurface_Vs=1.5km/s

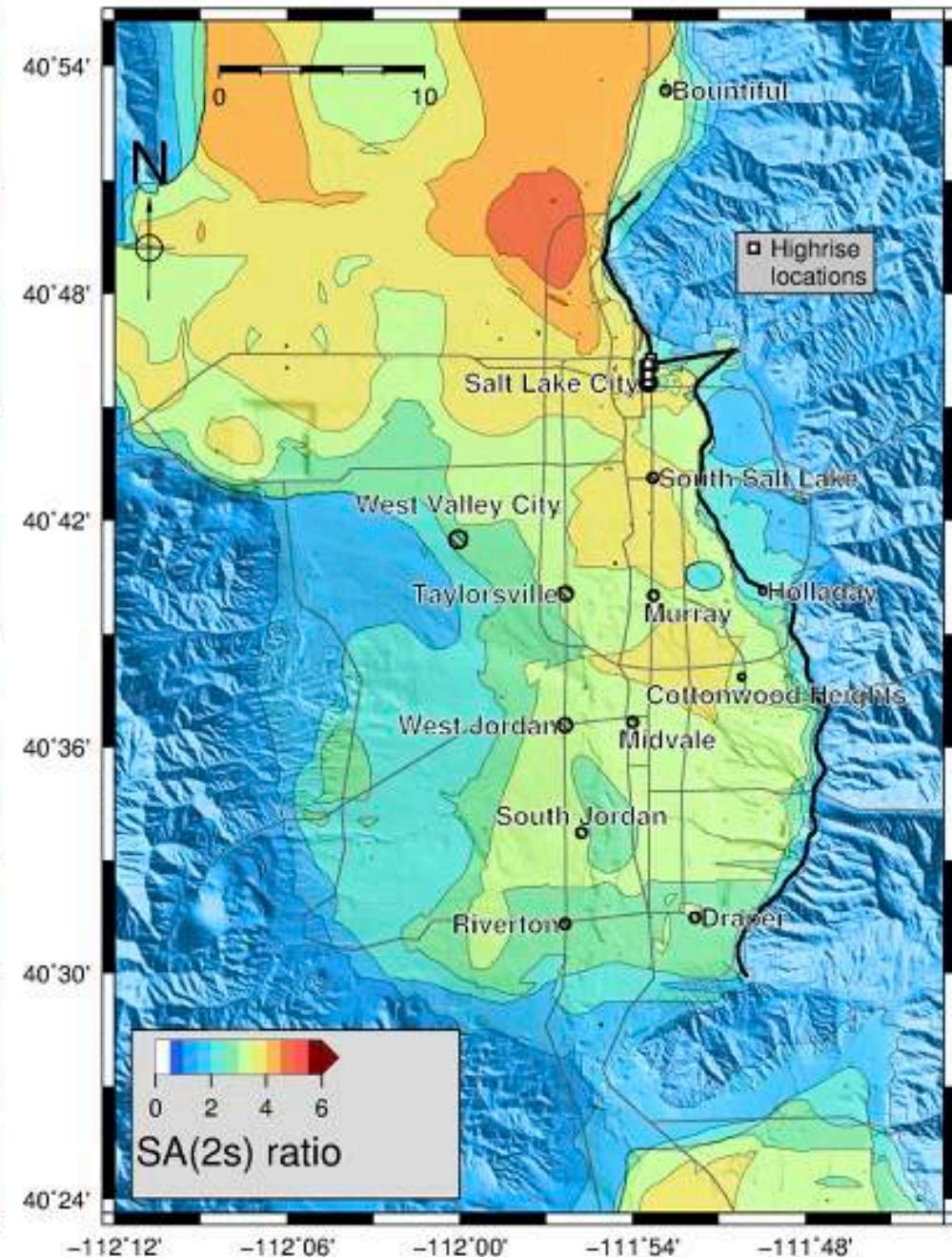


Comparison
of mean
3D/1D
amplification
from
simulations
to BSSA14

Mean



BSSA14



Regression for Basin Amplification

$$W_{nj} = \begin{cases} 1, & \text{if } (D_n^{bin} - \Delta D/2) \leq D_j \leq (D_n^{bin} + \Delta D/2) \\ 0, & \text{otherwise} \end{cases}$$

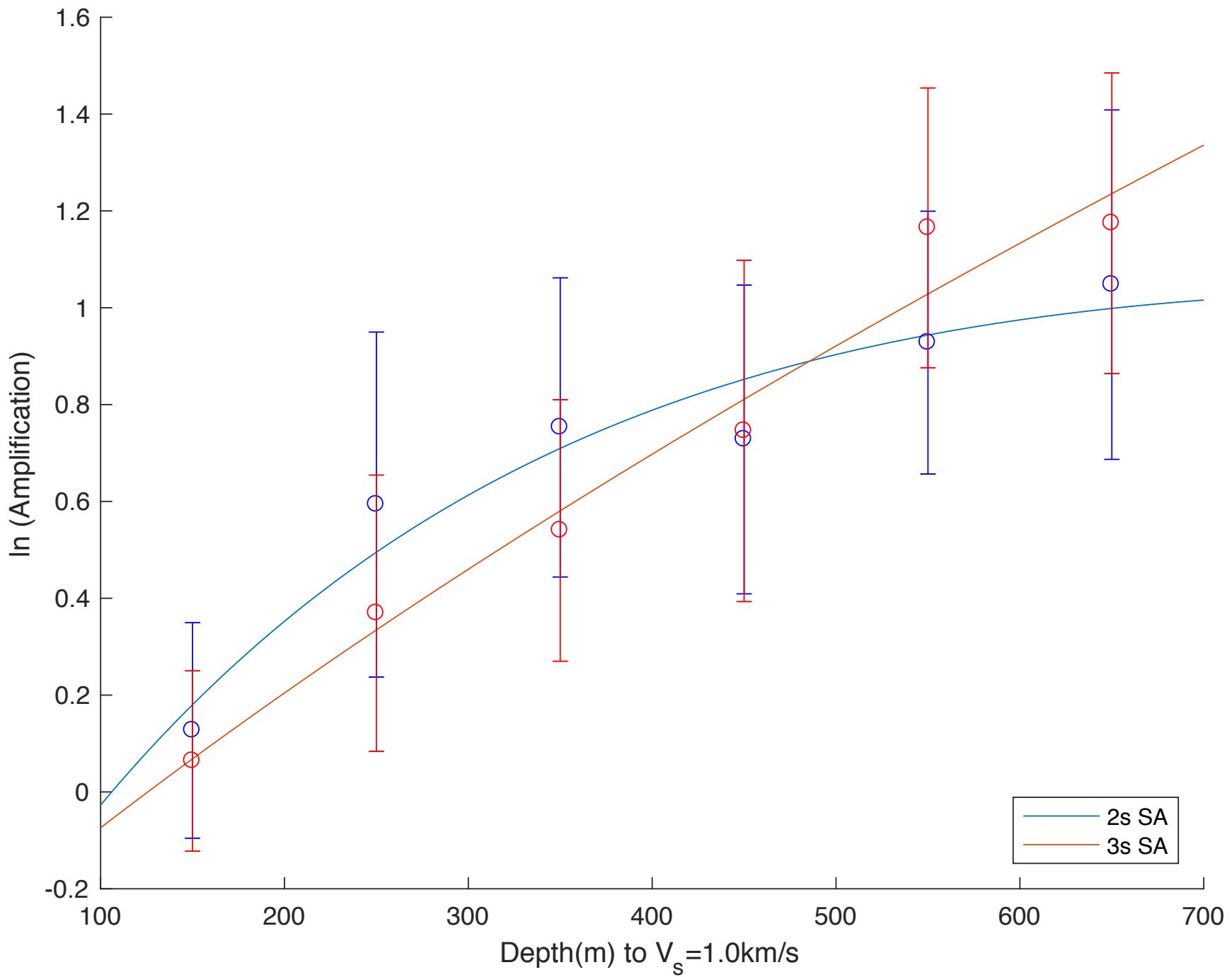
$$B(D_n, T_m) = \left(N_{sn} \sum_{j=1}^{N_{site}} W_{nj} \right)^{-1} \sum_{i=1}^{N_{sn}} \sum_{j=1}^{N_{site}} W_{nj} \ln [SA_{ij}^{3d}(T_m)/SA_{ij}^{1d}(T_m)]$$

$$A(D, T) = a_0(T) + a_1(T)[1 - \exp(-D/300)] + a_2(T)[1 - \exp(-D/4000)]$$

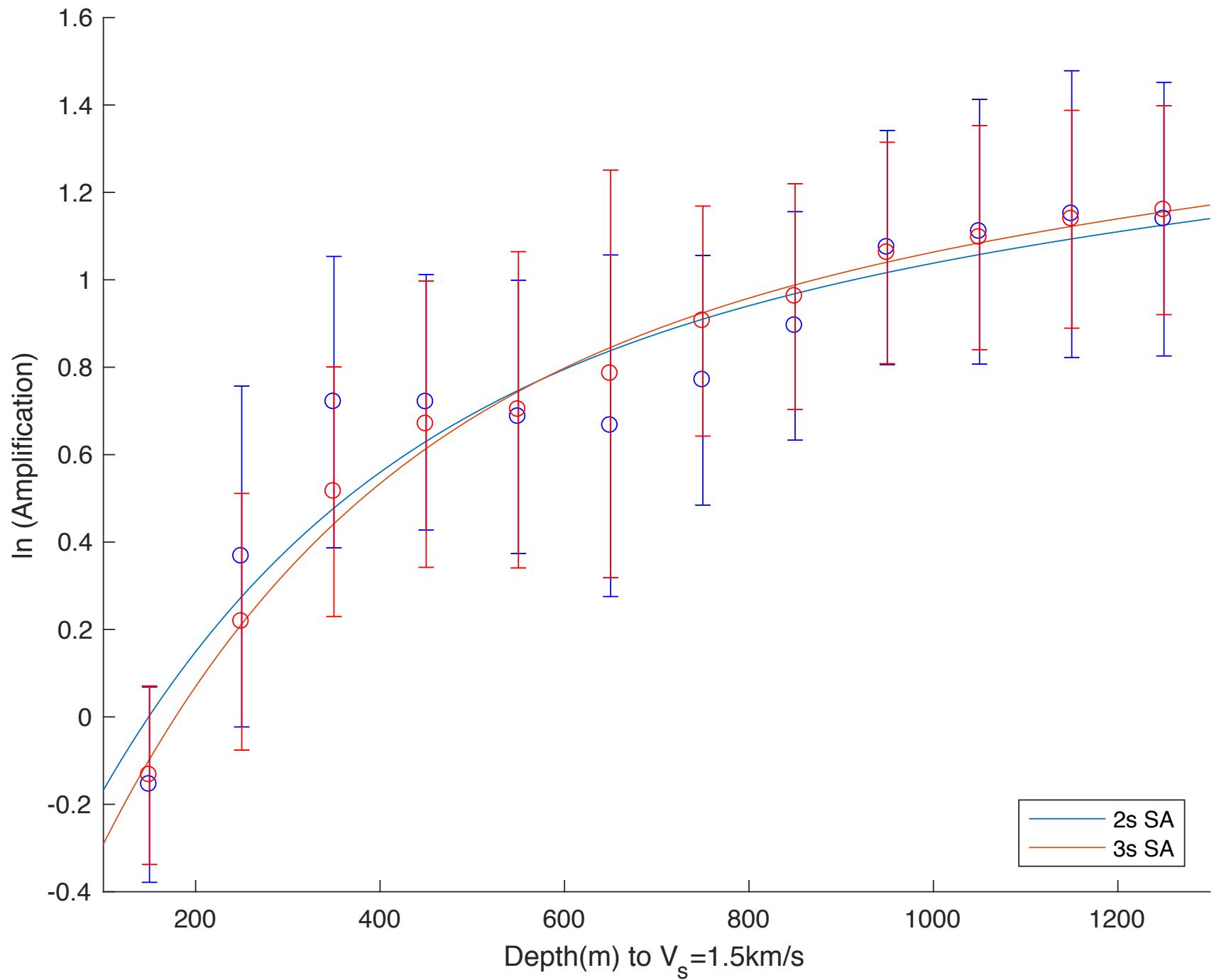
where

$$a_i(T) = b_i + c_i T, \quad i = 0, 1, 2$$

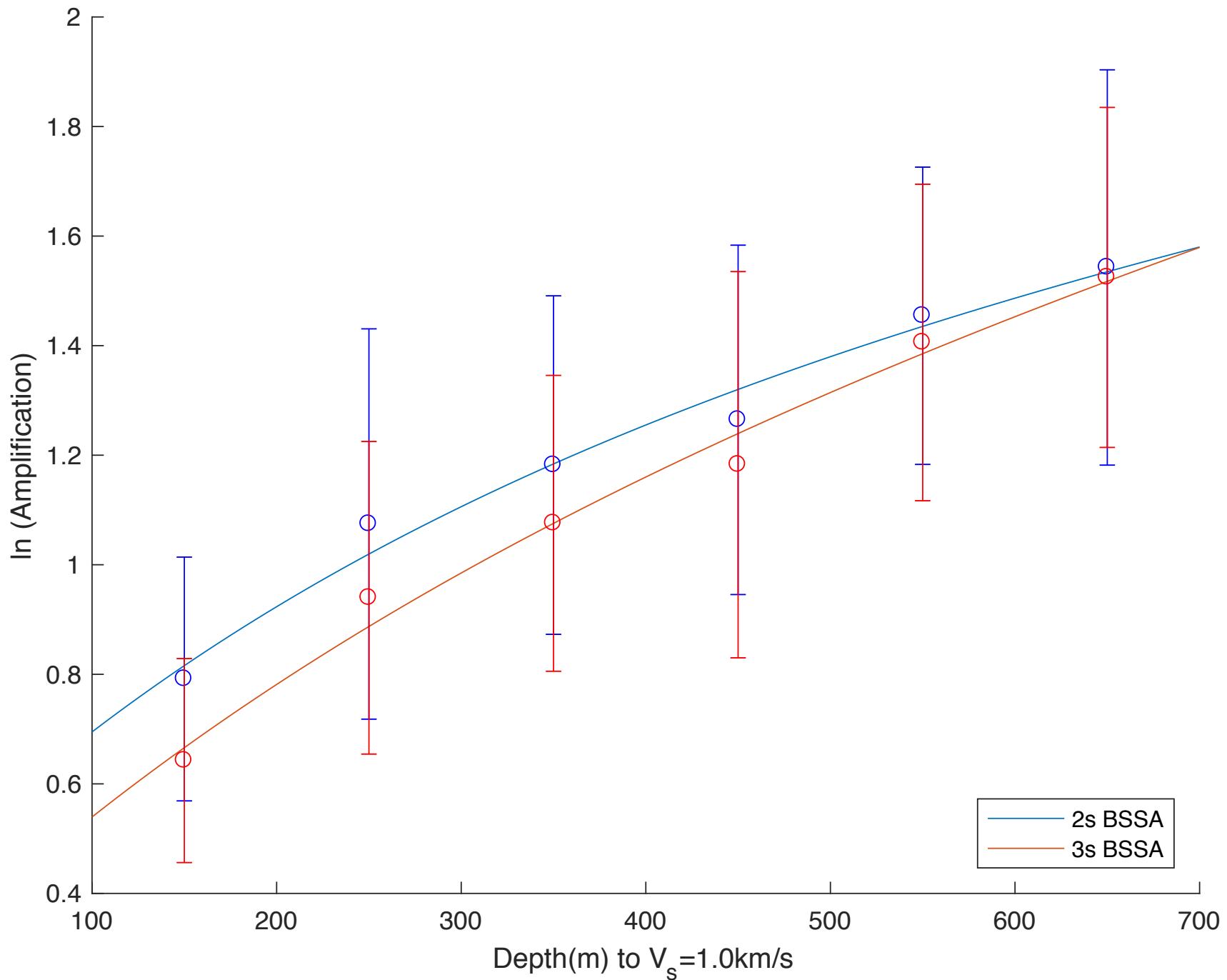
Natural log amplification factors as a function of depth



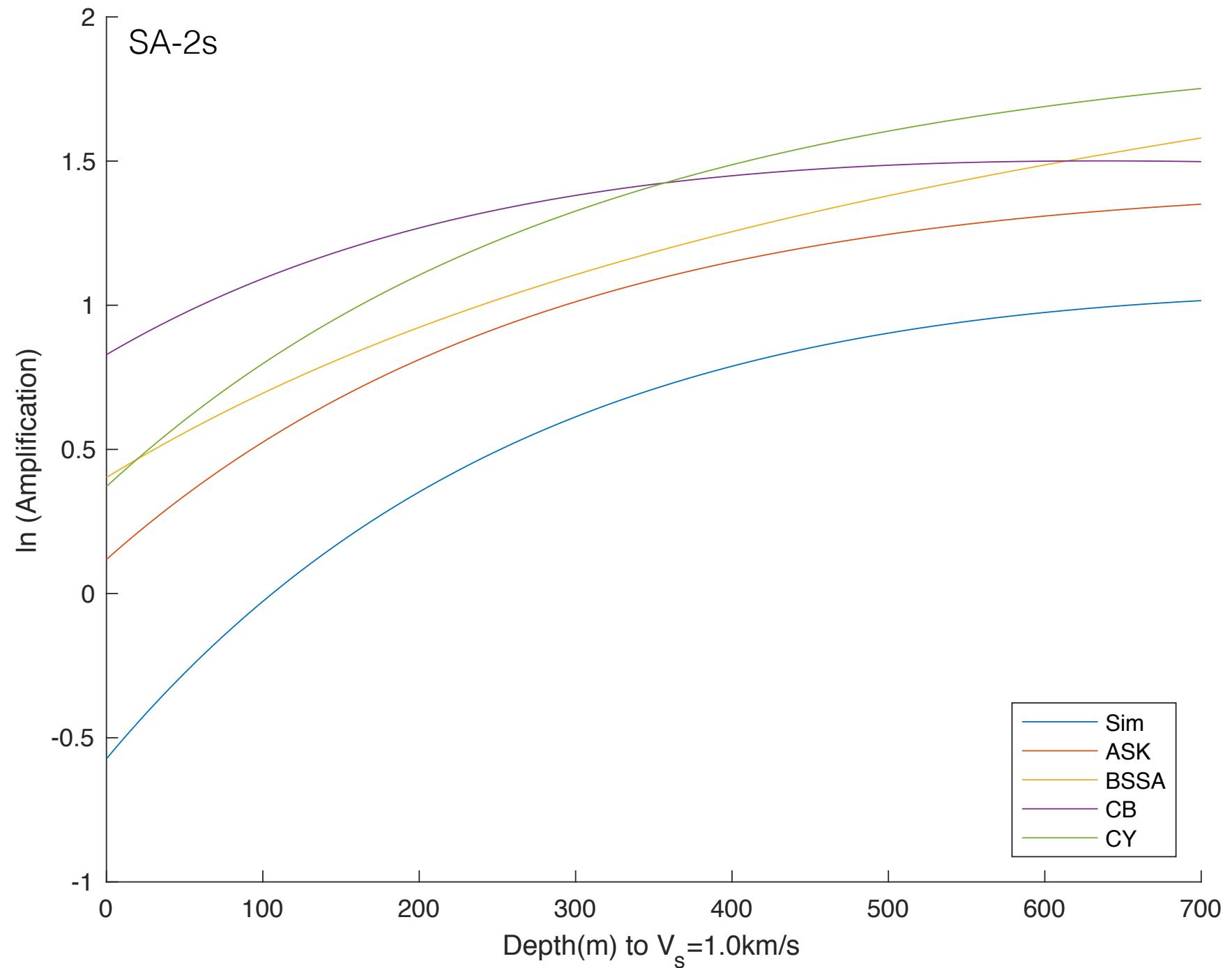
Natural log amplification factors as a function of depth



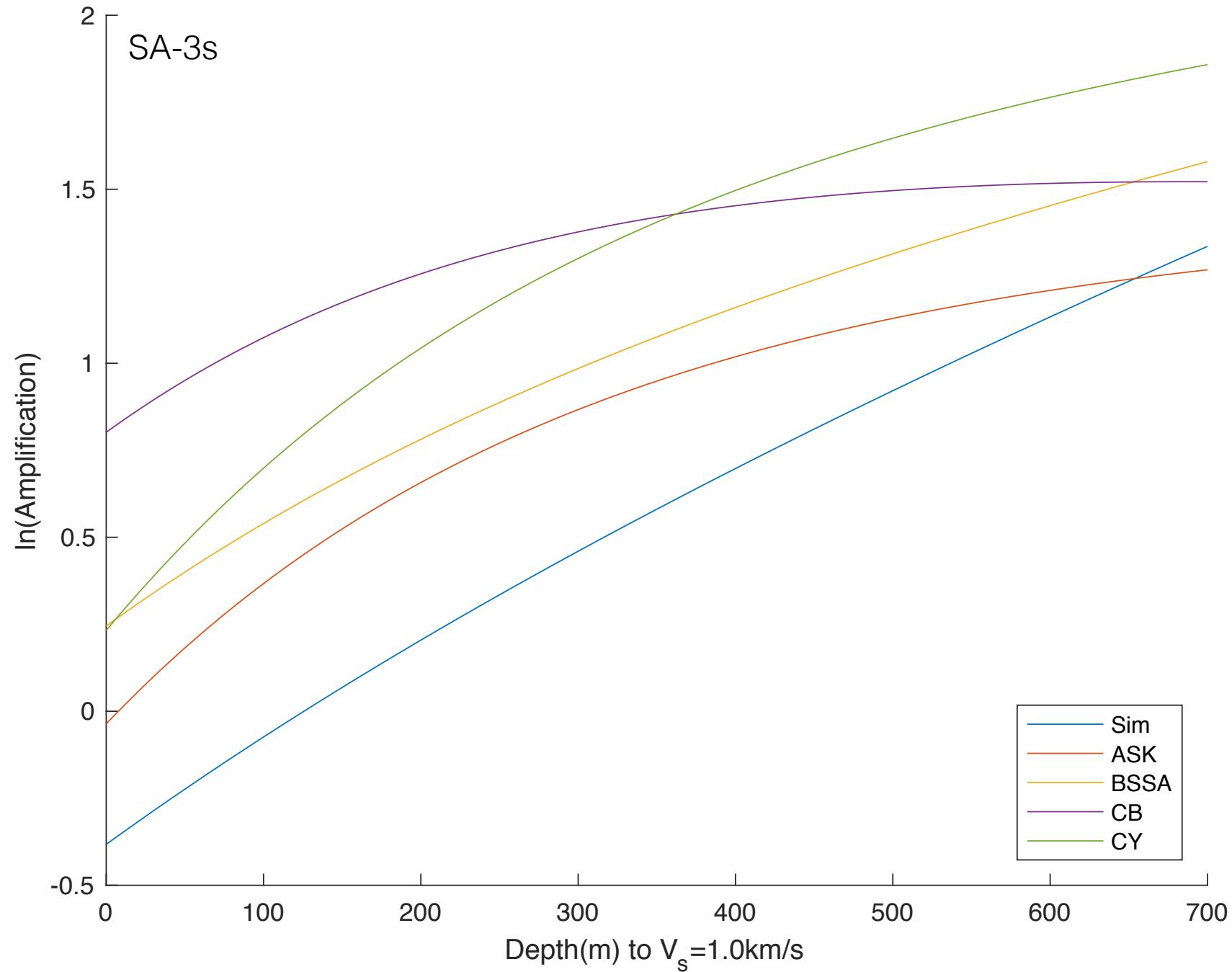
Natural log
amplification factors as
a function of depth.



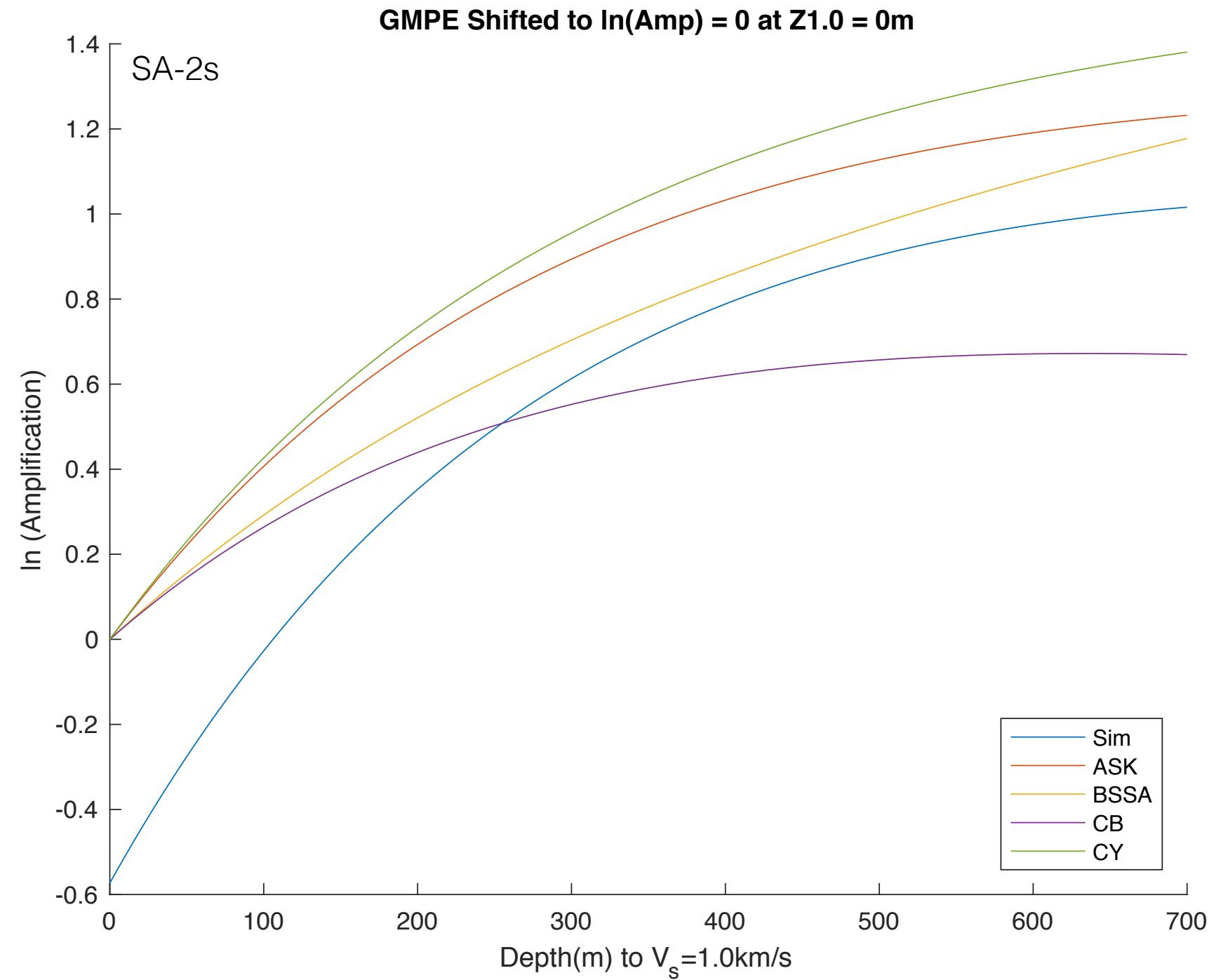
Comparison of the basin depth amplification factors regression results for 2s period from the GMPEs to the regression results for the simulations.



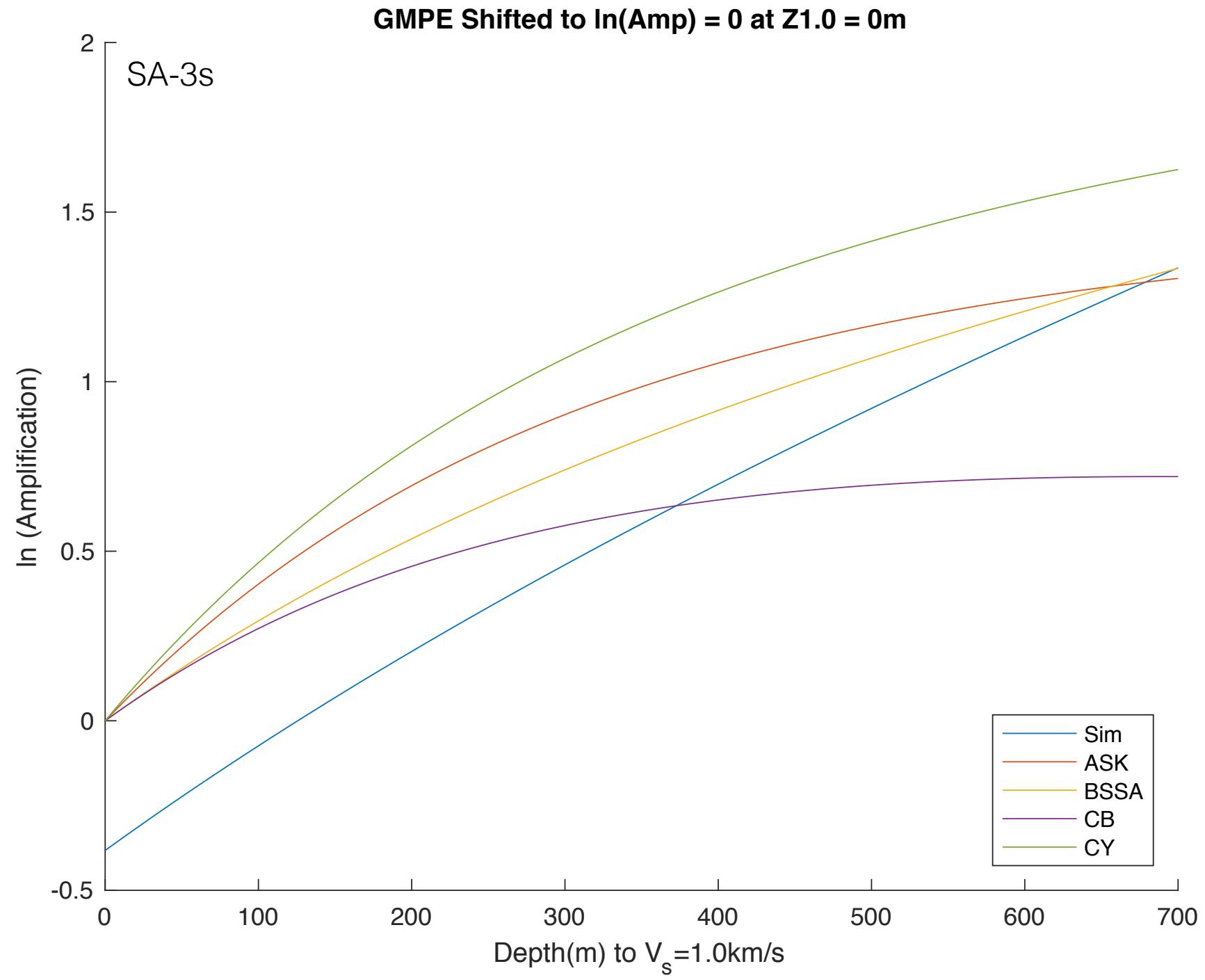
Comparison of the basin depth amplification factors regression results for 3s period from the GMPEs to the regression results for the simulations.



Comparison of the regression results for the basin depth amplification factors at a period of 2s from the GMPEs to the results of the simulations. The GMPEs' regression curves are shifted to $\ln(\text{Amp})=0$ at a depth to the $V_s=1.0 \text{ km/s}$ isosurface of 0 m.

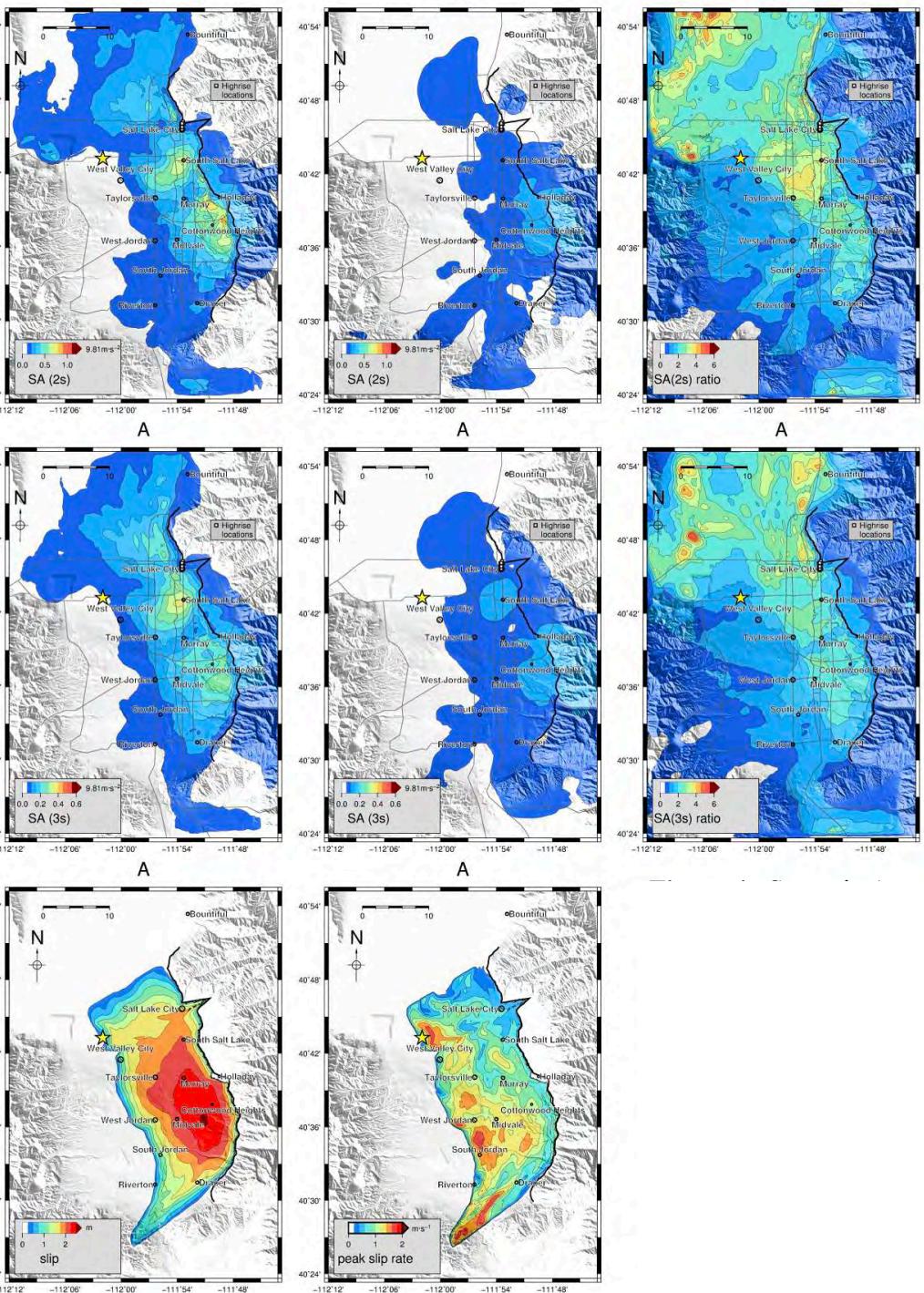


Comparison of the regression results for the basin depth amplification factors at a period of 2s from the GMPEs to the results of the simulations. The GMPEs' regression curves are shifted to $\ln(\text{Amp})=0$ at a depth to the $V_s=1.0 \text{ km/s}$ isosurface of 0m.

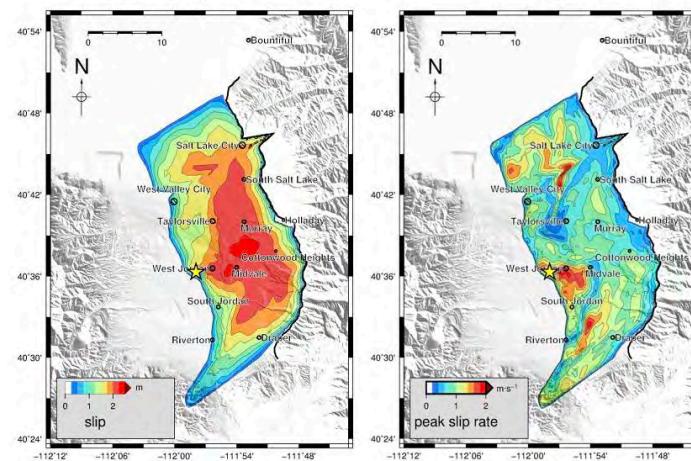
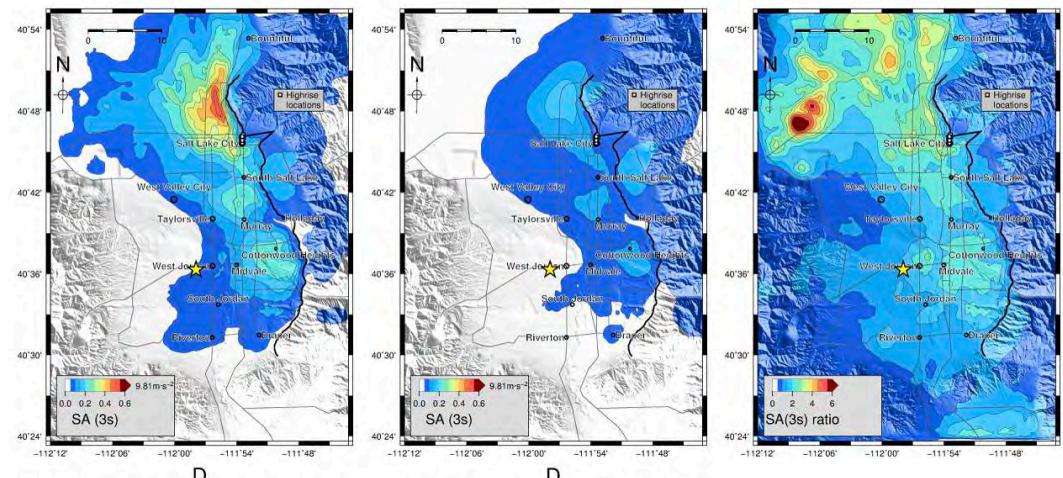
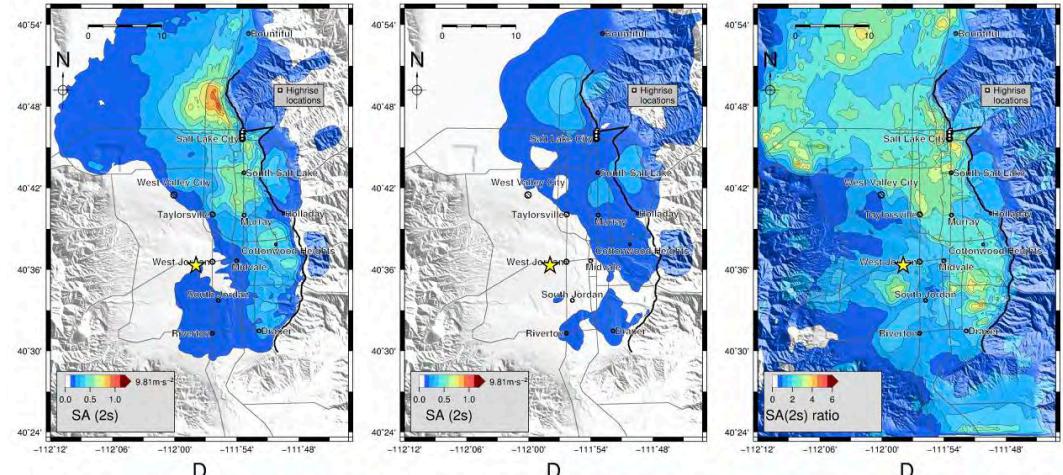


Correlation of SAs with
source parameters

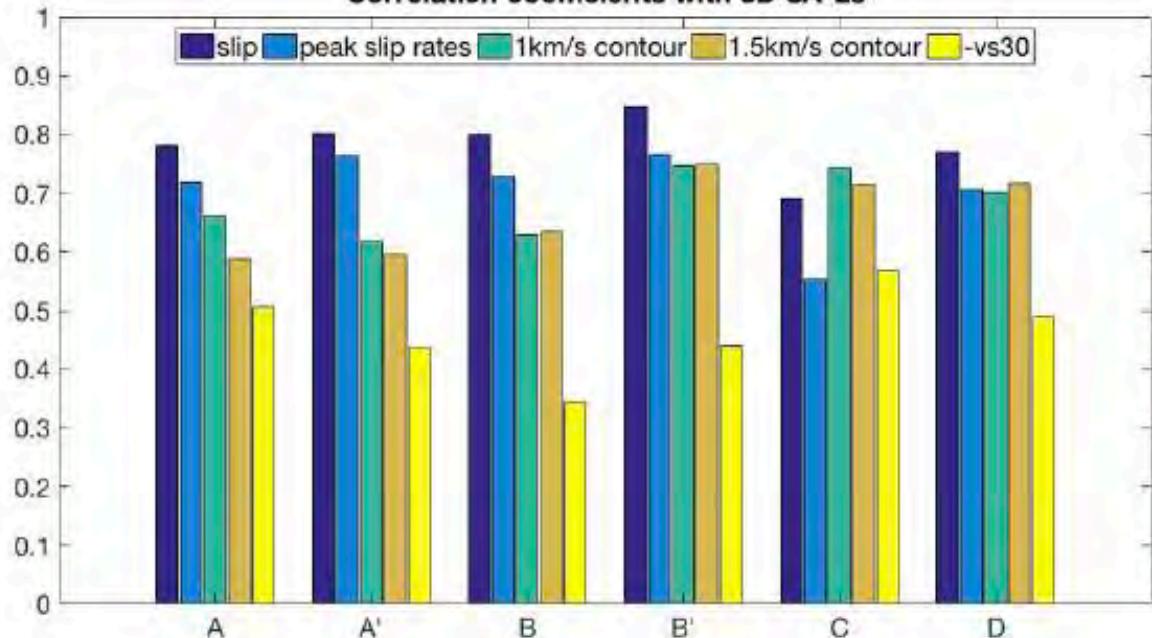
Correlation with slip and peak slip rate



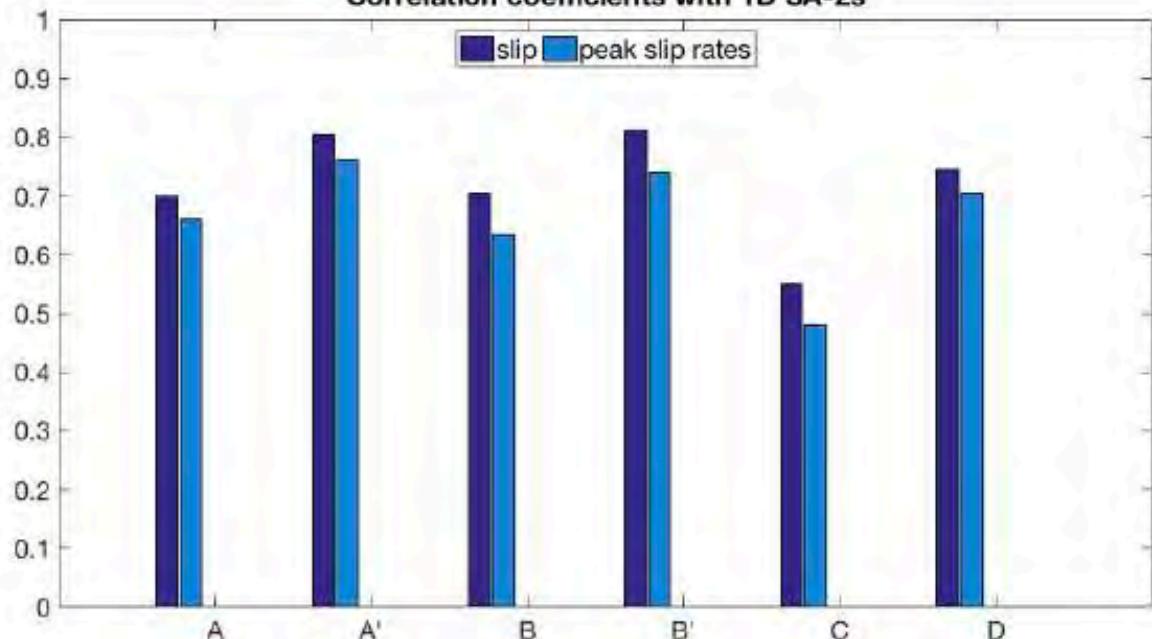
Correlation with slip and peak slip rate



Correlation coefficients with 3D SA-2s



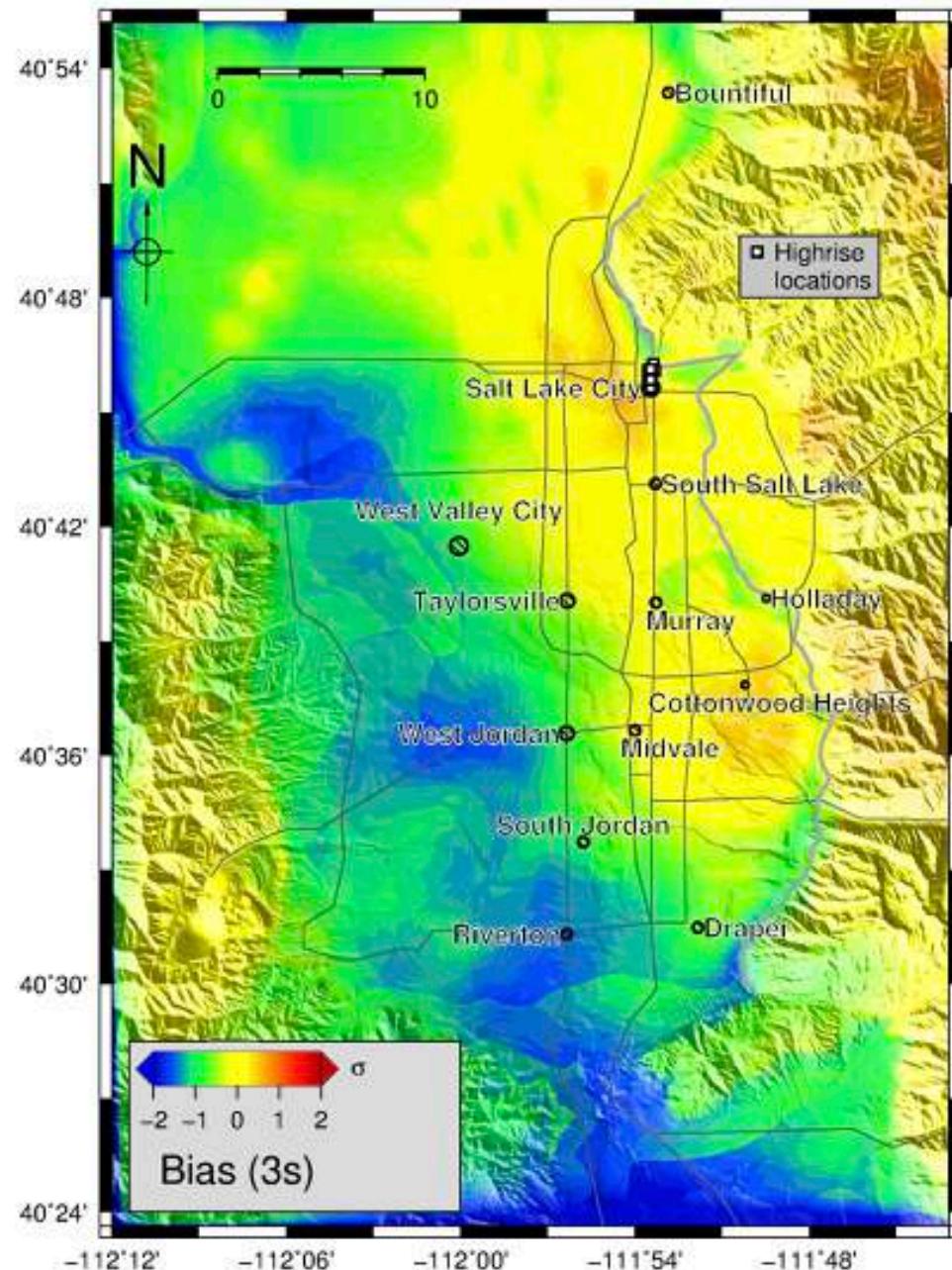
Correlation coefficients with 1D SA-2s



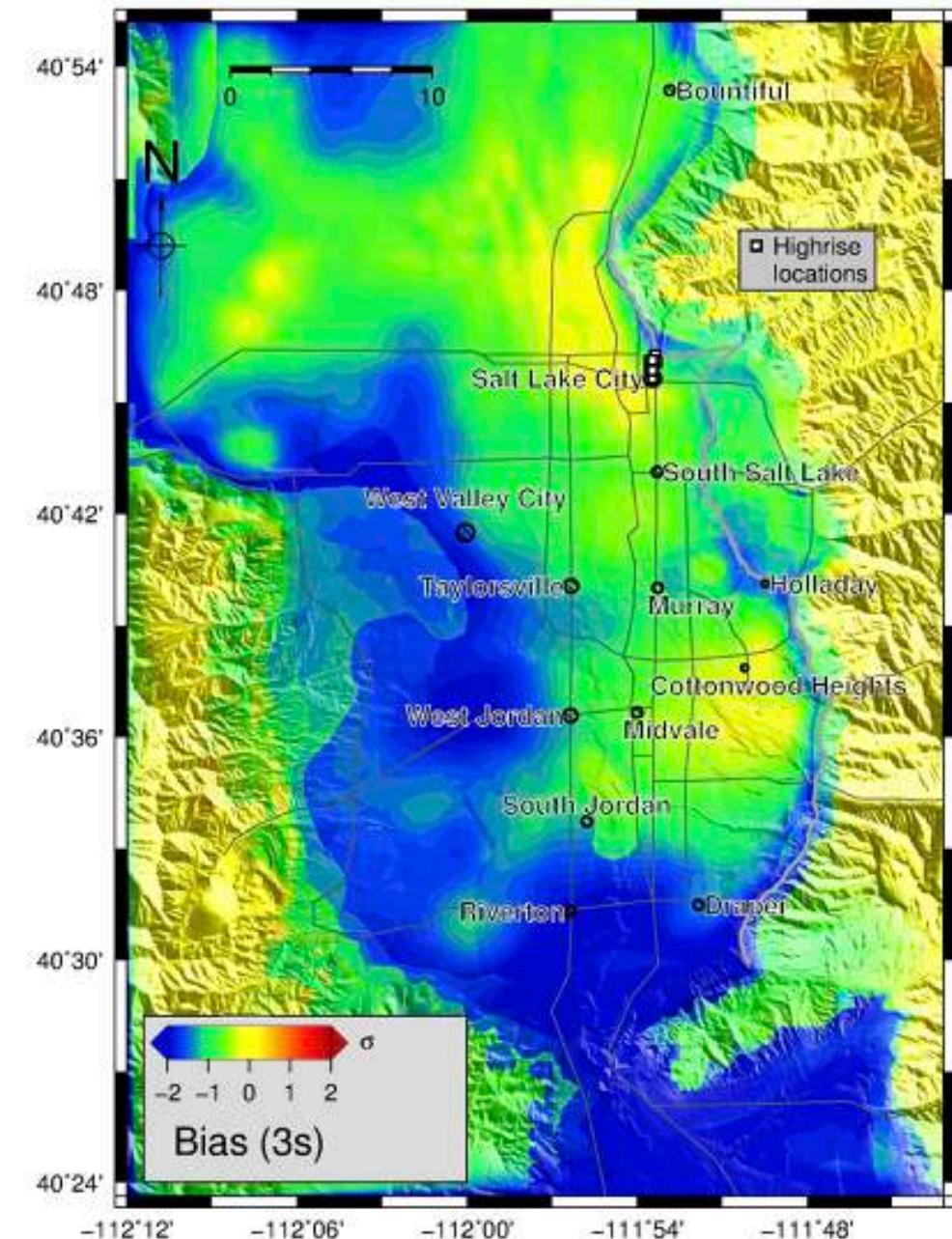
Distance Dependence for Ground Motion

Bias between
the ensemble
of SA-3s(3D)
and (left)
BSSA14 and
(right) CB14.

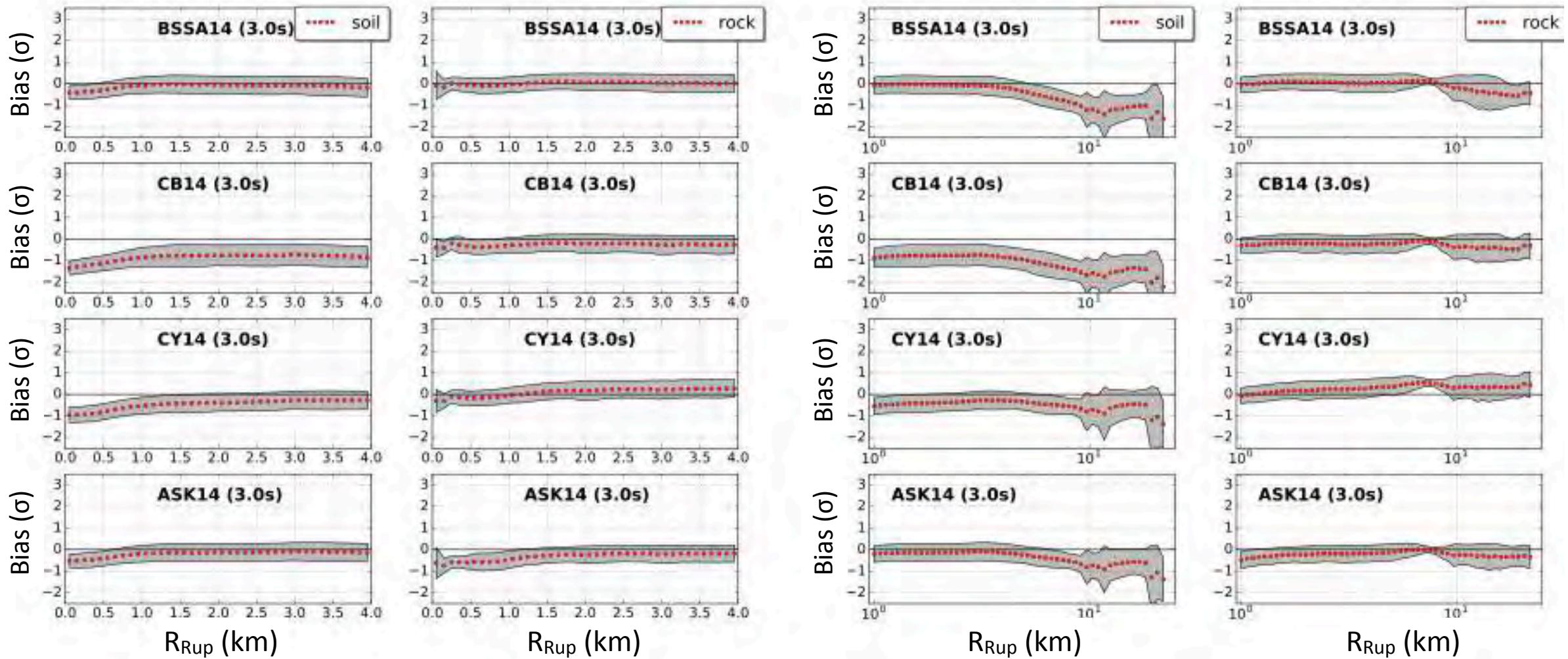
BSSA14



CB14

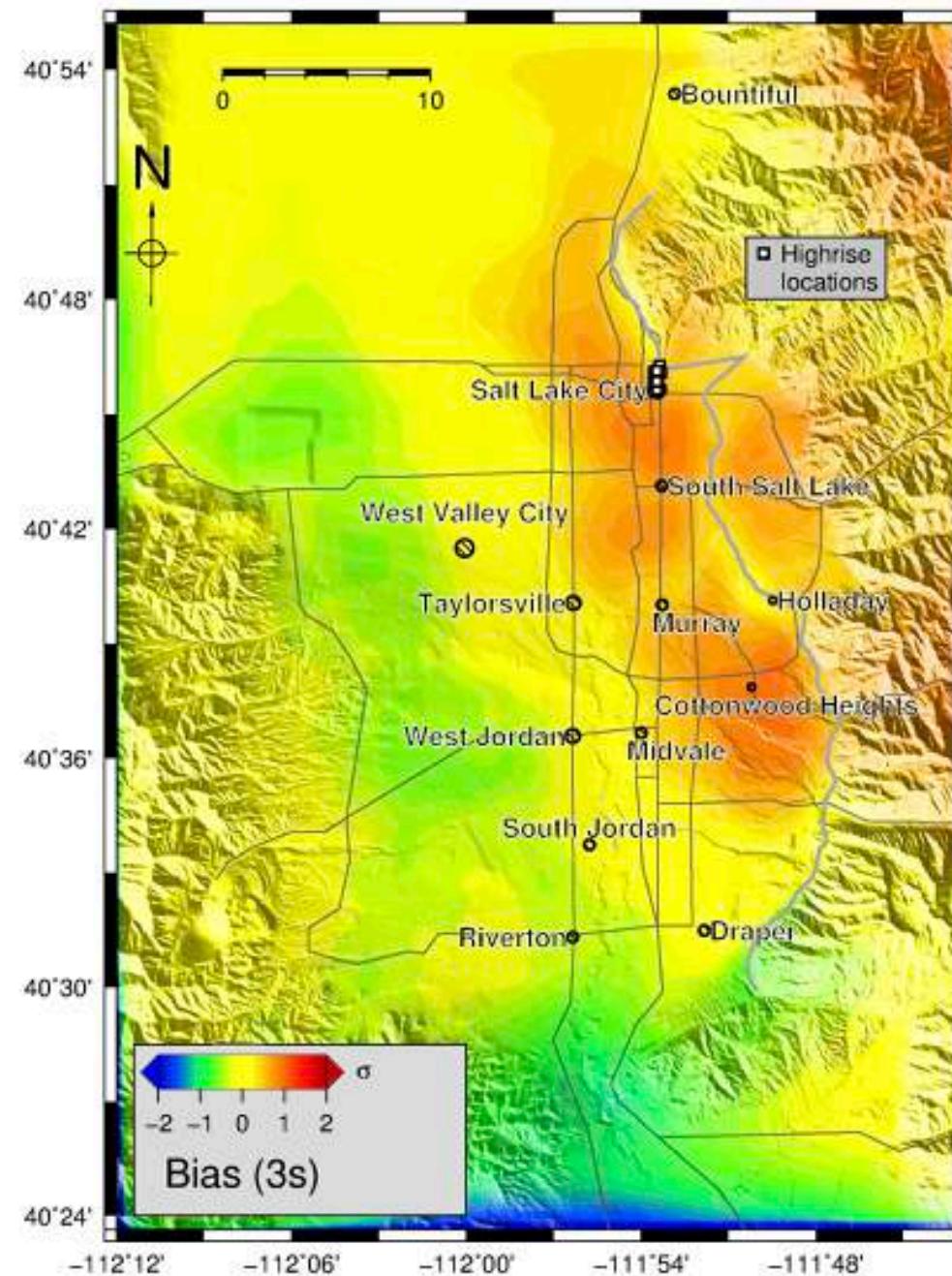


Bias between the 6-scenario ensemble of SA-3s(1D) and four leading NGAWest2 GMPEs for soil sites ($V_{s30} < 750$ m/s) and rock sites ($V_{s30} > 750$ m/s).

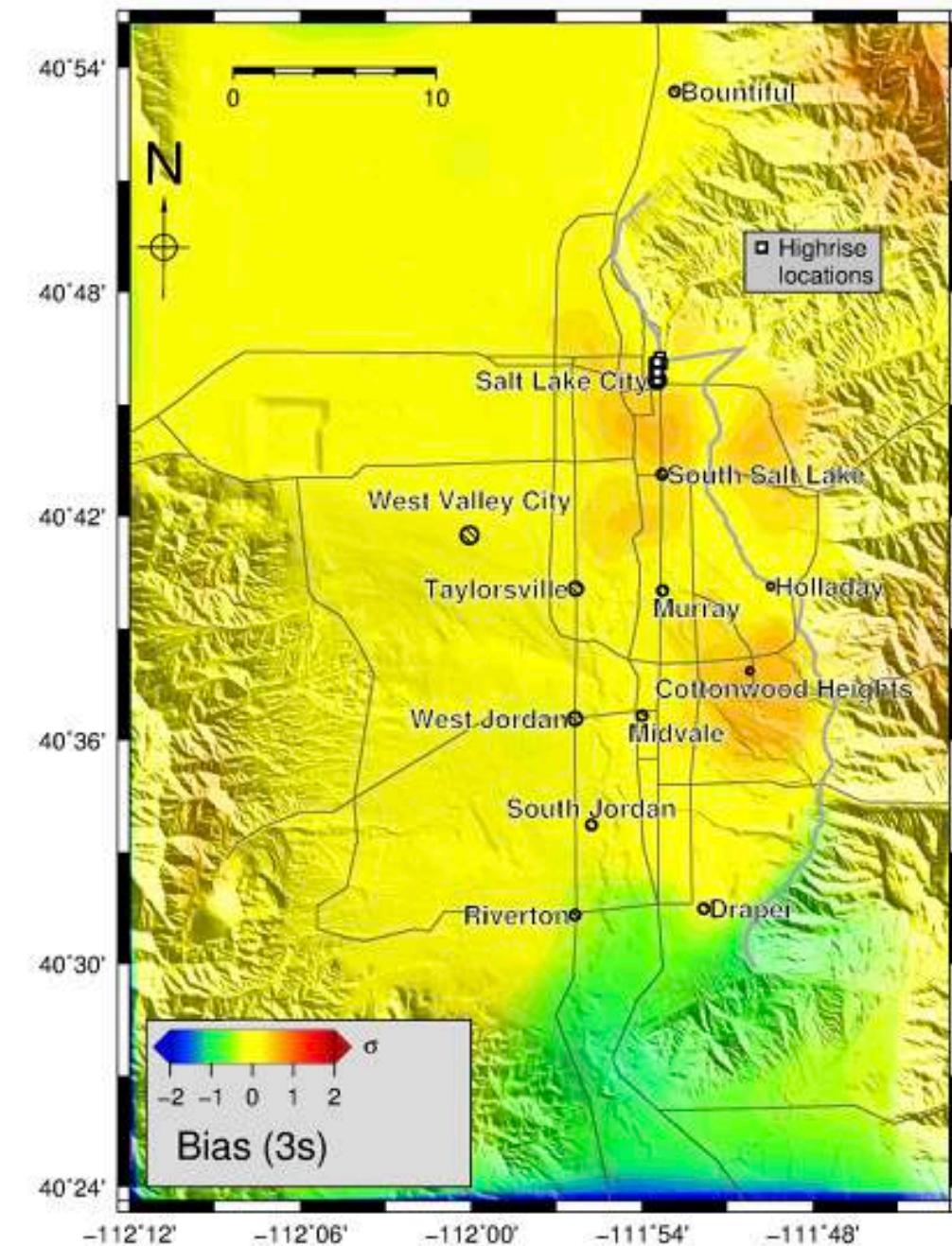


BSSA14

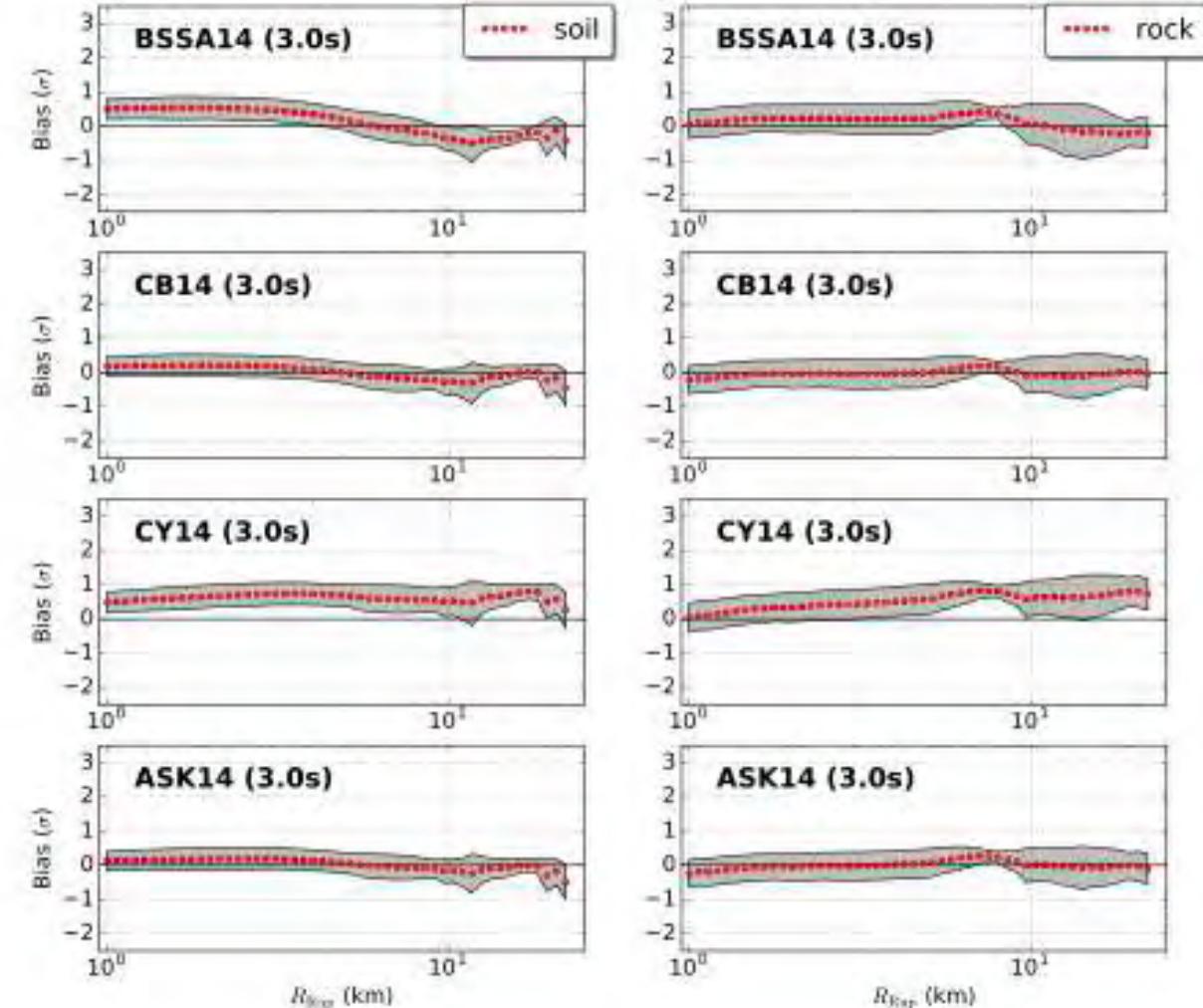
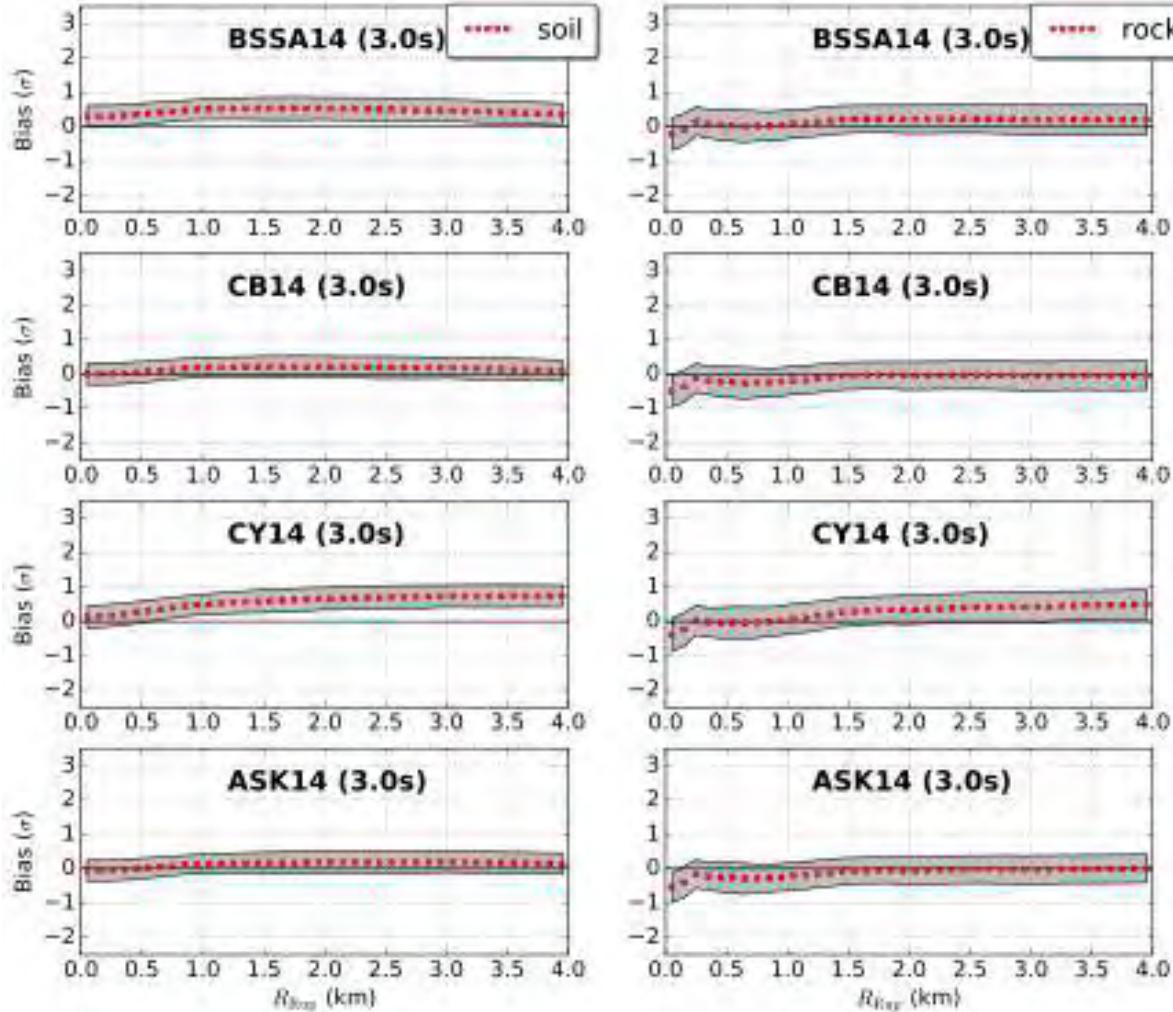
Bias between
the ensemble
of SA-3s(1D)
and (left)
BSSA14 and
(right) CB14.



CB14

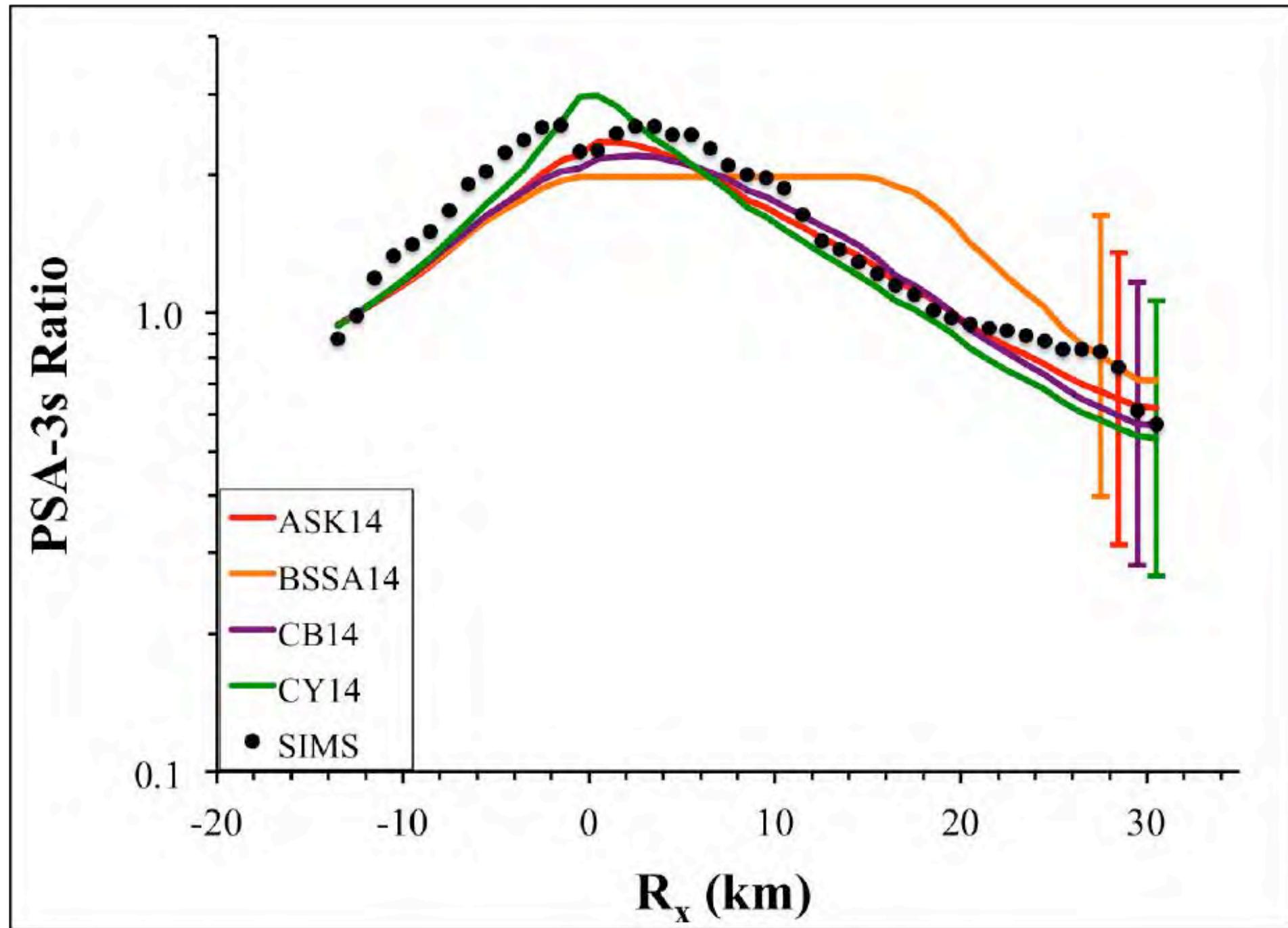


Bias between the 6-scenario ensemble of SA-3s(1D) and NGAWest2 GMPEs for soil sites ($V_{s30} < 750$ m/s) and rock sites ($V_{s30} > 750$ m/s).

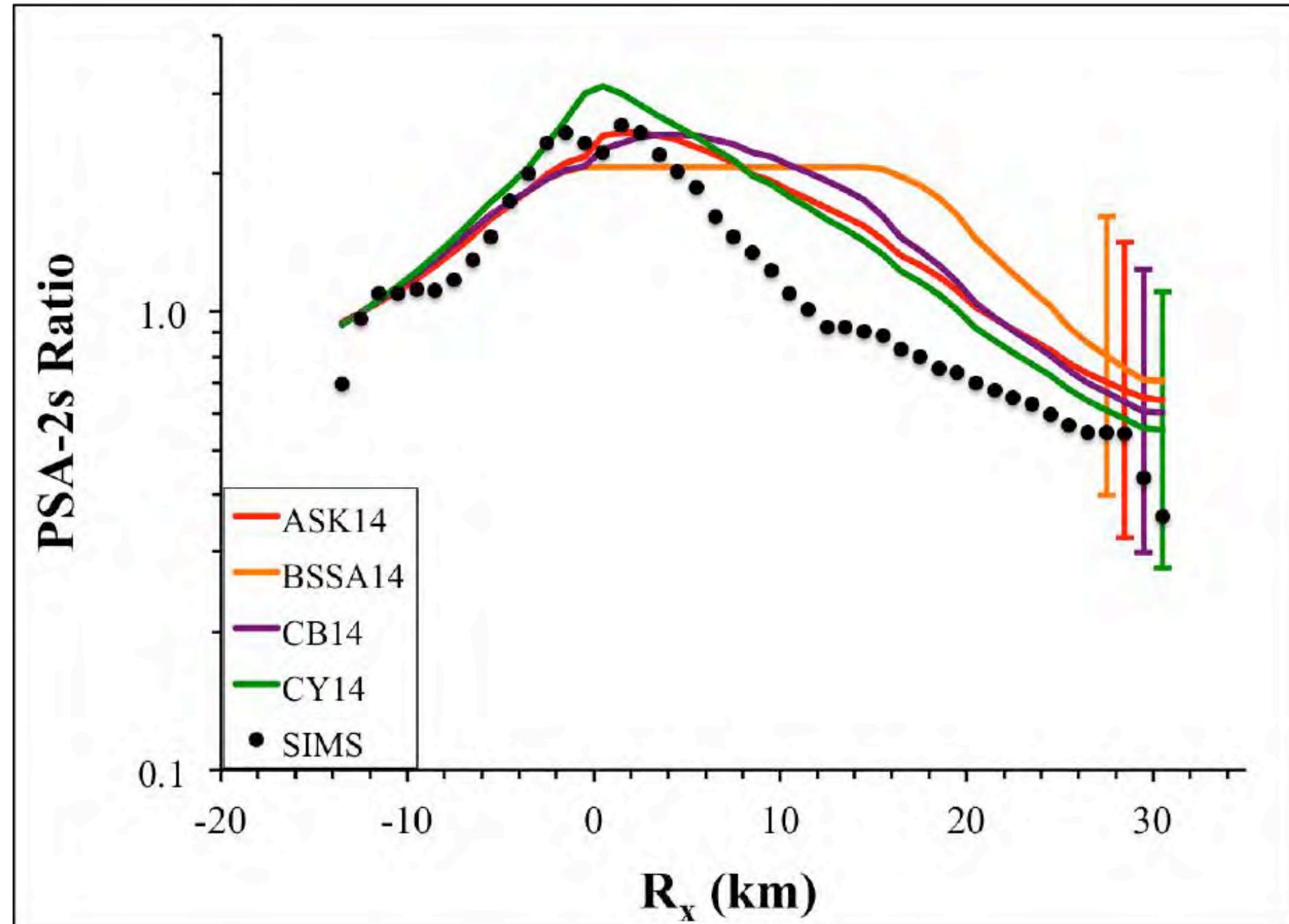


Hanging Wall Effects

Hanging-
wall
Effects
SA-3s



Hanging-
wall
Effects
SA-2s



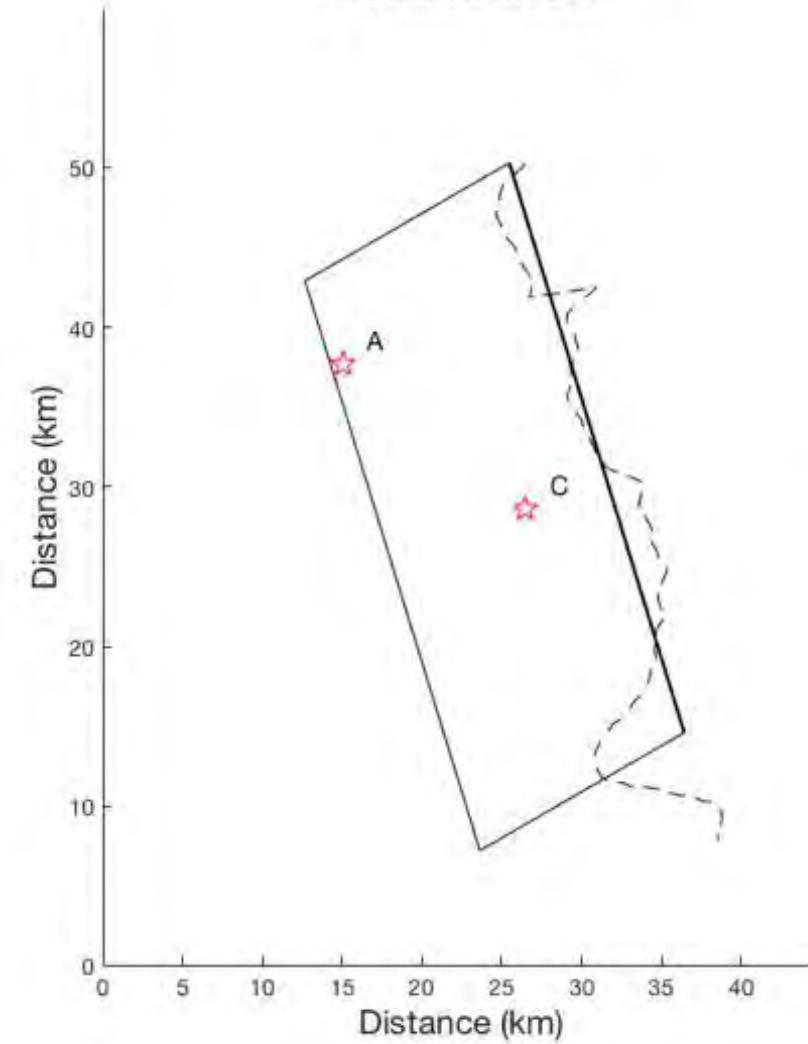
Directivity

Bayless and Somerville (2013) Multi-Segment Directivity Approach

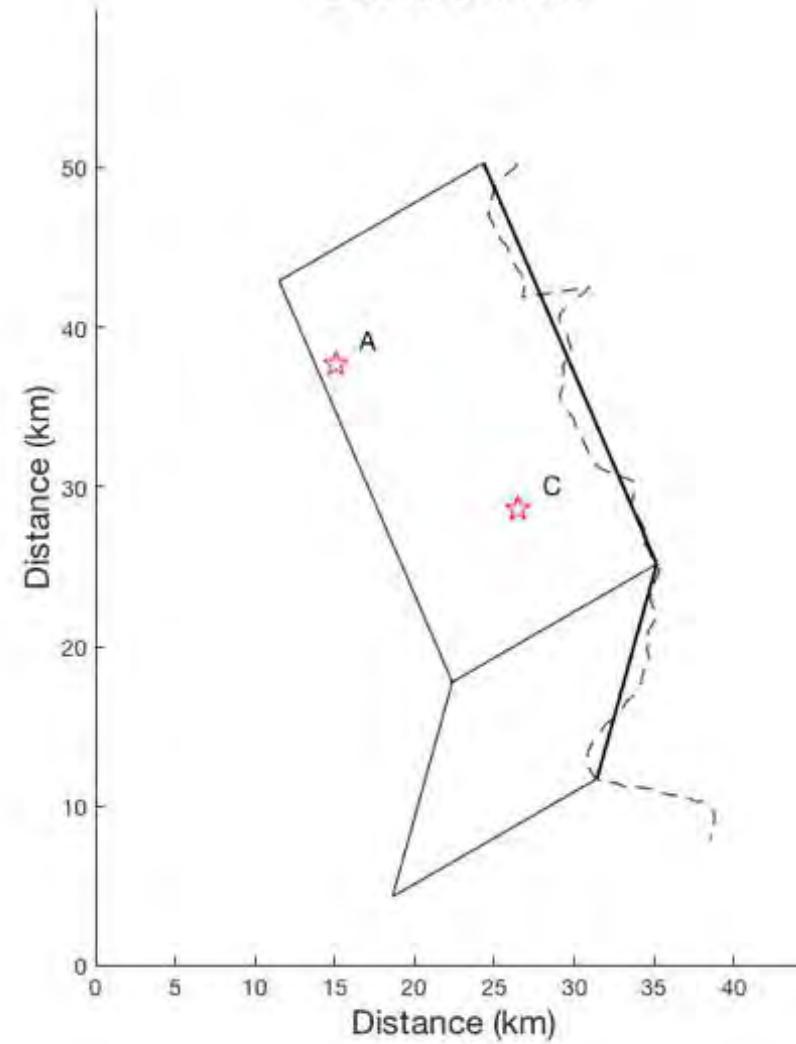
$$f_D = f_D(d, R_x, W, R_{rup}, M_w, A_z, T) = [C_0(T) + C_1(T) \ln(d) \cos(R_x/W)] T_{CD}(R_{rup}, W) T_{Mw}(M_w) T_{Az}(A_z),$$

Surface projections of WFSLC approximation models used in the calculation of directivity factors with the Bayless et al. (2013) model.

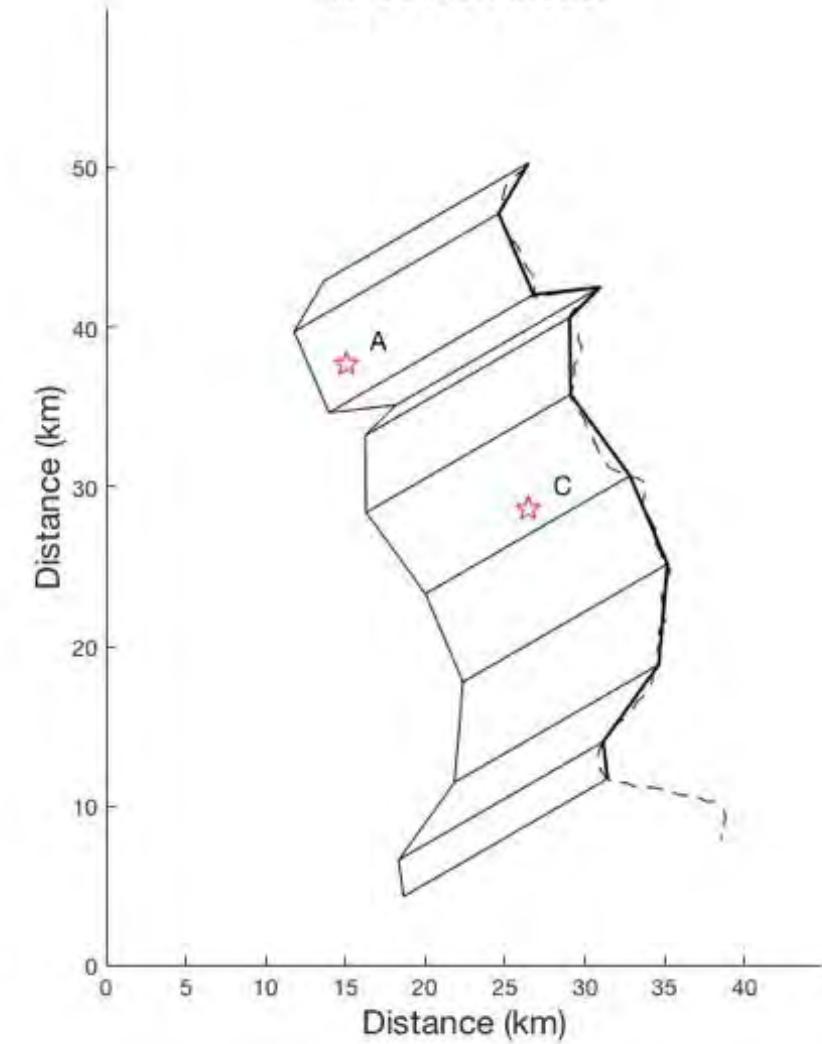
1-Section Model



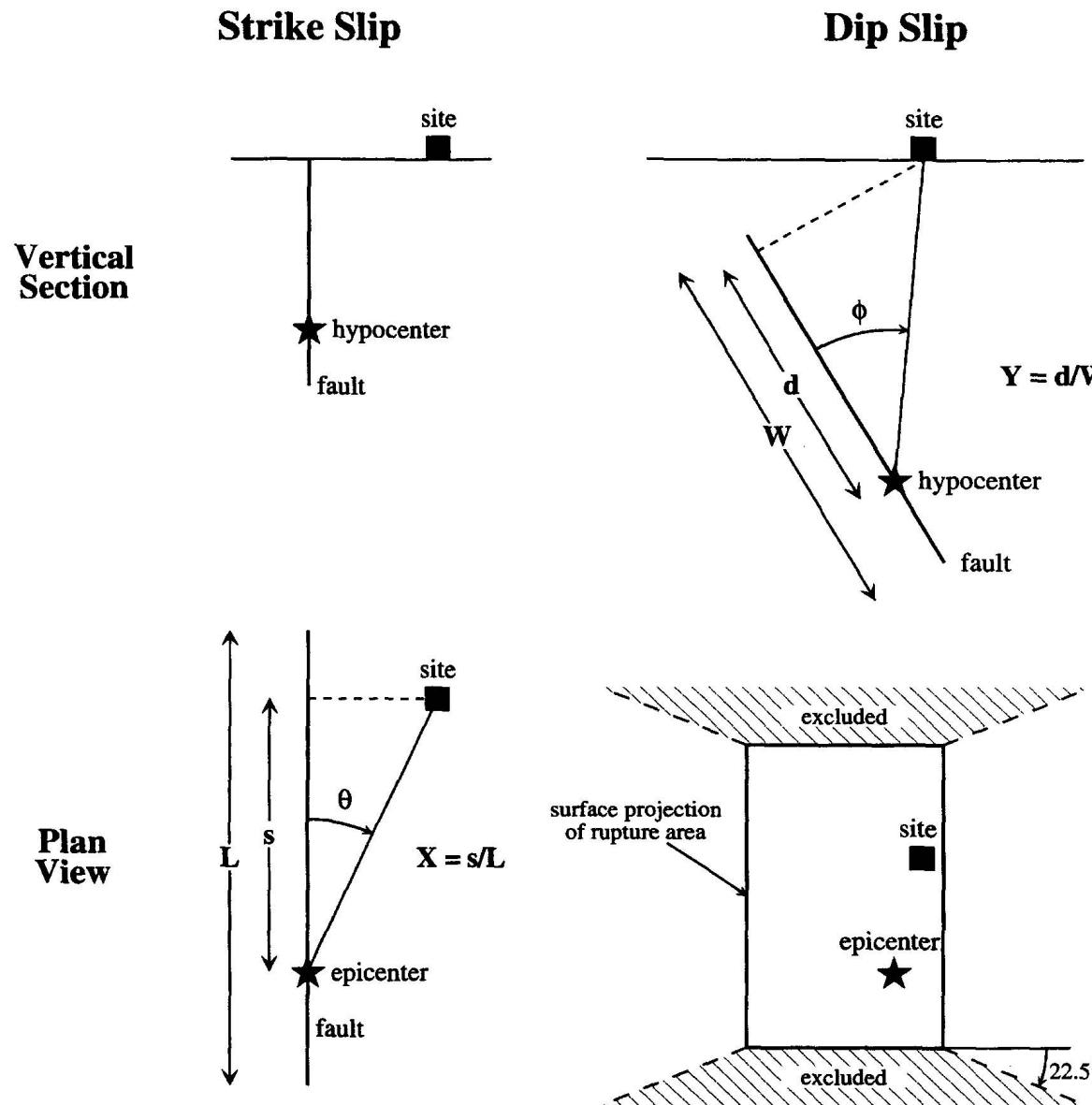
2-Section Model



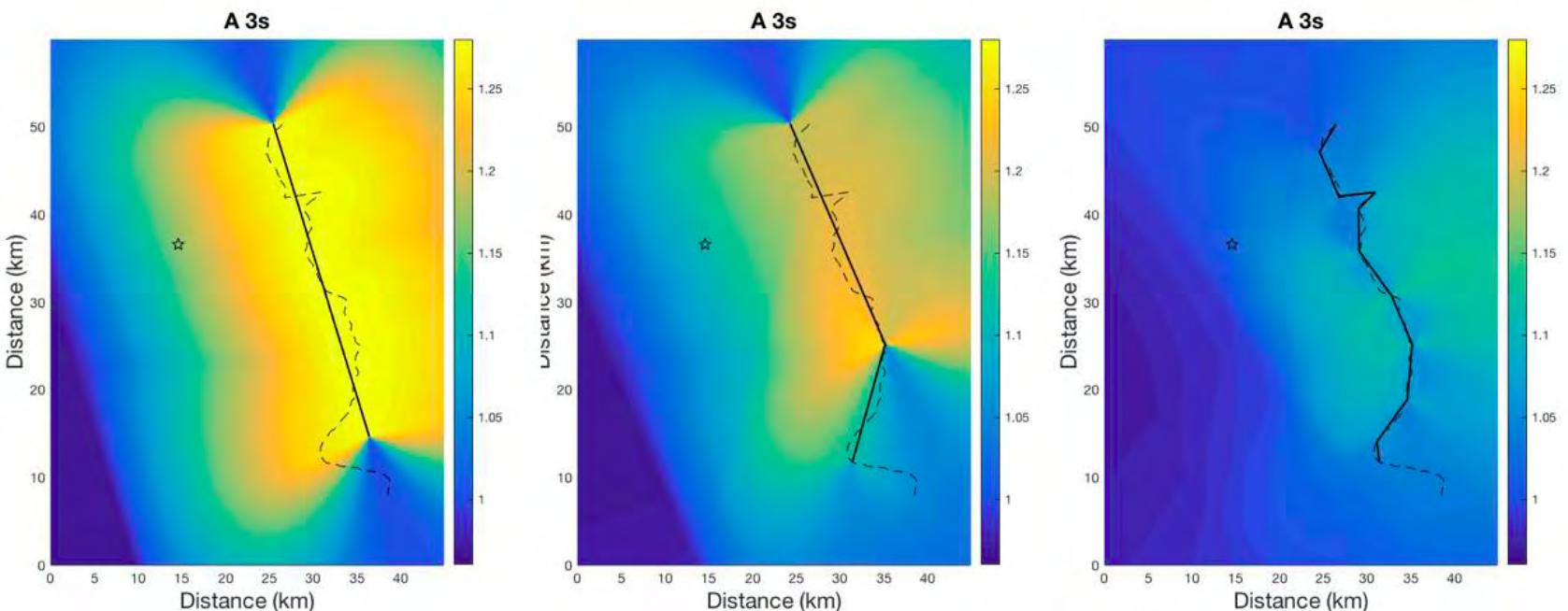
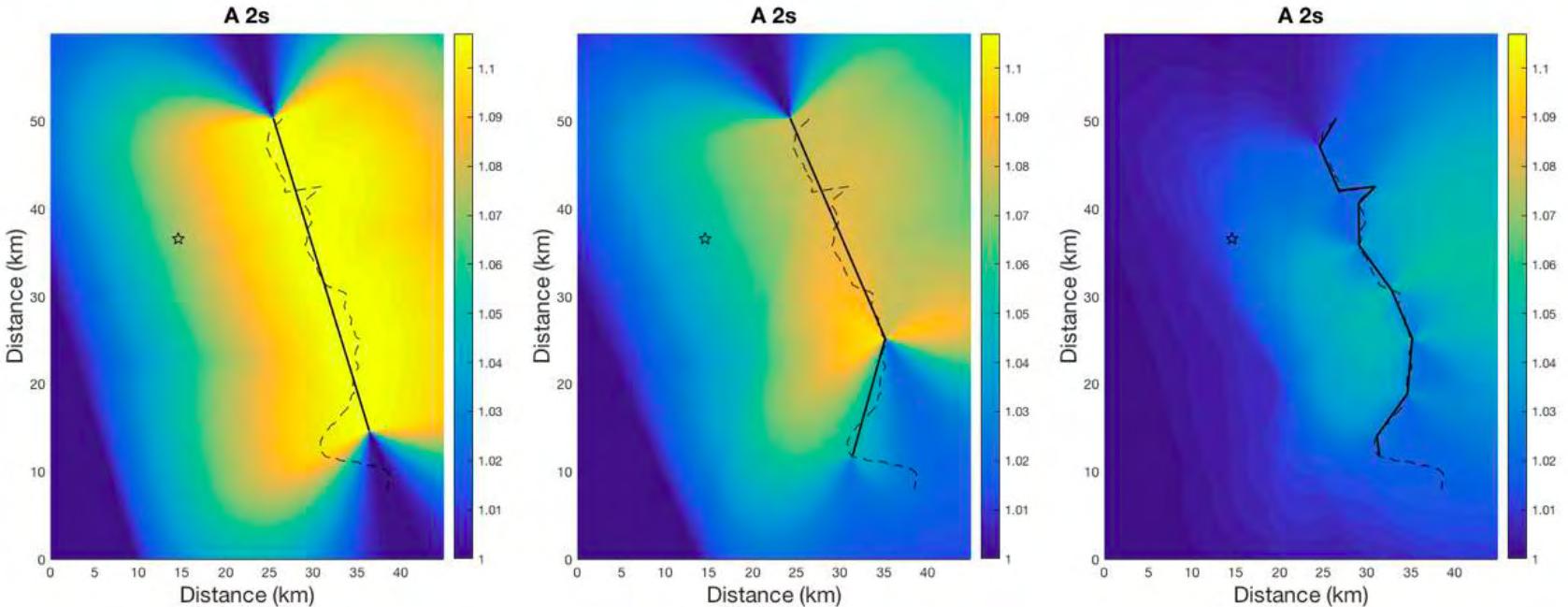
10-Section Model



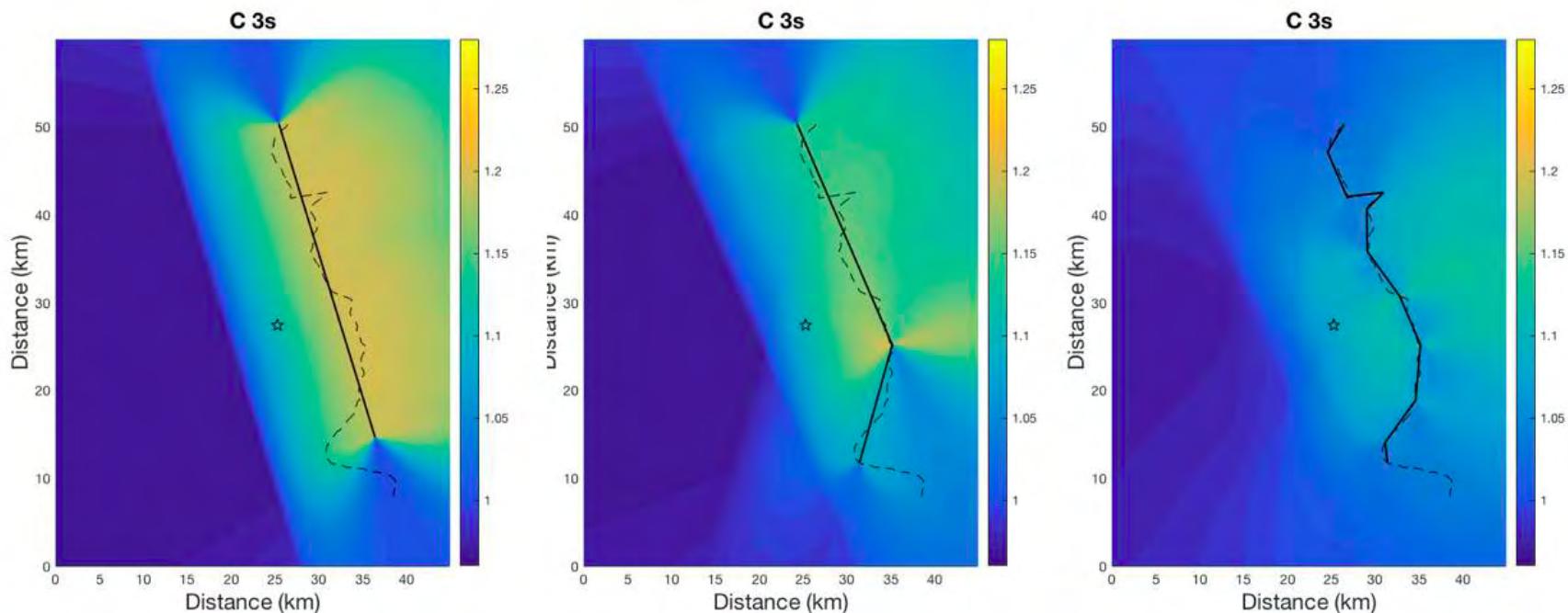
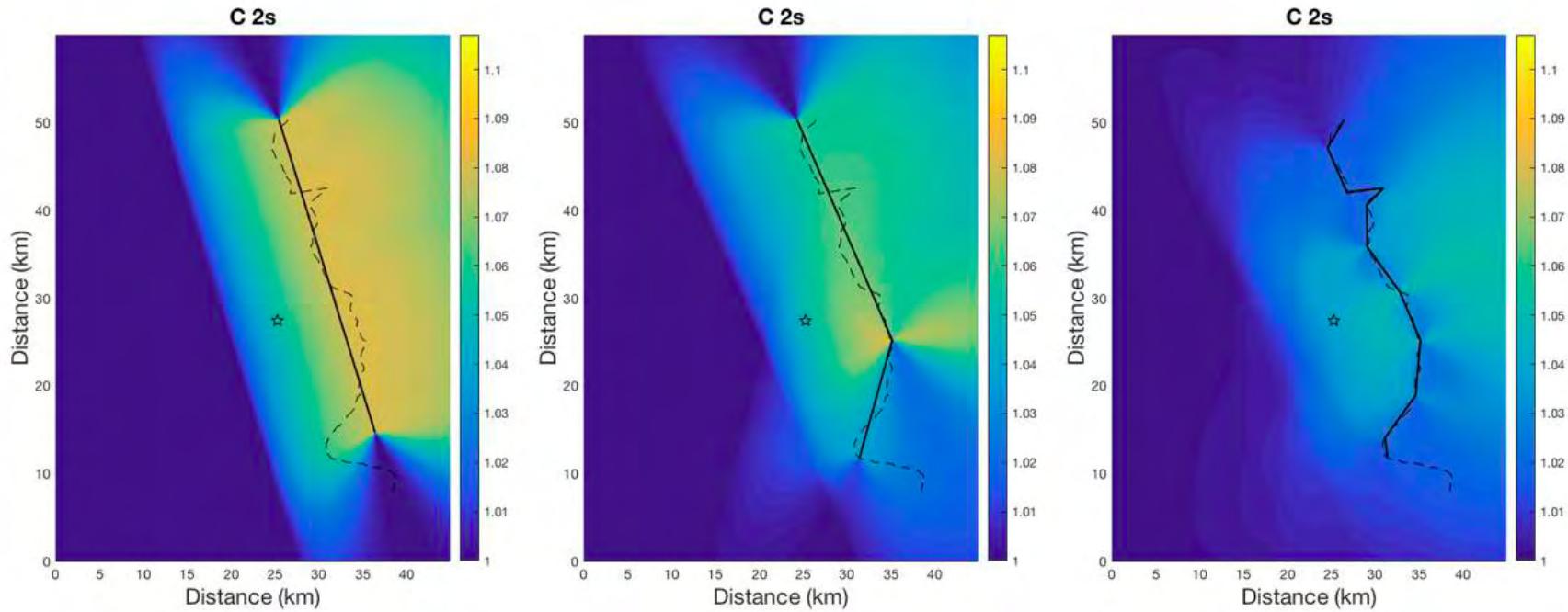
Multi-segment version of Somerville et al. (1997)



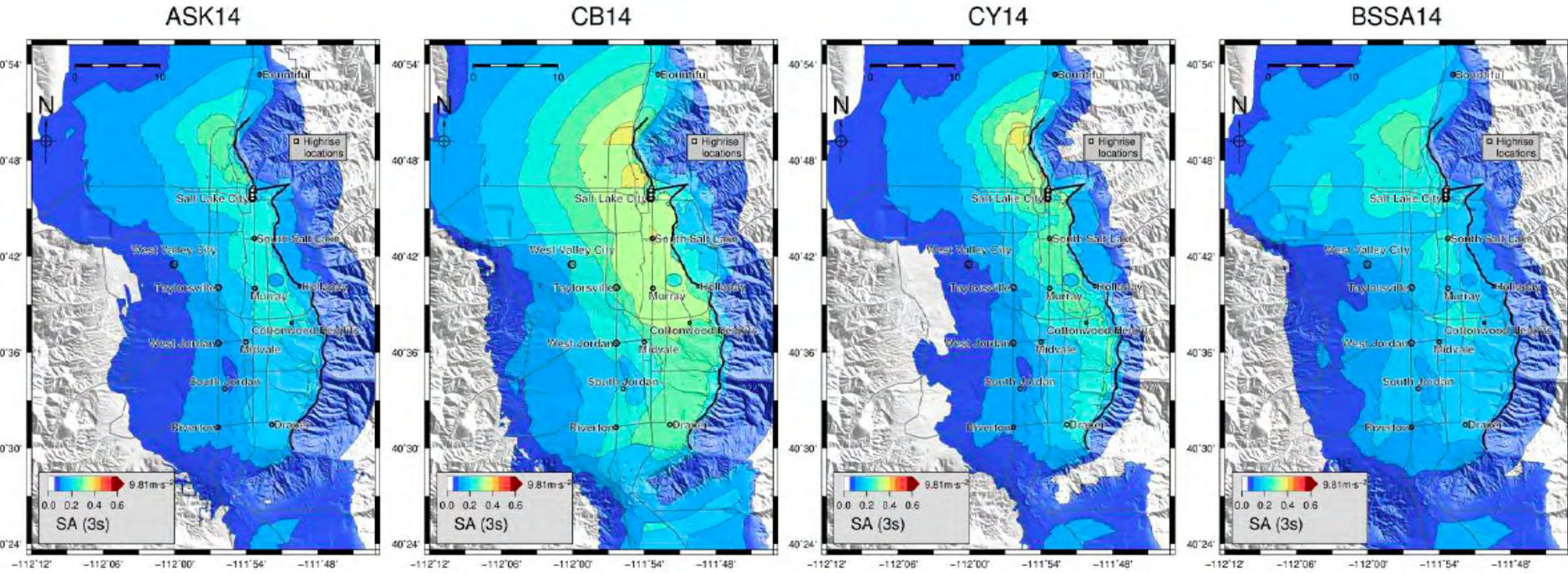
Maps of the directivity factors calculated from different WFSLC approximation models for scenario A



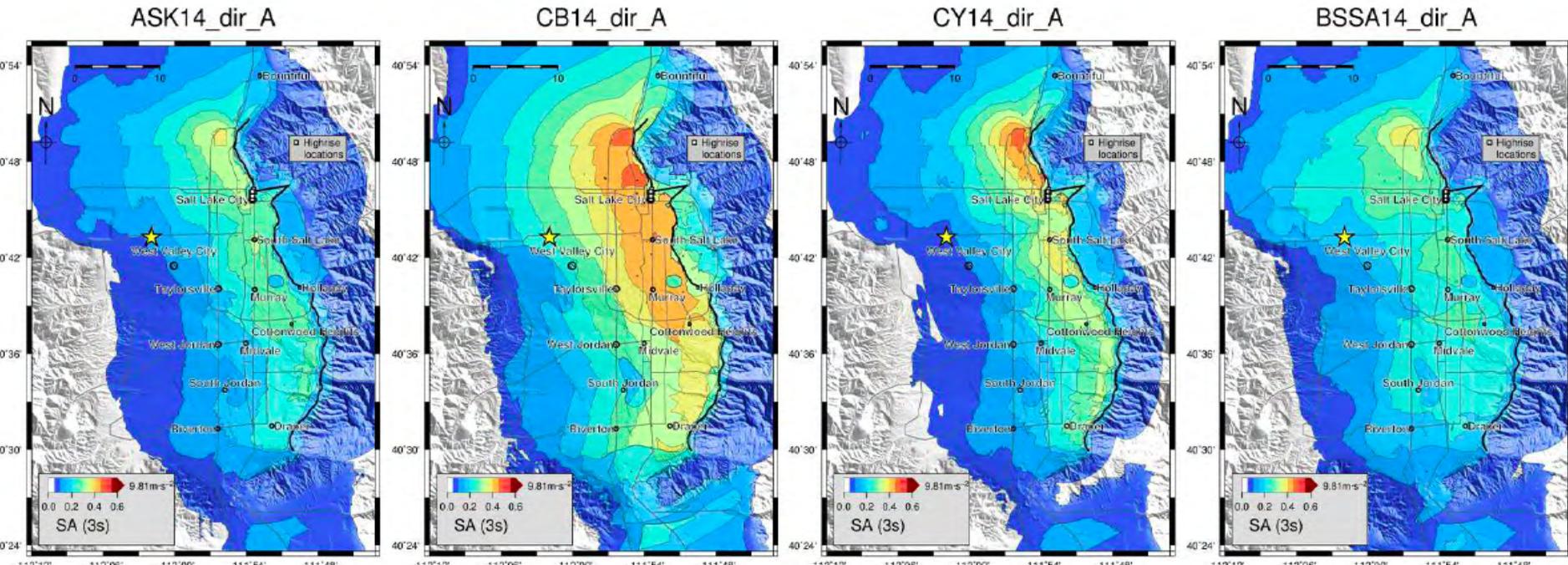
Maps of the directivity factors calculated from different WFSLC approximation models for scenario C



SA-3s for Scenario A.



SA-3s for Scenario A,
modified with the
directivity term from
Bayless and
Somerville (2013).



Conclusions

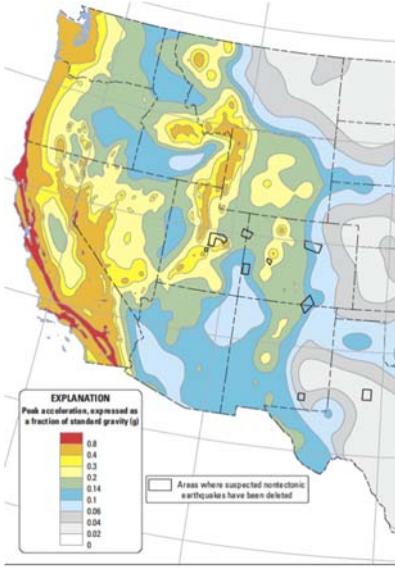
- SA-1D are generally smoother and smaller in amplitude than SA-3D due to higher Vs₃₀ values and the lack of underlying 3D structure
- The SAs show a strong correlation [0.6 to 0.8] with Vs=1.0 km/s and Vs=1.5 km/s in the WFCVM
- Parametric models for the 1.0 km/s isosurface show amplification factors of up to ~2.7 and ~3.7 above the deepest part of the basin for SAs
- Correlations between the long-period scenario ground motions in the SLV and the underlying fault slip range from 0.55 to 0.87
- The correlations with peak slip rate are somewhat lower, ranging from 0.41 to 0.80
- The source correlations are larger for the simulations using the 3D basin model, as compared to those obtained from the 1D model, suggesting an interaction between the source characteristics and the basin structure

Conclusions (cont.)

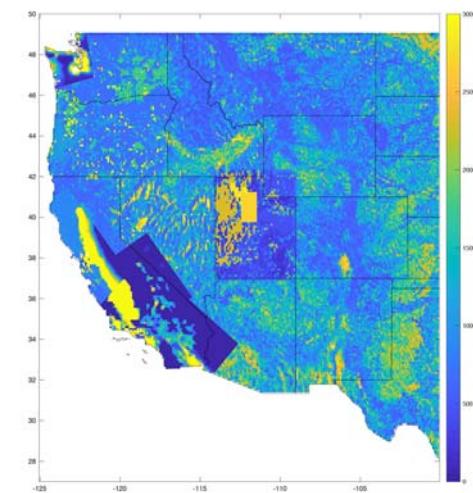
- Bayless and Somerville (2013) multi-segment directivity model increases the SA values by less than 30% for the scenarios
- The WF scenario ground motions on soil sites show a gradual increase in bias from $Rrup=0$ to 1-1.5 km → basin edge effect and/or entrapment of waves in the deeper parts of the basin, scenario specific conditions such as slip distributions not captured by the GMPEs + velocity strengthening in source model
- The WF scenario ground motions on soil sites show a gradual decrease in bias from $Rrup\sim 4$ to ~ 10 km → basin as well as directivity effects, westward termination of the WF, slip in the M7 scenarios?
- GMPEs do a reasonably good job of predicting the increased ground motions over the hanging wall for SA-3s, but overpredict slightly for SA-2s

Incorporating basin effects into NSHM

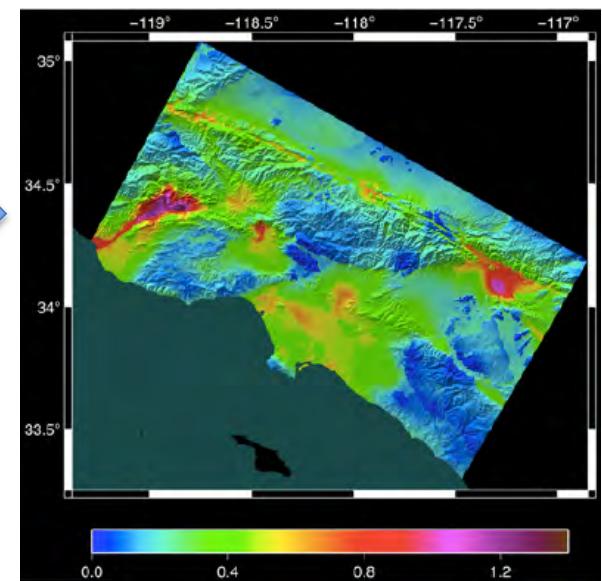
Default basin depths



WUS-wide basin depths



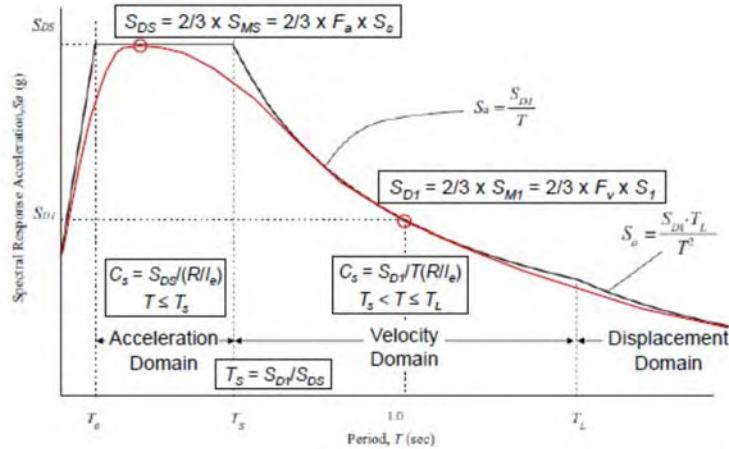
3-D ground motion simulations



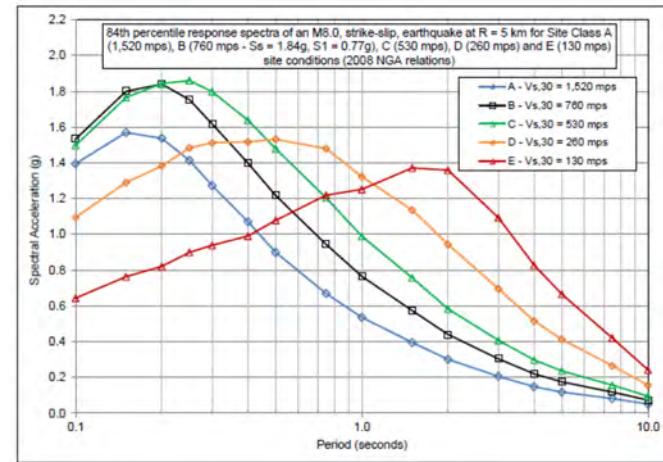
- 1) Empirically based GMPEs, default basin depths
- 2) Empirically based GMPEs, basin depths from seismic velocity models
- 3) Empirically based GMPEs, basin amplifications from 3-D simulations

Multi-Period Spectrum:

ASCE 7 Design Spectrum based on Ss and S1:



Kircher study showing that the spectral shape varies:



- **Solution:** USGS to develop maps for more periods and site-classes in addition to the Ss and S1 value maps at BC site-class.
- **At long periods:** due to the questionable accuracy of GMPEs, multi-period spectra can benefit from utilizing simulations

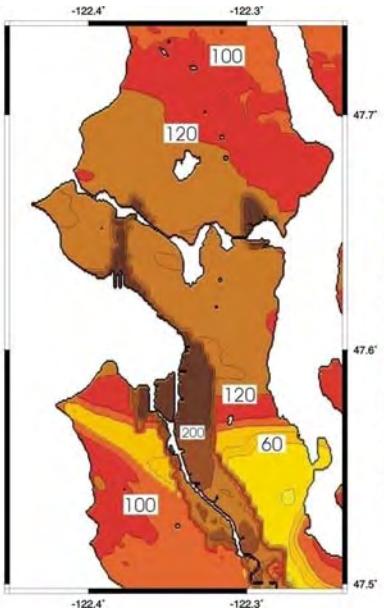
(slide courtesy Sanaz Rezaeian)

Outline

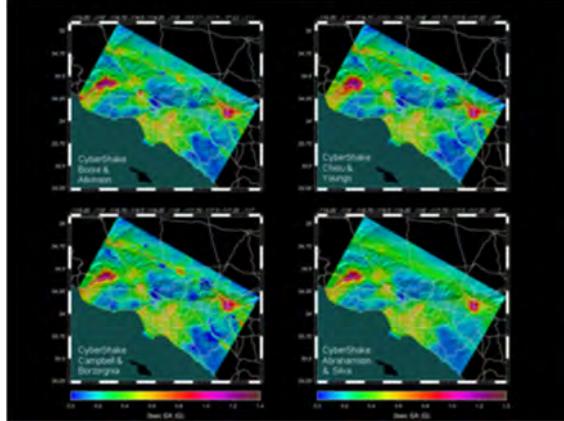
- *Plan for incorporating basin effects from empirically based GMPEs – presentation by Mark Petersen (USGS)*
 - Sensitivity of hazard to basin depths (NSHM-2018)
 - Plan for developing WUS-wide Zx maps (NSHM-2018/2020)
- ***Context for simulation-based seismic hazard analyses across the U.S.***
- ***US Geological Survey efforts around “urban seismic hazard maps”***
- ***Plan for harmonizing Urban and National Seismic Hazard Models (USHM/NSHM)***
- ***Plan for incorporating ground motions from 3-D simulations into NSHM***
 - Update from Working Group on Urban Seismic Hazard Maps:
white paper on harmonizing USHMs and NSHM
 - Incorporating 3-D ground motions into the NSHM

Working Group motivation: Urban seismic hazard maps

Seattle



Los Angeles (CyberShake)



Evansville, IN



St. Louis



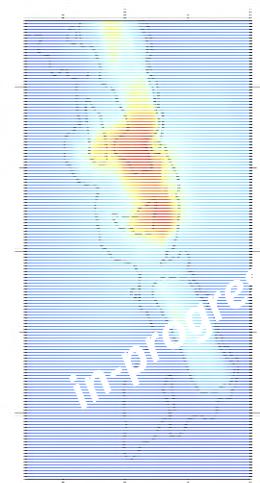
What is earthquake hazard?

Hazard is currently cannot be predicted, but scientists can estimate how strong an earthquake will be based on the type of rock it passes through. The U.S. Geological Survey (USGS), which produces earthquake hazard maps for the Nation, is working with local partners to produce hazard maps for the St. Louis area. The USGS and its partners in the St. Louis Area Earthquake Hazard Mapping Project include the Missouri University of Science and Technology, Missouri Department of Natural Resources, Illinois State Geological Survey, Saint Louis University, Missouri State Emergency Management Agency, and CDM Corporation.

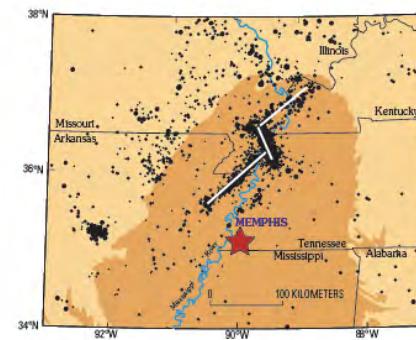
Who uses earthquake hazard maps?

Public and private groups can use hazard maps for planning, engineering, and emergency preparedness decisions resulting from earthquake shaking. Planners can use the maps to identify areas where buildings are most vulnerable and where new structures can be built more safely. Engineers can use the maps to better manage risk exposures. Businesses can use the maps to evaluate potential risks to their operations. Individuals can use the maps to better consider the location of their home and consideration in locating new developments, schools, day care centers, and emergency facilities. Businesses can use the maps to evaluate potential risks to their operations. Individuals can use the maps to better consider the location of their home and

Salt Lake City



Memphis



Multiple classes of urban seismic hazard maps

- 3-D simulation-based ground-motions* (Seattle and southern California)
- Near-vertical propagation of S-waves to account for effects of shallow sub-surface
- Vs30-based GMPE calculations

Working Group Composition, Goals, History

- Internal U.S. Geological Survey Working Group
- Goals
 - Address technical and programmatic issues related to USHMs
 - Responding to available urban seismic hazard maps
 - (*Largely focusing on incorporating ground motions from 3-D simulations*)

Morgan Moschetti*
Nico Luco*
Brad Aagaard
Annemarie Baltay*
Mike Blanpied
Oliver Boyd*
Art Frankel*
Rob Graves*
Steve Hartzell
Sue Perry
Mark Petersen*
Sanaz Rezaeian
Bill Stephenson
Eric Thompson*
Rob Williams
Kyle Withers

OPINION

Integrate Urban-Scale Seismic Hazard Analyses with the U.S. National Seismic Hazard Model

For more than 20 yrs, damage patterns and instrumental recordings have highlighted the influence of the local 3D geologic structure on earthquake ground motion (e.g., M 6.7 Northridge, California, [Gao et al., 1996](#); M 6.9 Kobe, Japan, [Kawase, 1996](#); M 6.8 Nisqually, Washington, [Frankel et al., 2002](#)). Although this and other local-scale features are critical to improving seismic hazard forecasts, historically they have not been explicitly incorporated into the U.S. National Seismic Hazard Model (NSHM, national model and maps), primarily because the necessary basin maps and methodologies were not available at the national scale. Instead, the U.S. Geological Survey (USGS), its partners, and external groups developed urban seismic hazard maps (urban models and maps) that consider detailed site effects in local areas (e.g., [Wong et al., 2002; Cramer et al., 2006; Frankel et al., 2007; Graves et al., 2011](#)). The disconnect between the urban and national hazard models, however, means that the national models, which underlie U.S. building codes and other applications, do not make use of all of the scientific results informing earthquake ground-shak-

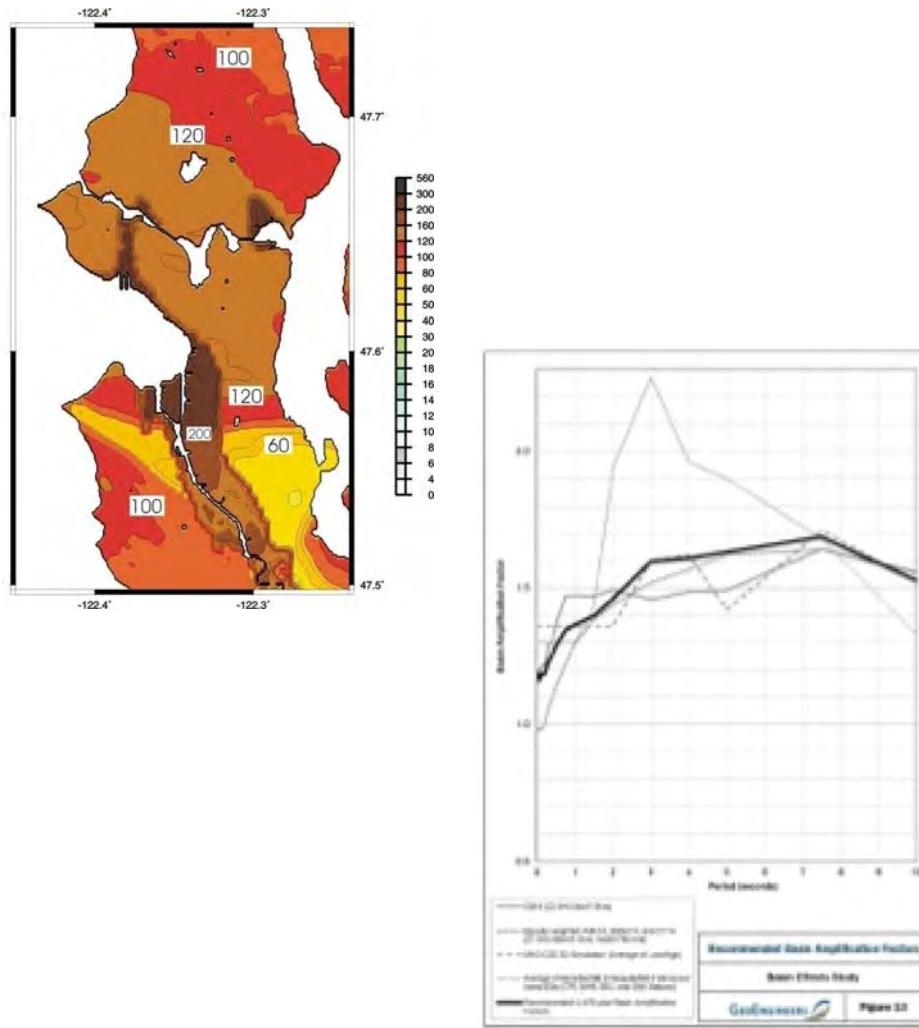
comparison of hazard in different parts of the country ([Frankel et al., 2000; Moschetti et al., 2015; Rezaeian et al., 2015](#)). Since 1996, the hazard maps have directly formed the basis for the seismic provisions in U.S. building codes ([Leyendecker et al., 2006; Frankel et al., 2002; Petersen et al., 2008, 2015; Luco et al., 2015](#)). The connection between U.S. building codes and the NSHM represents one critical way in which knowledge about earthquake occurrences and effects can be used to reduce seismic risk. Because of this role, the NSHM updates must achieve widespread consensus from the scientific and engineering communities. This model-vetting process has historically been achieved through a series of public workshops which have solicited feedback and new scientific models ([Frankel et al., 2000; Petersen et al., 2015](#)). As a consequence, the NSHM represents a state-of-practice for earthquake science.

Urban-Scale Seismic Hazard Assessments

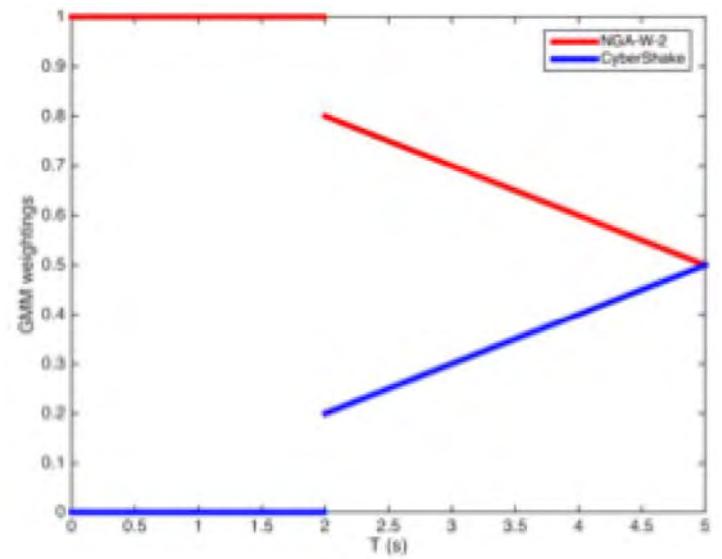
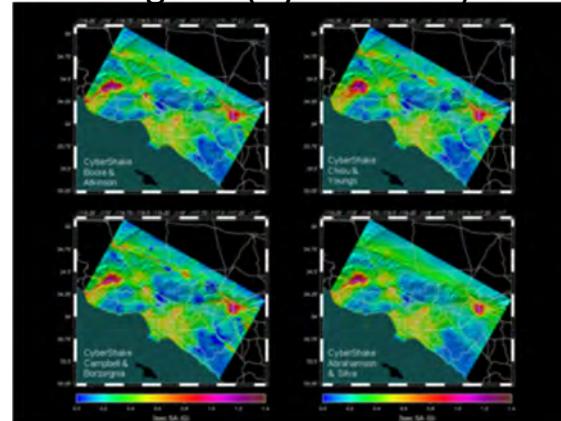
In parallel with these national-scale analyses, a growing number

Local engineering use of ground motions from 3-D simulations

Seattle



Los Angeles (CyberShake)



Working Group Recommendations on integrating USHMs and NSHM

- NSHM should integrate well-vetted features of USHMs with national-scale seismic hazard assessments
- Moving forward we expect that USHMs will make increasingly important contributions to NSHM
- USHMs remain independent products
 - USHMs are a “platform for cutting-edge research into topics affecting earthquake ground shaking forecasts and have helped to define important scientific questions and motivate future research”
 - Integration of USHM features will be facilitated by early and on-going coordination with NSHMP

Background on and plan for incorporating ground motions from 3-D simulations into NSHM

- Based on feedback from WG-USHM, Earthquake Hazards Program, NSHMP Steering Committee
- Only incorporate well-vetted components from earthquake simulations
 - Focus on basin amplifications
 - Not (currently) considering effects from path, directivity, source complexity
- Validate the simulated ground motions (or components); are simulations providing improvements to empirically based predictions

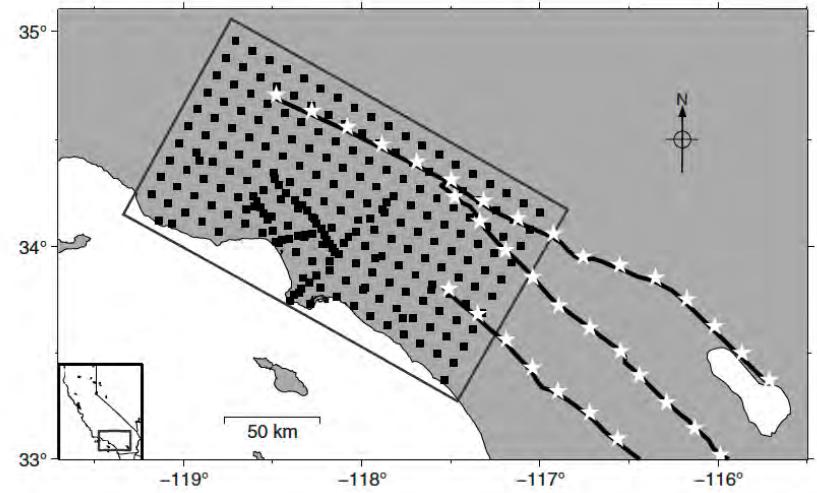
Averaging-based factorization (ABF)

(Wang and Jordan, 2014)

$$G(r, k, x, s) \equiv \ln Y(r, k, x, s).$$

$$A \xleftarrow{R} B \xleftarrow{K} C \xleftarrow{X} D \xleftarrow{S} E.$$

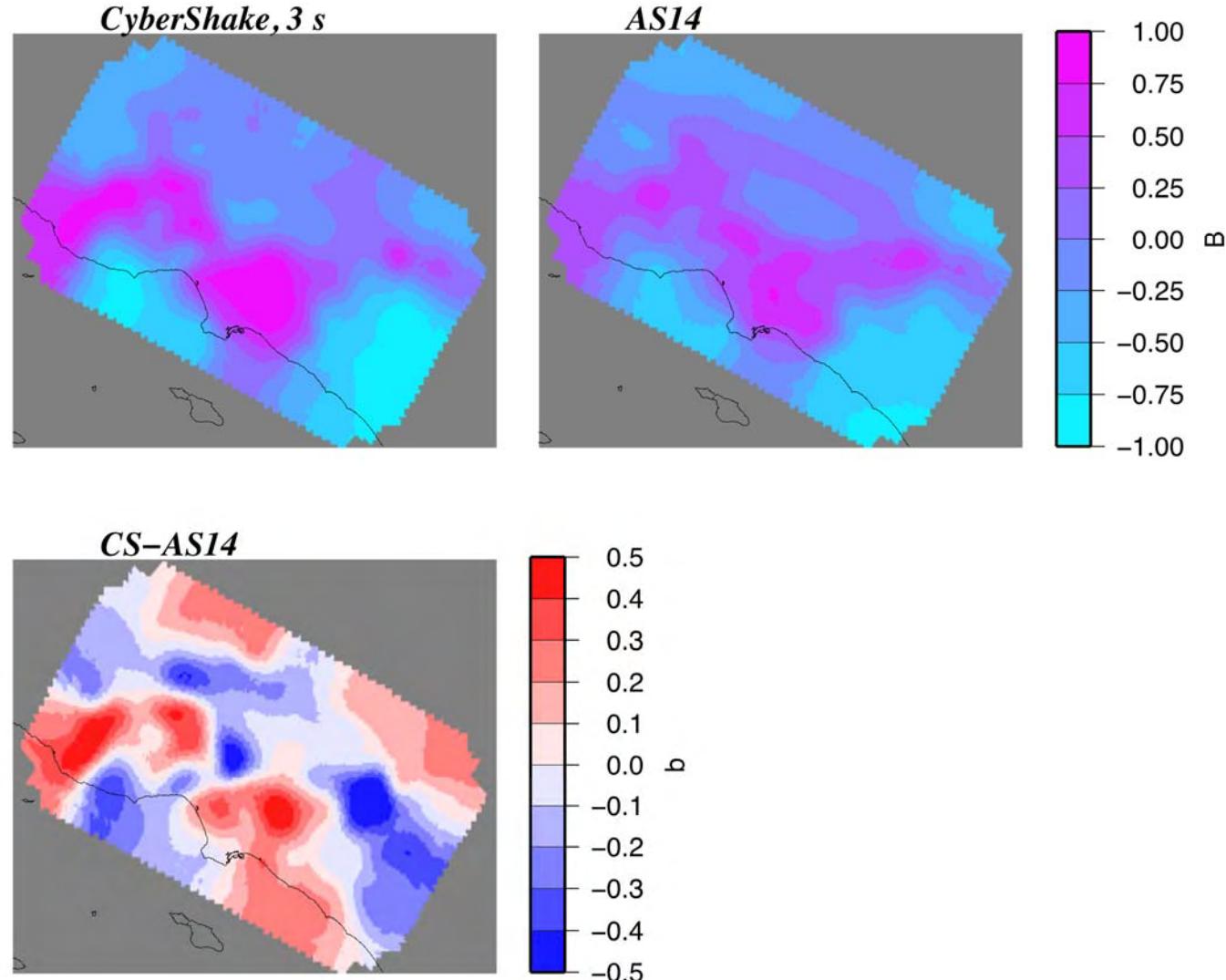
$$G(r, k, x, s) = A + B(r) + C(r, k) + D(r, k, x) \\ + E(r, k, x, s).$$



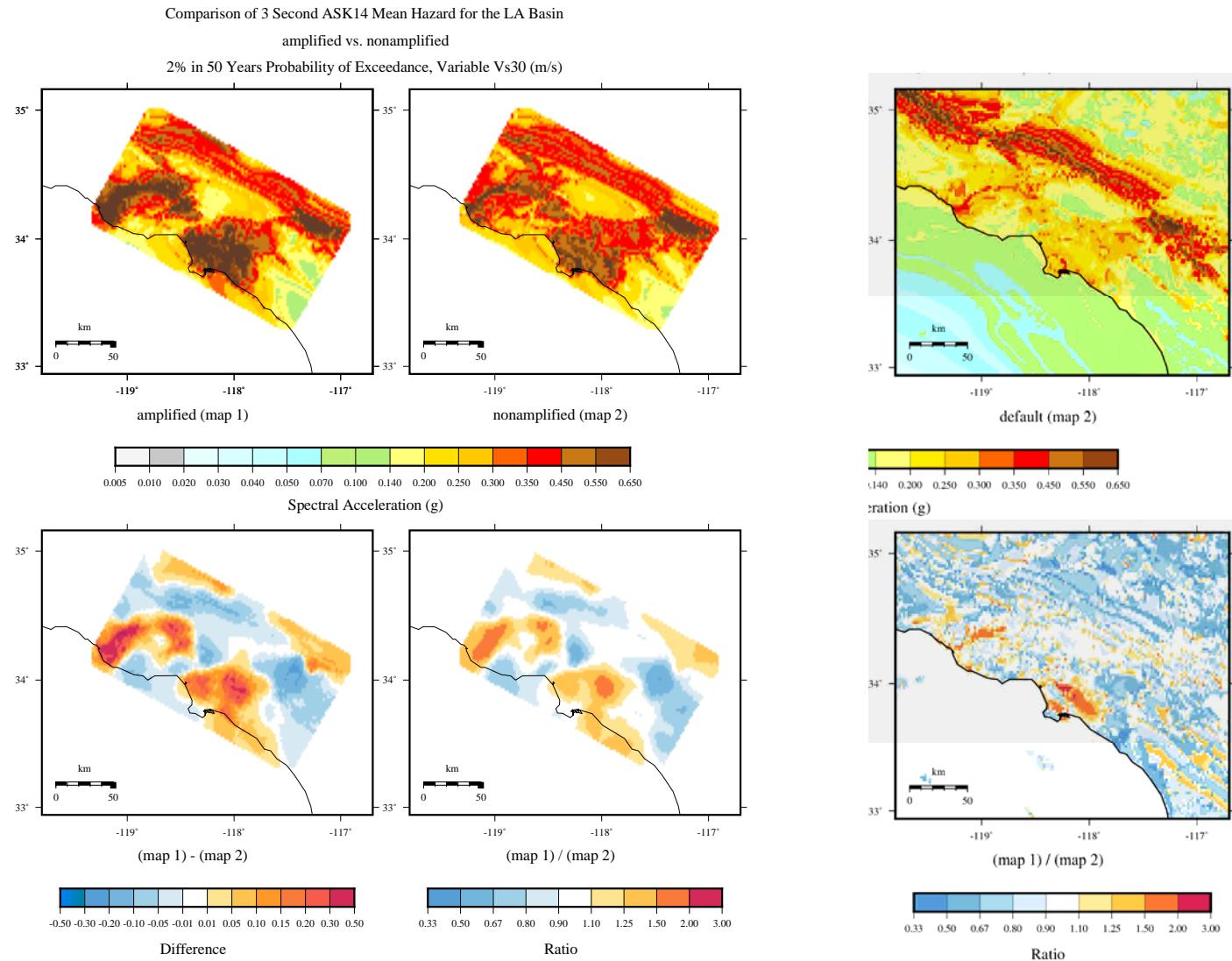
Successive averaging over sets of simulated ground motions permits parameterization of simulated ground motions into terms similar to GMPEs:

- E: Total excitation level; source complexity
- D: expectation over slip functions S; directivity effect
- C: Expectation over hypocenters X; path effect
- B: Expectation over seismic sources K; site effect
- A: Expectation over all sites R; regional excitation level

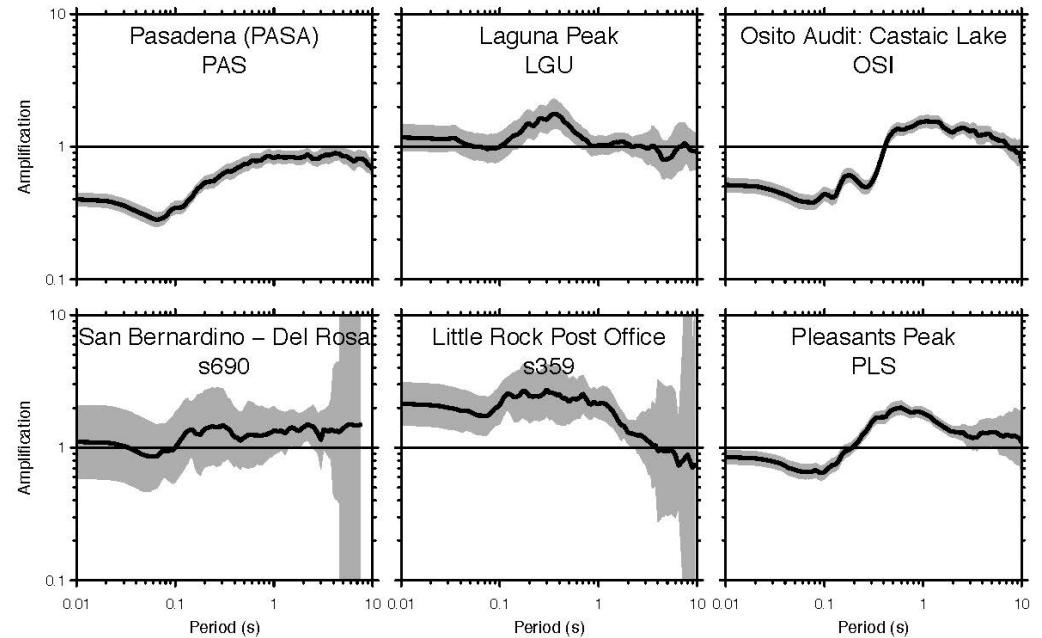
Basin amplifications, CyberShake, ABF



Hazard sensitivity tests, 3-s: Basin effects from 3-D simulations



Validation of 3-D-simulation-derived site amplification factors: LA (future SLC?)

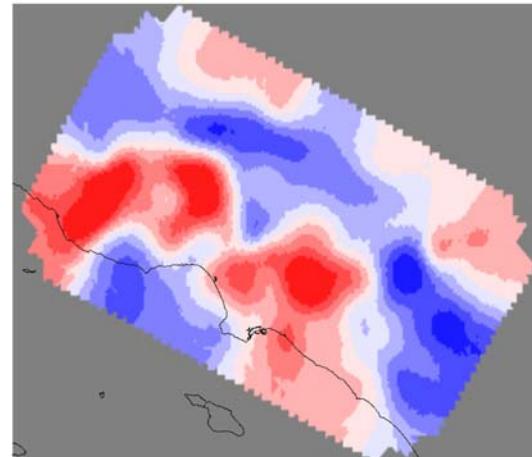
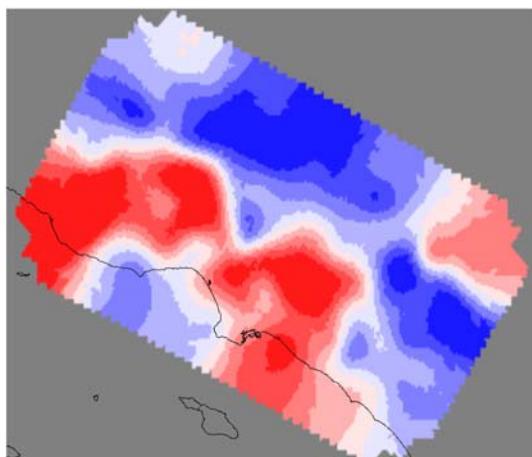
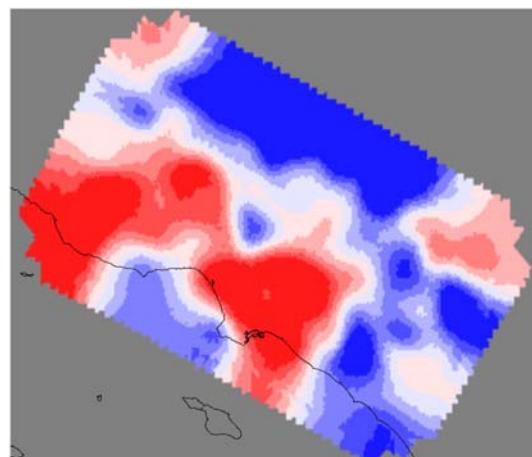
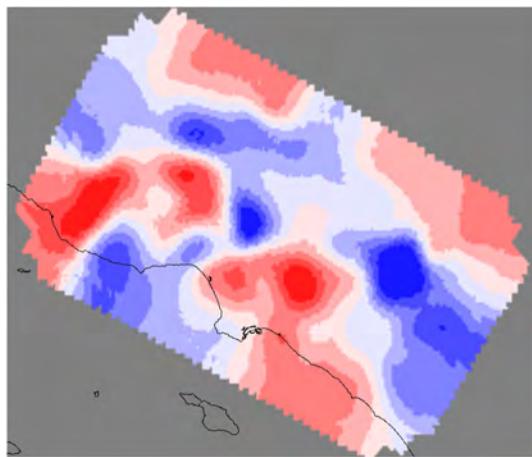


Moschetti et al. (2017, WCEE)

- Empirical amplification factors, Thompson and Wald (2016)
- Comparison of small-M ground motions with GMPE-predictions
- Use simulation-derived site response terms to assess whether empirical amplification factors improve

Basin amplifications, CyberShake, ABF

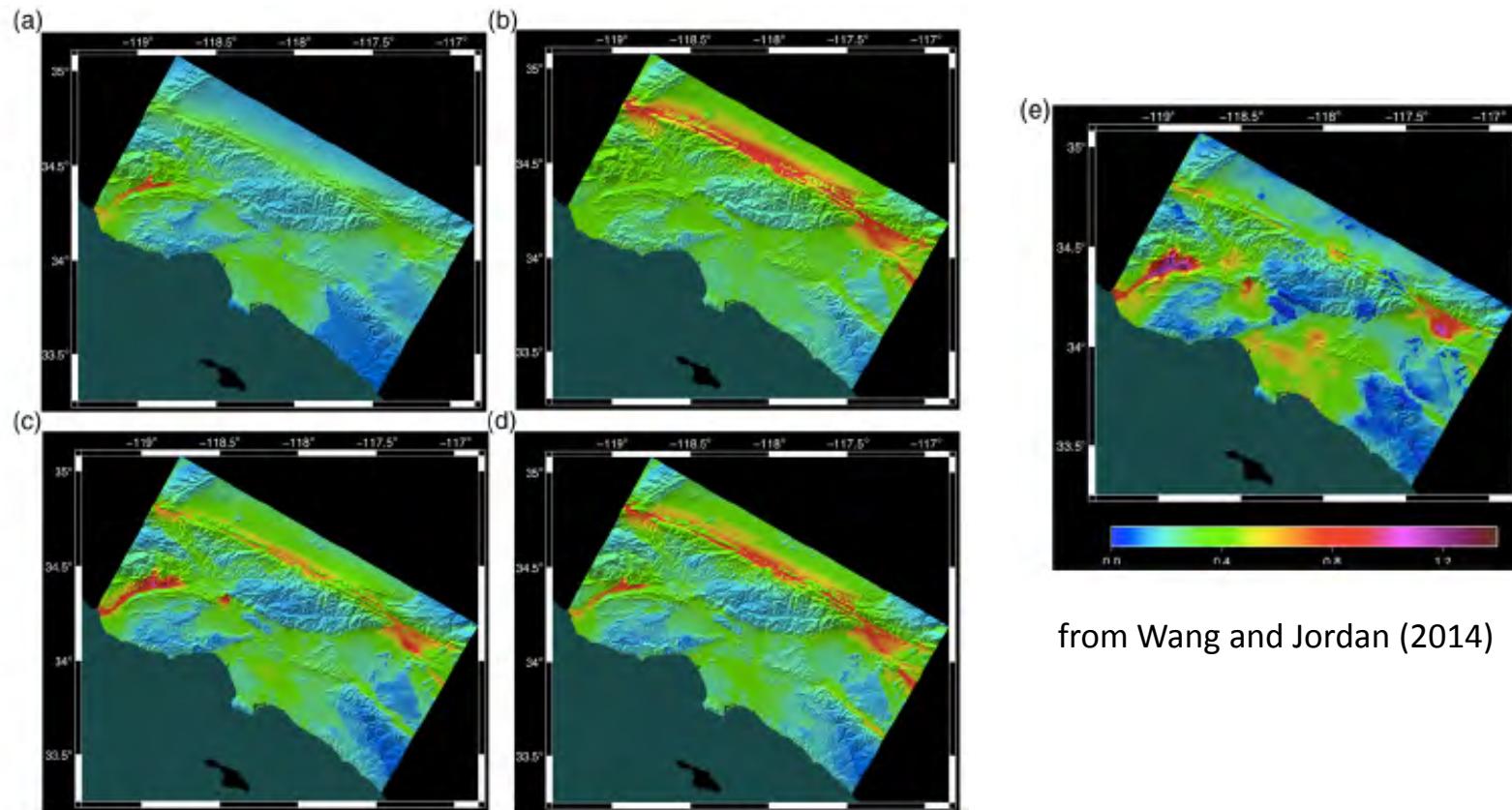
3-s SA



Plan for implementing ground motions from 3-D simulations into NSHM

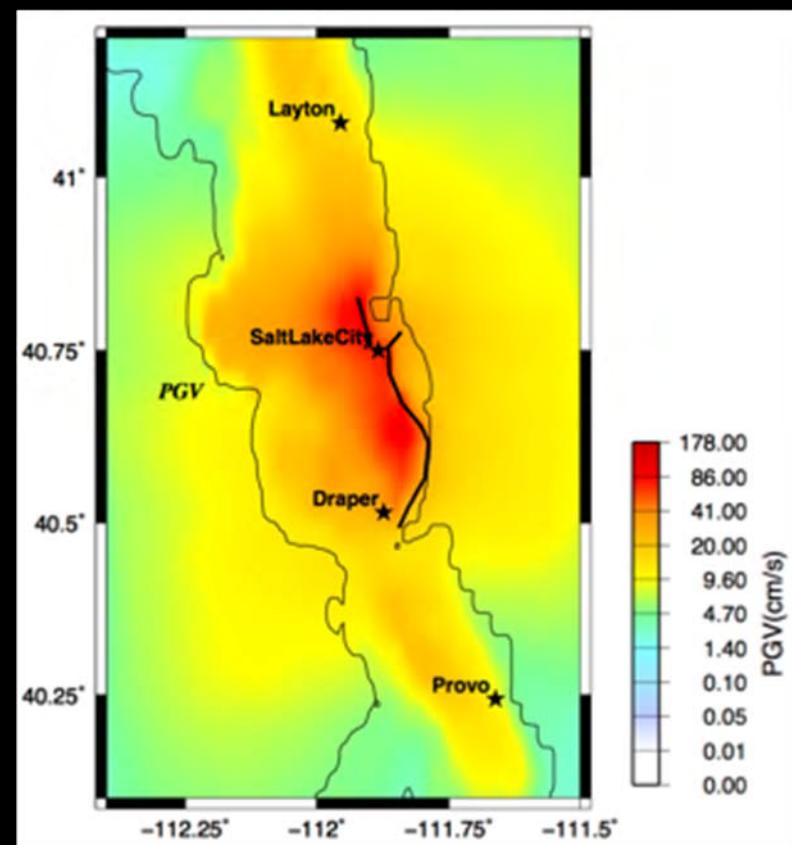
- Empirically based GMPEs, with basin amplifications from 3-D simulations
 - Implementation of basin amplification terms from CyberShake in nshm-haz code and sensitivity testing (Los Angeles)
 - Validation of 3-D-simulation-derived amplification factors—comparison with small-M earthquake data
 - Sensitivity testing for other regions and incorporation, 2020 NSHM
 - NSHM GMMs would presumably use weightings between simulated and empirically based GMPEs (period-dependent, similar to SCEC-UGMS recommendations?)
 - On-going simulation efforts in Seattle and Salt Lake City

Seismic hazard maps from 3-D simulations



from Wang and Jordan (2014)

3-D ground motion simulations of the Salt Lake City segment of the Wasatch fault zone: Scenarios and applications to seismic hazard



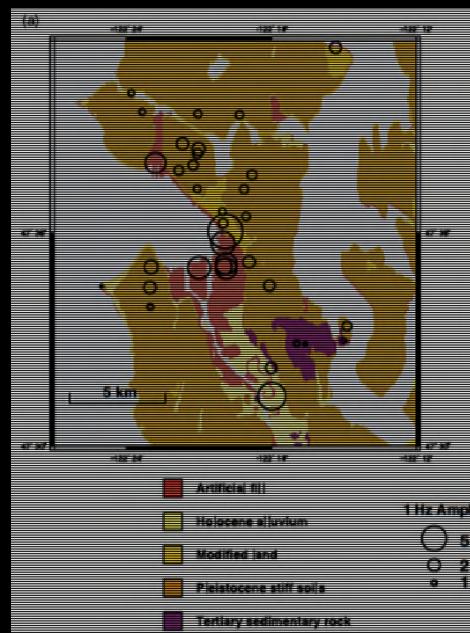
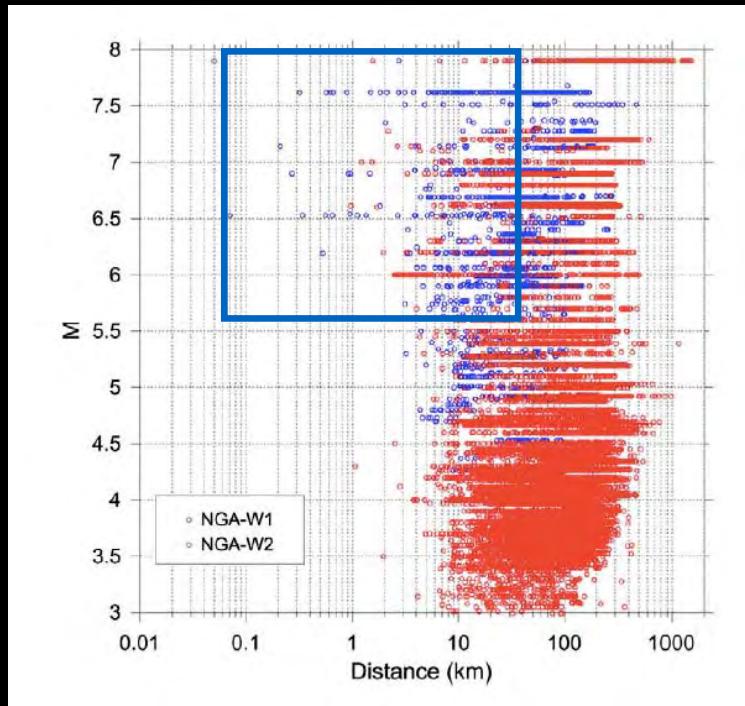
Morgan Moschetti

(Stephen Hartzell, Leonardo Ramirez-Guzman, Steve Angster, Arthur Frankel, Peter Powers, Eric Thompson)

Utah Geological Survey: Utah Ground Shaking Working Group
February 13, 2018
Salt Lake City, UT



Motivation for use of earthquake simulations



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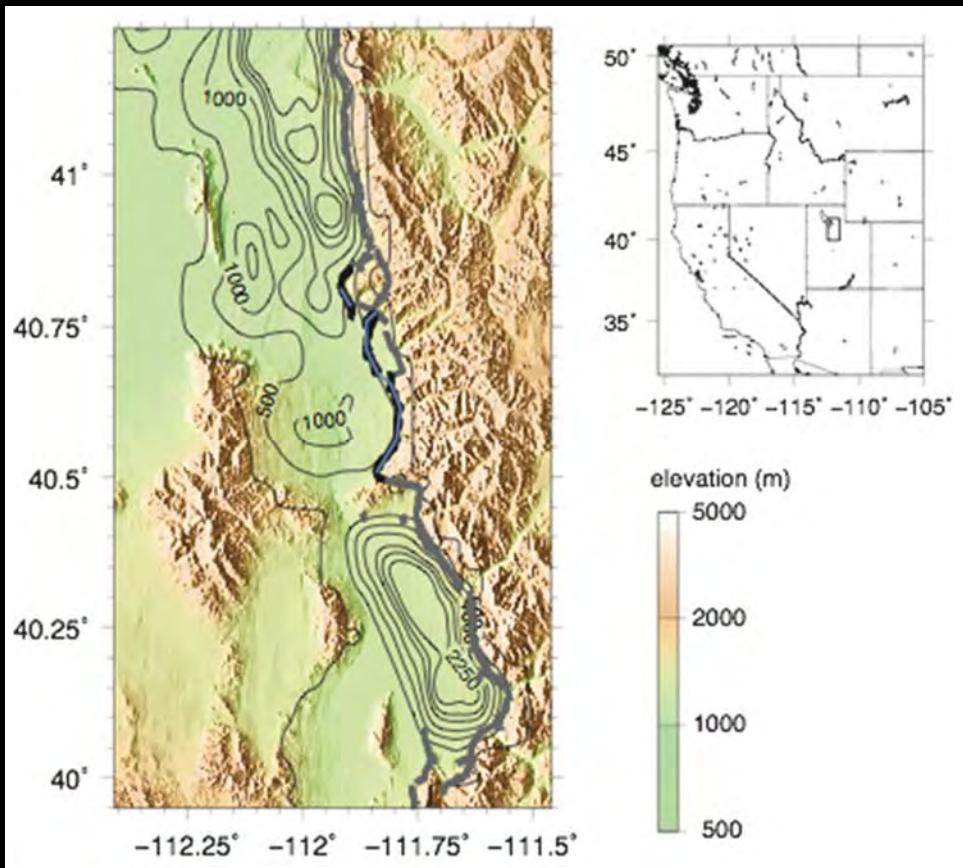
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- Z run#vxssruþj#surjuhvv# wrz dugv#Z dvdwfk#Eurqw#xuedq# vhlp lf#kd}dugþ dsv
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Outline

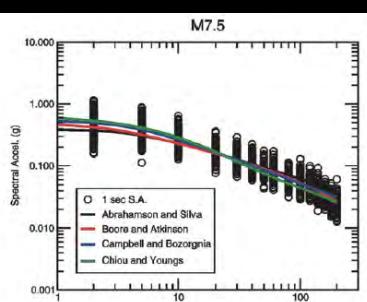
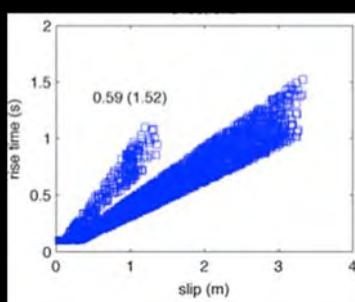
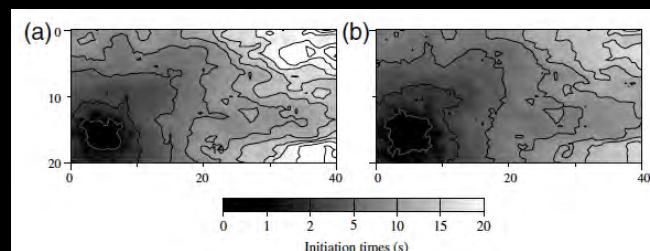
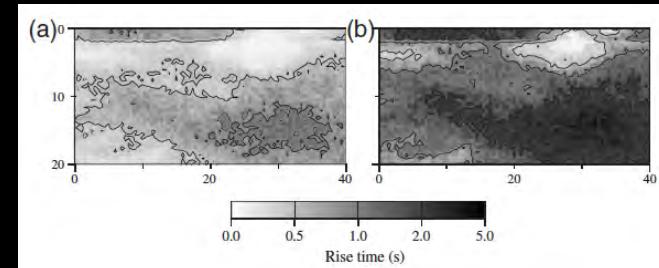
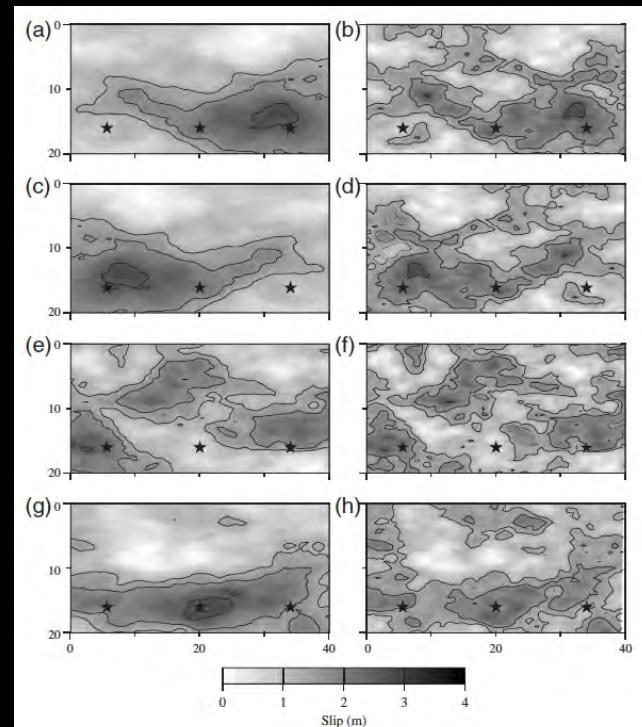
- 60G #vp xolwlrqv#rk#vh#Vdoh#Dnh#F w#vhjp hqw#Z dvdwfk#dxo# rqh# +P rvfkhw#hw#dd#34 : #EVVD ,
 - jurxqg#p rwlrq#sdwhuqv
 - jurxqg#p rwlrq#ydu#lqj#duktxdnh#uxswuh#sdwp hhuw
- Hihfw#rq#jurxqg#p rwlrq#r#ydu| lqj#duktxdnh#uxswuh#sdwp hhuw
- Ehwz hhq0 dqg#z lkq0hyhqw#hvlgxdo#urp #50G #vp xolwlrqv#r#frqvwudq#qsxw# uxswuh#sdwp hhuw

Salt Lake City segment, Wasatch Fault Zone



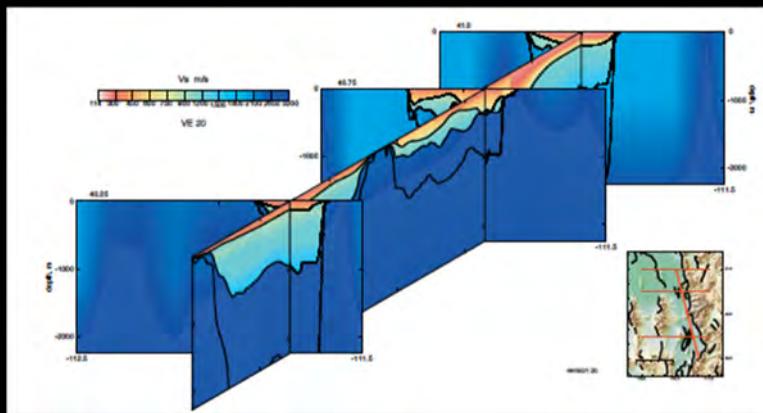
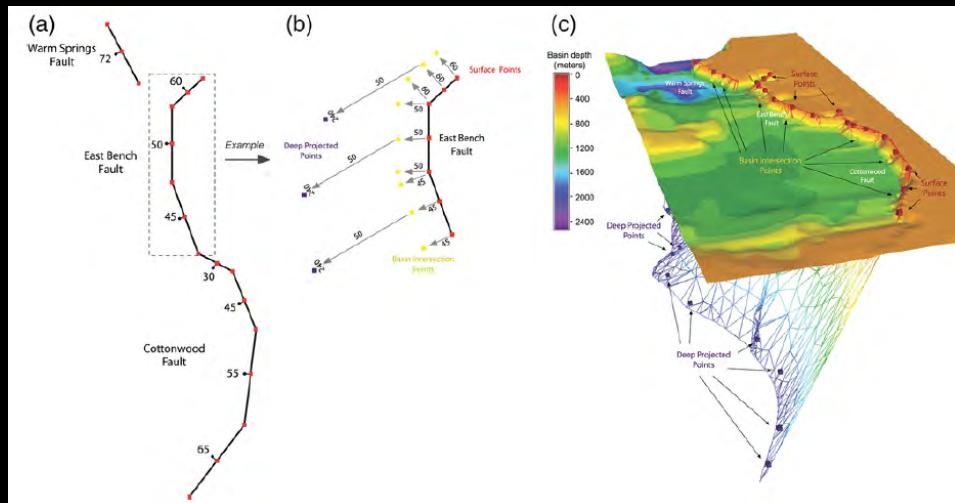
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- Hduktxdnh#xsxuh#vhjp hqw#z lk# kljkhvw#kd}dug#rq#B#fhqw#dvhjp hqw
- Vdo#Ddnh#F w#vhjp hqw#frqw#exwhv# A83 (#rk#kd}dug#5 (#SH#B3#hduv,

Earthquake rupture models



- Nbhph dwf#xswkuhp rghv
- <9#vhqdukv#irp #ydu|bj#B# uxswkuhsdudp hwhuv#dqgrp #hg# uhdd}dwraq#6 ,#ruhcolwraq#hbjwk# +5 ,#dyhudjh#xswkuh#shhg#5 ,# dyhudjh#vds#harf w#5 ,# k|srfhqwh#rfdwraq#6 ,
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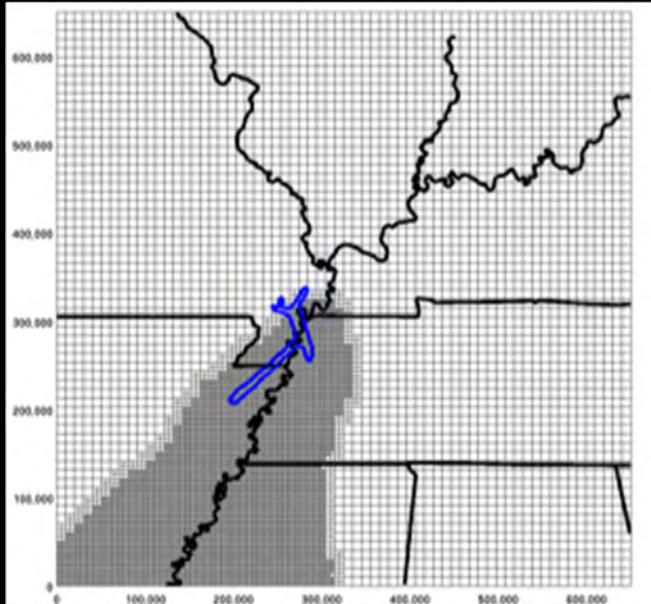
Fault representation and Seismic velocity model



- 6 OG #idxot#hsuhvhqwdwlrq#Dgkhuhv#W# jhrorj F#vwuhh#dgg#g ls#r#idxot#W# dgg#jhrsk |vFdd#revhuydwlrqv#
- Vhlp F#yhorflw|#p rghofurp #kh# Z dvdwfk#urqwf rp p xqlw|#Yhorflw|# P rghofurp dj lwdoh#ld#5338 ,# frqwuxfhg#v|p boud#W#rxwkhug#D# +VFHF ,#F YP

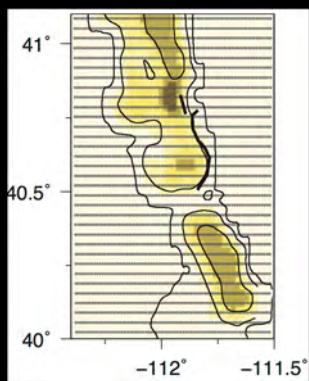
Urwhq#hw#ld#5344 ,

Wave propagation and simulations

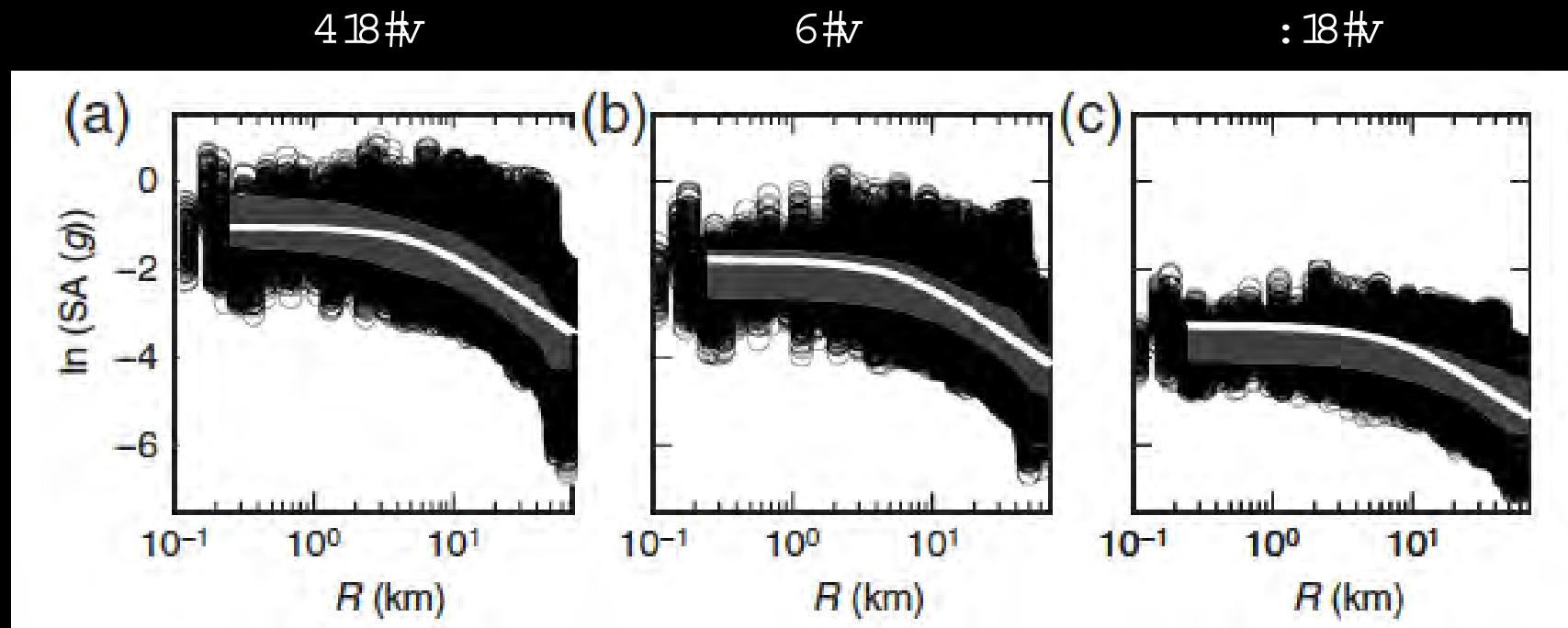


Upd 1h}W x}p dq#npl#5347,

- Khufxðnv#lb1hðhp hqw#rrdfkdlq/#F duqhj h#
P horq#Xqly#Wx#hwdd/#5339 ,
- Frgh#shuirup v#p hvkbqj #vroybj 1#P xo1hvraxwlrq#
vhlp F#harfM#Yvp b@533#p 2v ,
- ip d{@4#K }
- Vxuidfh#hfrogbj v#p#5933#v1hv#dfurvv#
v#p xo1wlrq#grp dbq#; 3#p #(493#p #(##; 3#p ,



Simulated ground motions

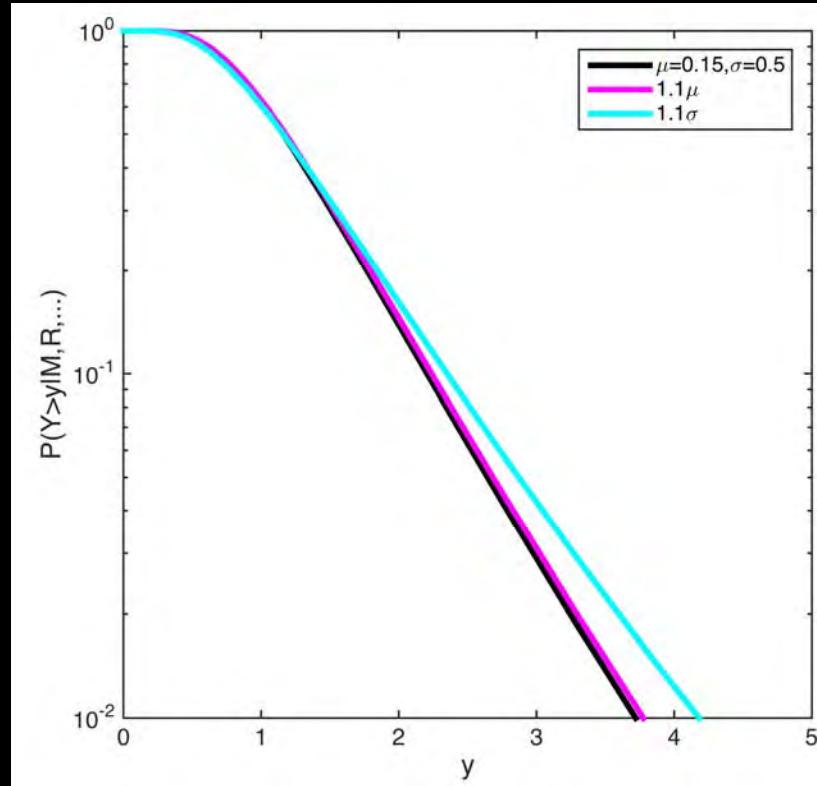


Ground motion simulations in PSHA

$$P(PGA > x | m, r) = 1 - \Phi\left(\frac{\ln x - \bar{\ln PGA}}{\sigma_{\ln PGA}}\right)$$

$$\lambda(IM > x) = \sum_{i=1}^{n_{sources}} \lambda(M_i > m_{min}) \int_{m_{min}}^{m_{max}} \int_0^{r_{max}} P(IM > x | m, r) f_{M_i}(m) f_{R_i}(r) dr dm$$

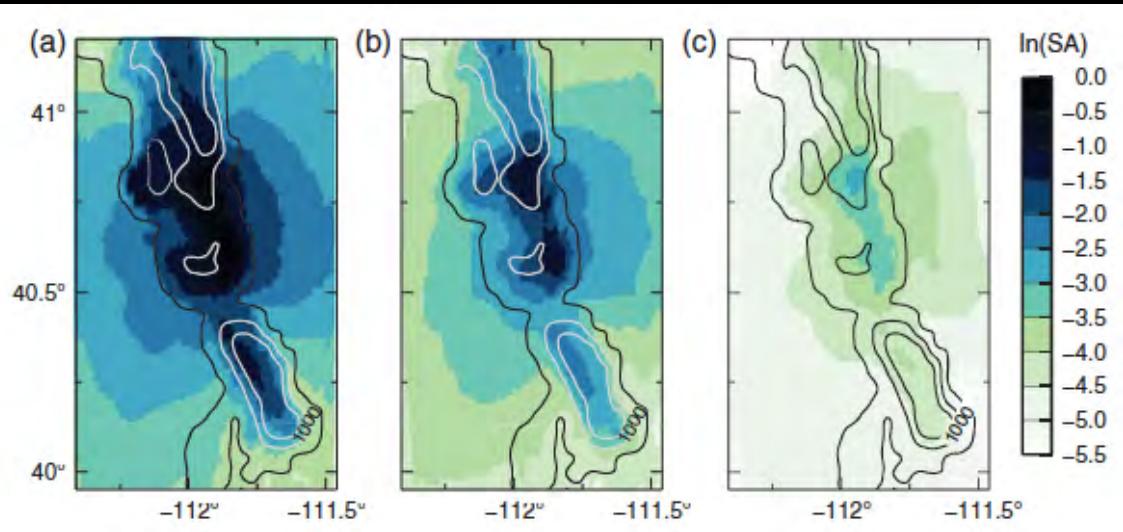
Baker (2008), An Introduction to PSHA



418#v

6#v

:18#v

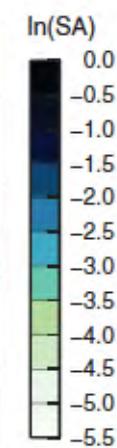
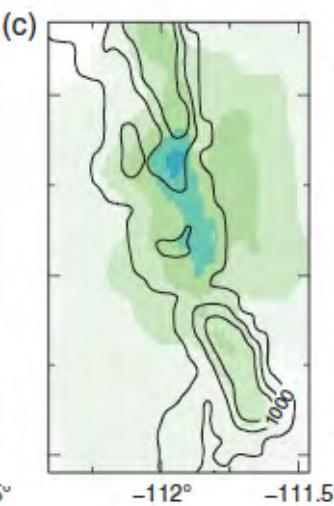
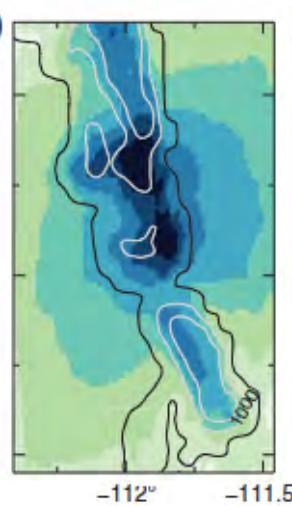
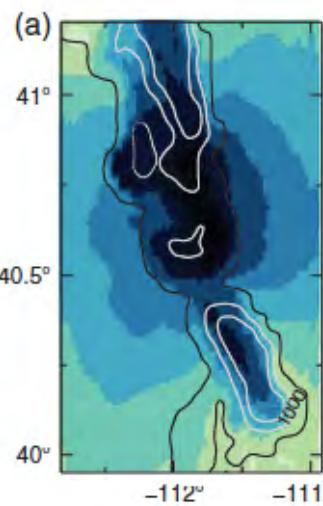


Vsdwddg#lwlelxwlrq#p hdq/#
vp xolwg#jurxqg#p rwlrqv

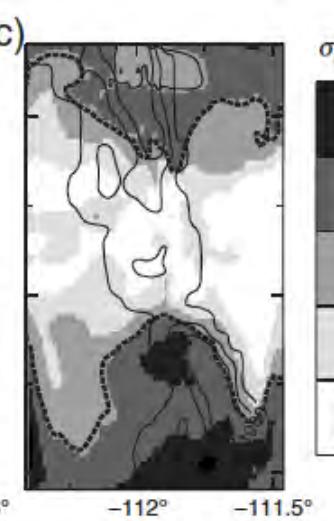
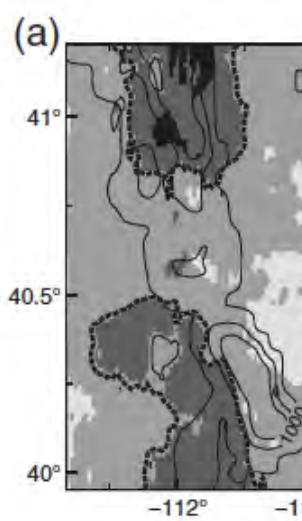
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6#v

:18#v

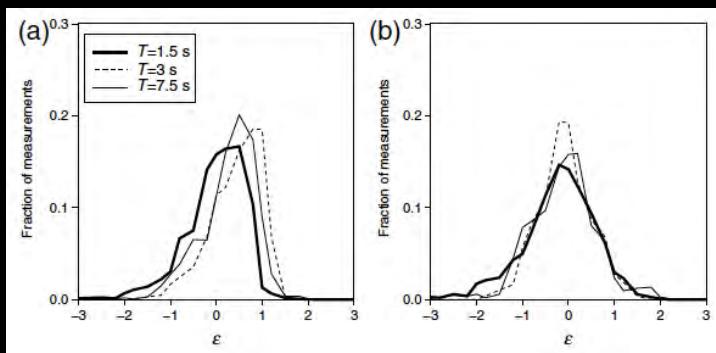


Vsdwddg#lwlelxwlrq##p hdq/#
vp xolwg##jurxqg##p rwlrqv

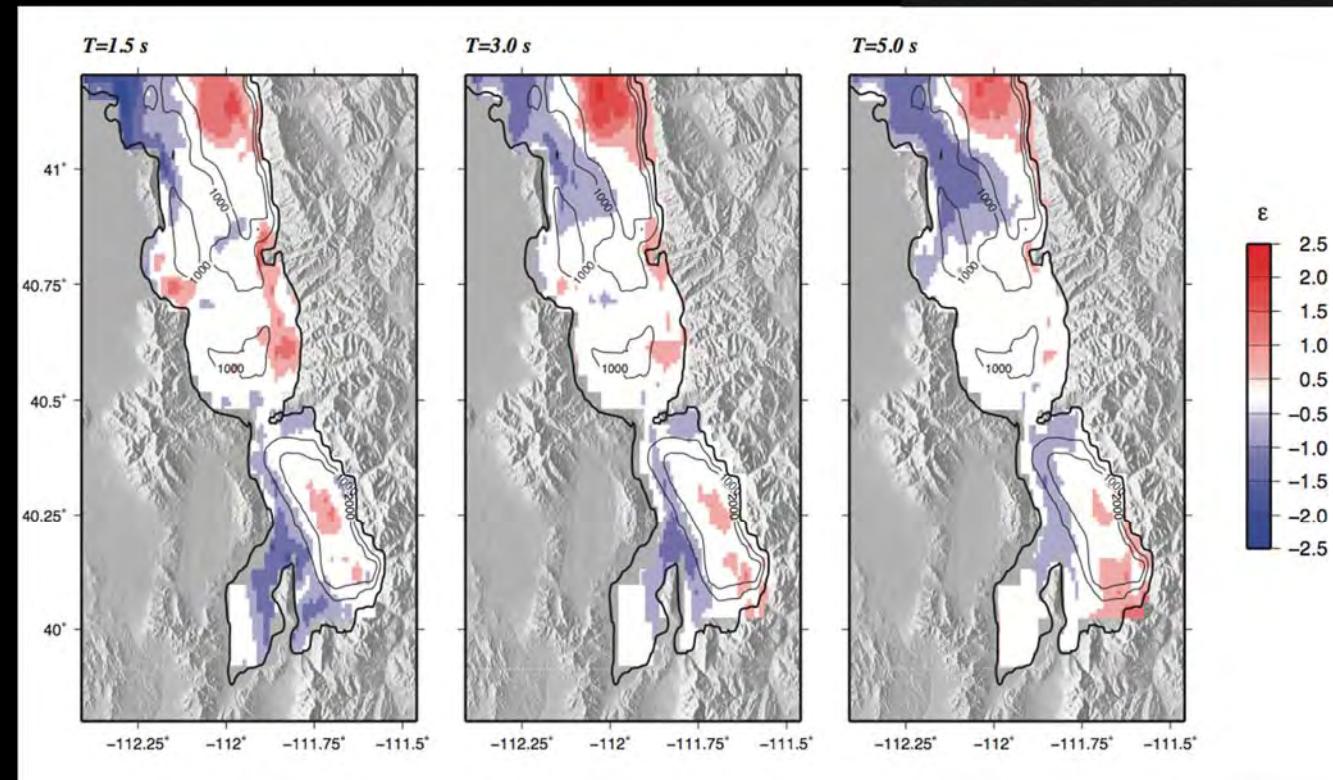


Vdqgdug##hybwlrq##orj ,#
vp xolwg##jurxqg##p rwlrqv#
dw##dfk##v###

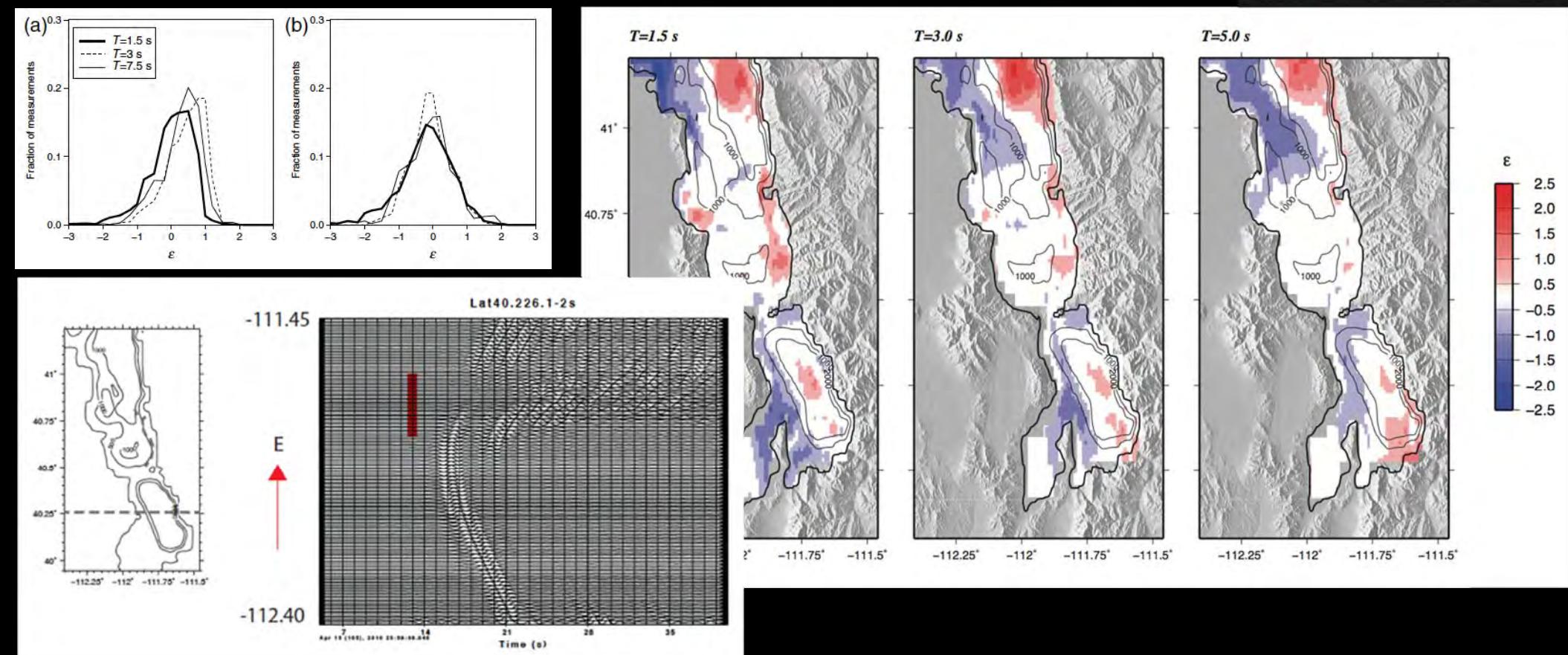
Ground motion residuals (total)



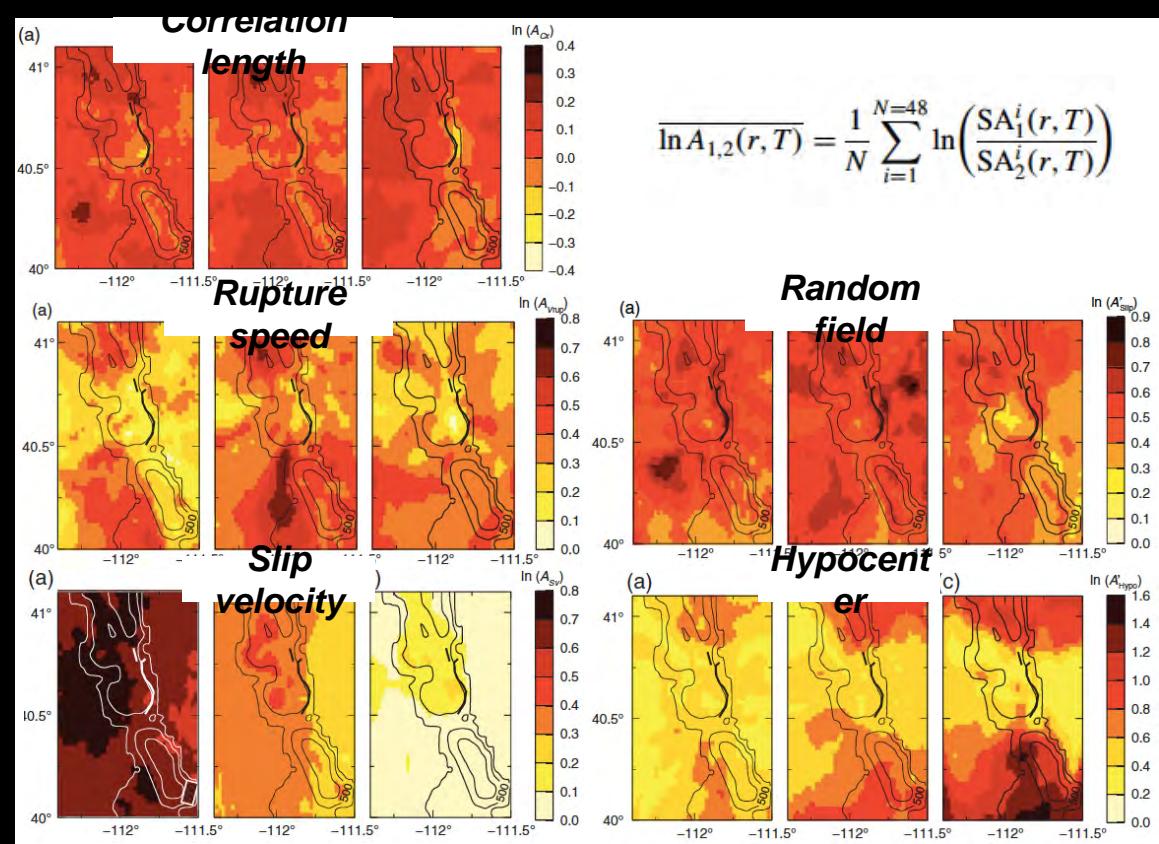
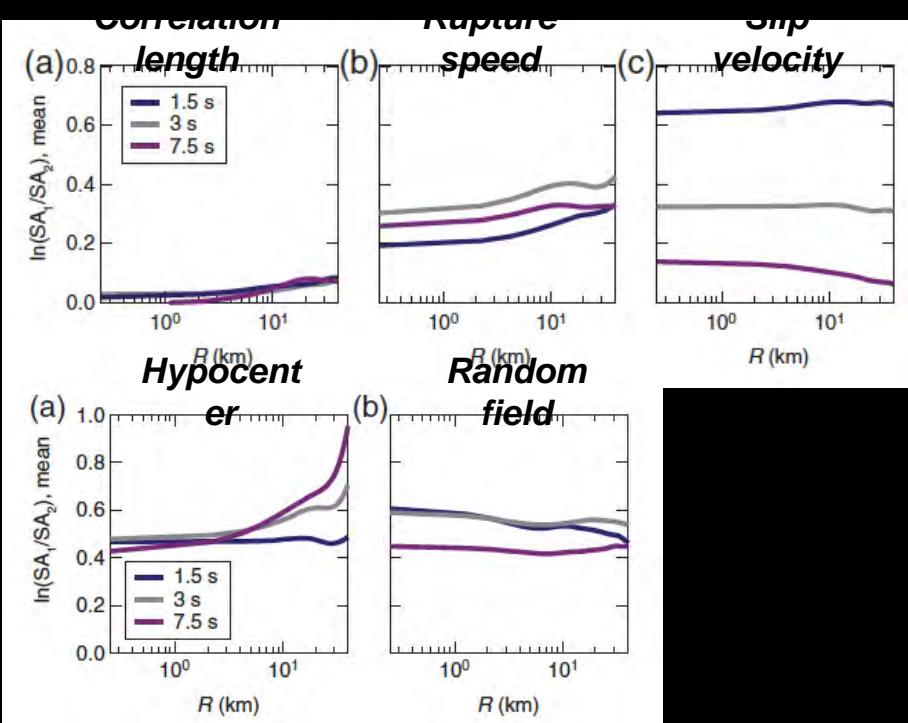
$$\varepsilon = \frac{\ln SA - \mu_{GMPE}}{\sigma_{GMPE}}$$



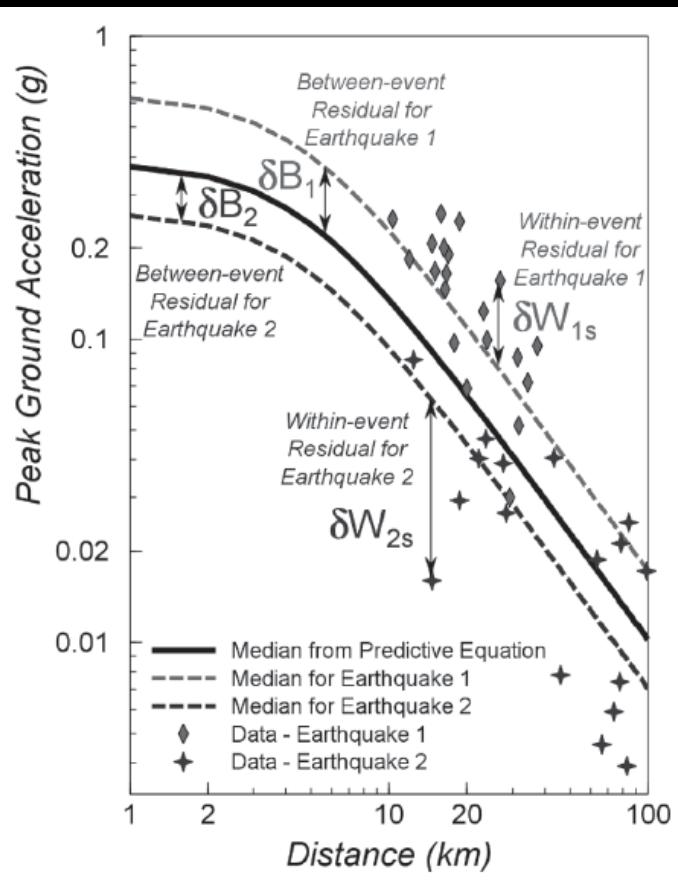
Ground motion residuals (total)



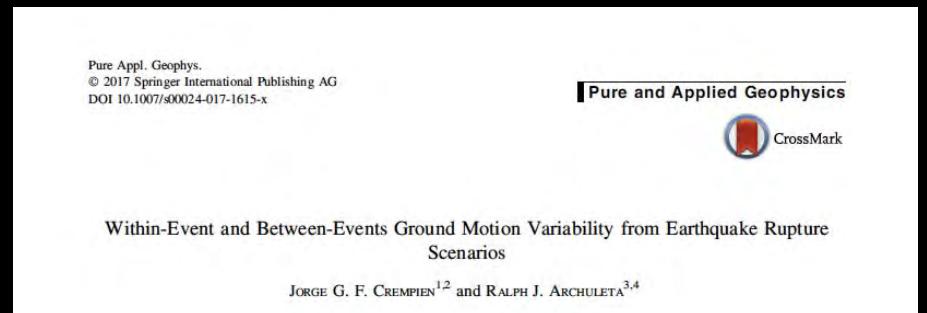
Ground motion amplifications from variations in rupture parameters



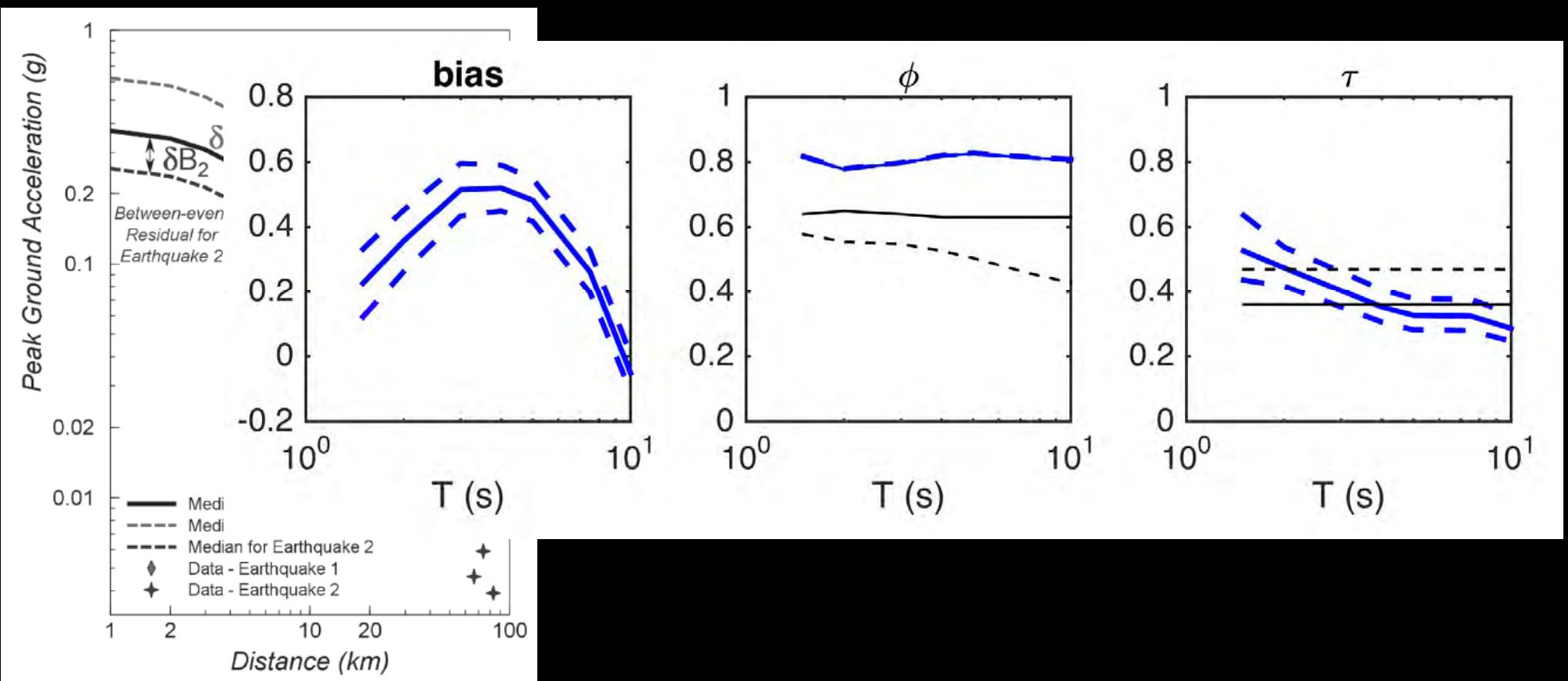
Comparison of simulated ground motions with empirically based GMPEs



DOI: <https://doi.org/10.1007/s00024-017-1615-x>

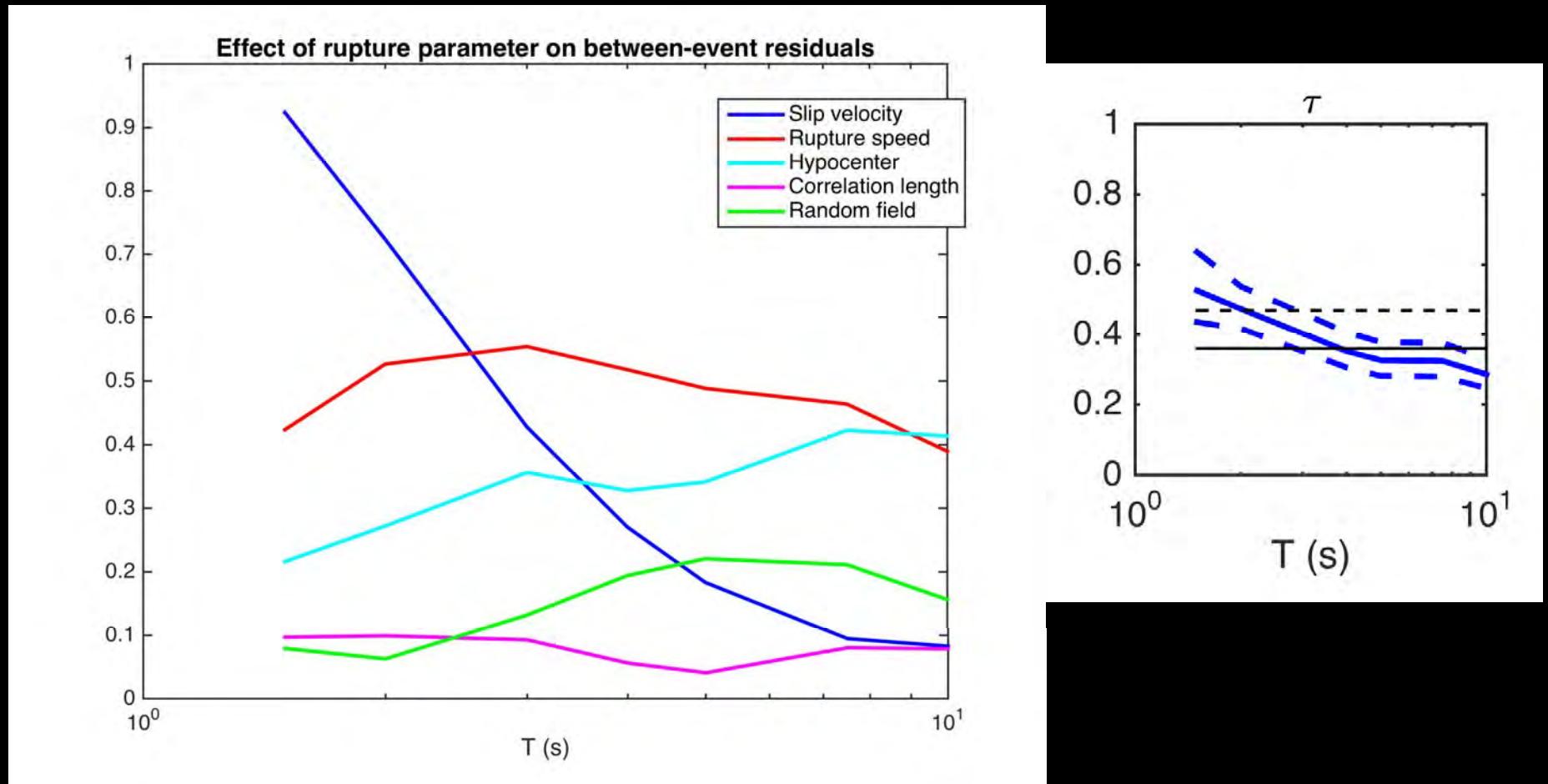


Comparison of simulated ground motions with empirically based GMPEs



DOI: 10.1186/1534-6042-2013-100

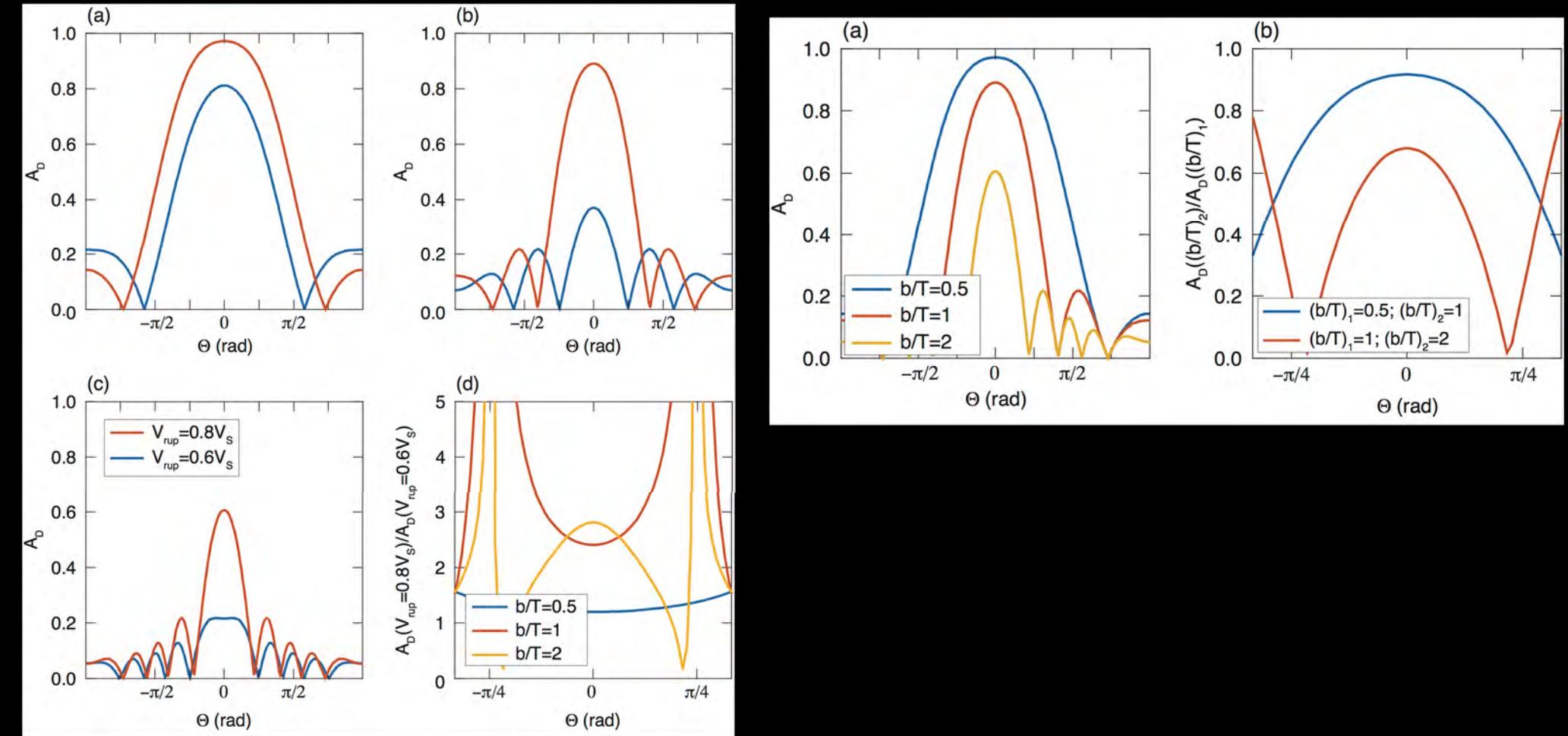
Comparison of simulated ground motions with empirically based GMPEs



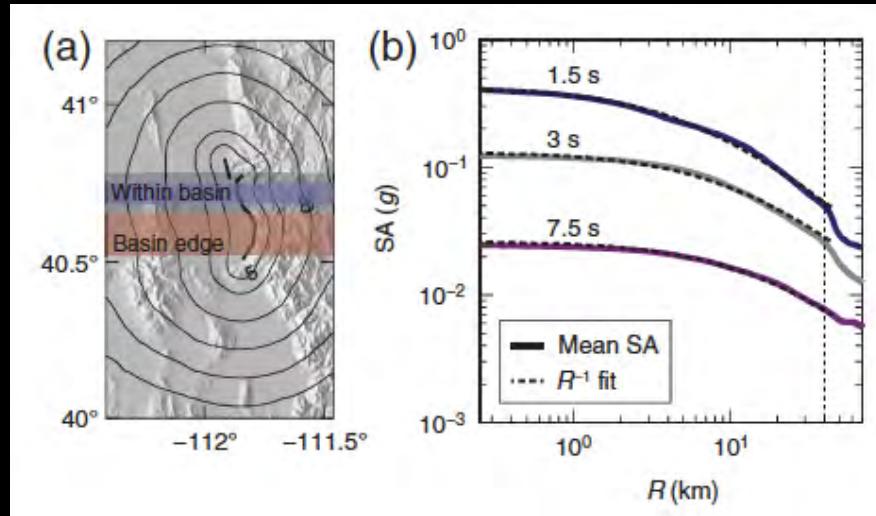
Conclusions and future directions

- 6 OG #j urxqg#p rwlrq#v#p xolwlrqv#lq#Z dwdwfk#lurqwh{klewkljkhut#kdq#J P SHOsuhg Ifhg#j urxqg#p rwlrqv#z lkq#ghs#hg#p hqwdul#edvlgv
 - Ohqd#gxh#r#edvlg0j hqhudwhg2dp sdihg#xuidfh#z dyhv#qrw#qfoghg#q#p sulfd#J P SHv,
- Vwurqj #olhudqydu#dudwlrqv#lq#j urxqg#p rwlrq#ydu#elw#hdg#bj#r#kjhkhut#kdq#J P SHOsuhg Ifhg#suredebw#j urxqg#p rwlrqv#p#kh#hggv#r#kh#idxo
- Ydudwlrqv#lq#j urxqg#p rwlrq#z lk#g lwdqfh#dqg#vsdwdd#rfdwlrq#gxh#r#ydu#dudwlrqv#lq#xsxuh#sdudp hhwu,, nqrz bj#kh#dqjh#dqg#rydudqfhv#r#sdudp hhwu#v#p srudqw#ru#kh#kvh#q#hlp If#kd}dug#dqddvhv
- Xvh#r#kh#g lwdexwlrq#r#j urxqg#p rwlrqv#htx1hv#yddg#dudwlrq#r#p hdq#dqg#wdqgdug#ghy#dudwlrqv
 - R qh#p hukrg#ru#frqvwdbqbj#j urxqg#p rwlrq#ydu#elw#p d|h#kurxjk#frp sdudrq#z lk#hp sulfd#edvhg#p rghov#r#hwz hhqchyhqwydu#elw#

Rupture directivity, Ben-Menahem (1961, 1962)



Hduktxdnh#xswuh# rghov#



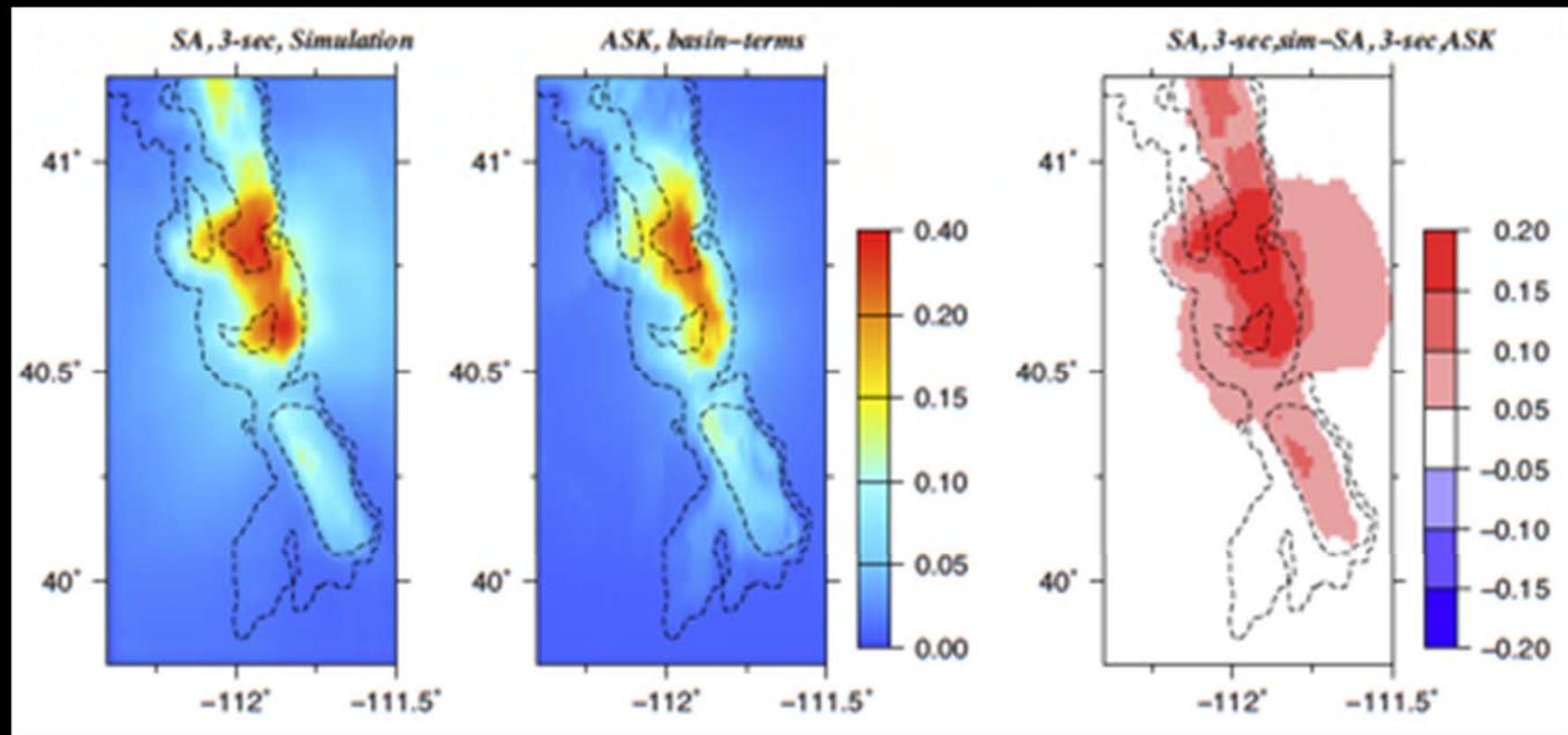
T (s)	SA_0 (g)	R_c (km)	R^2 , All Data
1.5	0.43	5.7	0.47
3	0.13	11.0	0.41
7.5	0.03	16.4	0.39

$$SA_{\text{Sim}}(T, R) = \frac{SA_0(T)}{1 + (\frac{R}{R_c(T)})}$$

- Vip s̄k̄#dqdqwfed̄irup #irup hdq#jurxqg# p rw̄rqv
- G hshqghqw#rq#hihihqf h#farvh0q,# jurxqg#p rw̄rq#hyhdqg#fruqhut#lwdqf h
- Irufqfuhdvbjj#shulrg#lbqg#ghfuhdvbjj # dhyhdqg#qfuhdvbjj#fruqhut#lwdqf h



Probabilistic ground motions, 2% PE 50 years



3D Dynamic Rupture Simulations along the Wasatch Fault

Kyle Withers¹

Utah Ground Shaking Working Group

Morgan Moschetti¹ and Kenneth Duru²

¹Geologic Hazard Science Center, USGS, Golden, CO

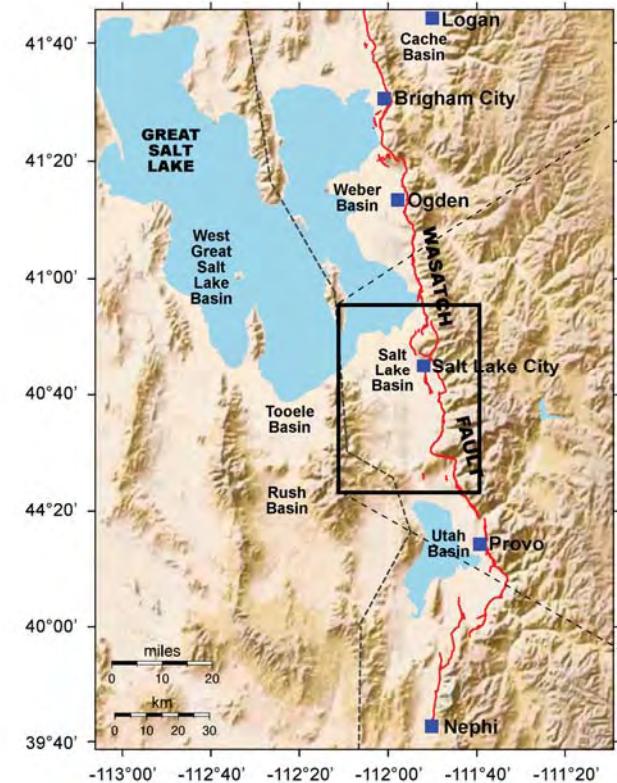
²Department of Earth and Environmental Sciences, LMU Munich

Outline

- Objectives and Motivation: extend ground motion to frequencies of interest to engineers along normal faults, specifically the Salt Lake City segment of the Wasatch Fault
- Limitations of kinematic techniques
- Approach: fully physics-based spontaneous earthquake ruptures
- Simulations: initial conditions and example ruptures
- Results: rupture and ground motion analysis
- Conclusions and future work

Objectives

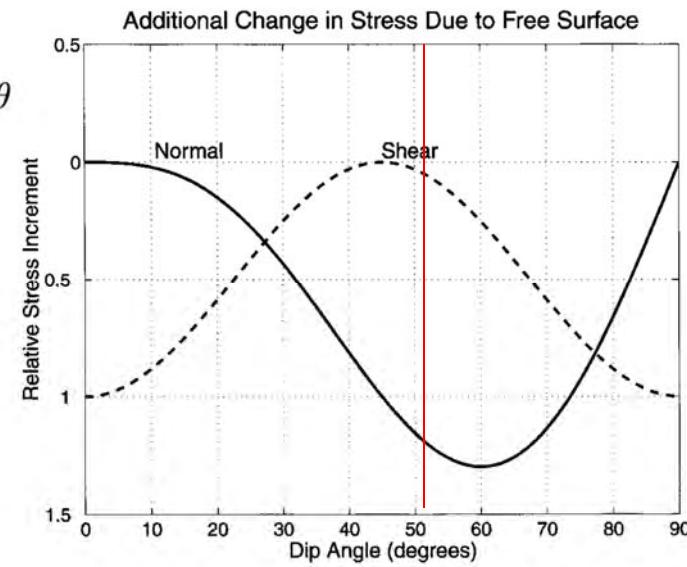
- Better constrain seismic hazard in bandwidth important for engineers (0.1 -10 Hz), particularly in data lacking regions along dip-slip faults
- Determine influence of fault geometry and topography on both rupture and ground-motion amplification
- Develop database of ruptures for Salt Lake City segment of Wasatch Fault, Utah



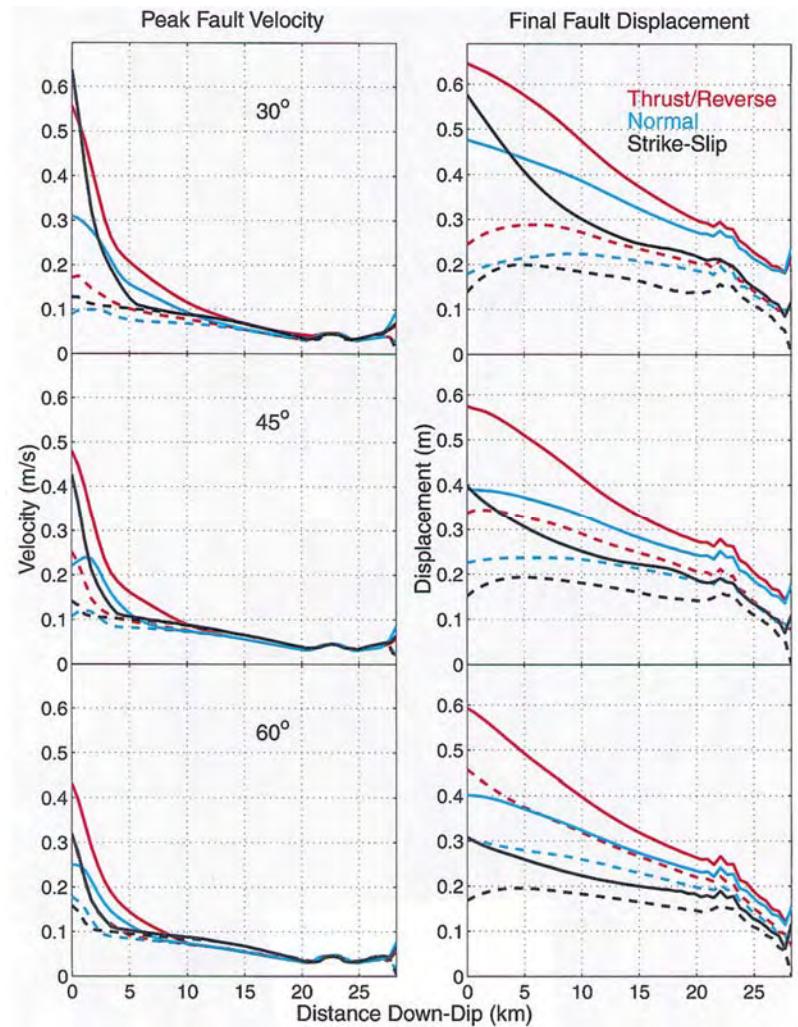
Limitations of Kinematic Simulations

- Asymmetric geometry of dip-slip faults can have large effects on the dynamics of earthquake rupture, leading to larger motion on the FW than the HW.

$$\Delta\tau = -\tau \cos^2 2\theta$$
$$\Delta\sigma_n = -4\tau \sin^3 \theta \cos \theta$$

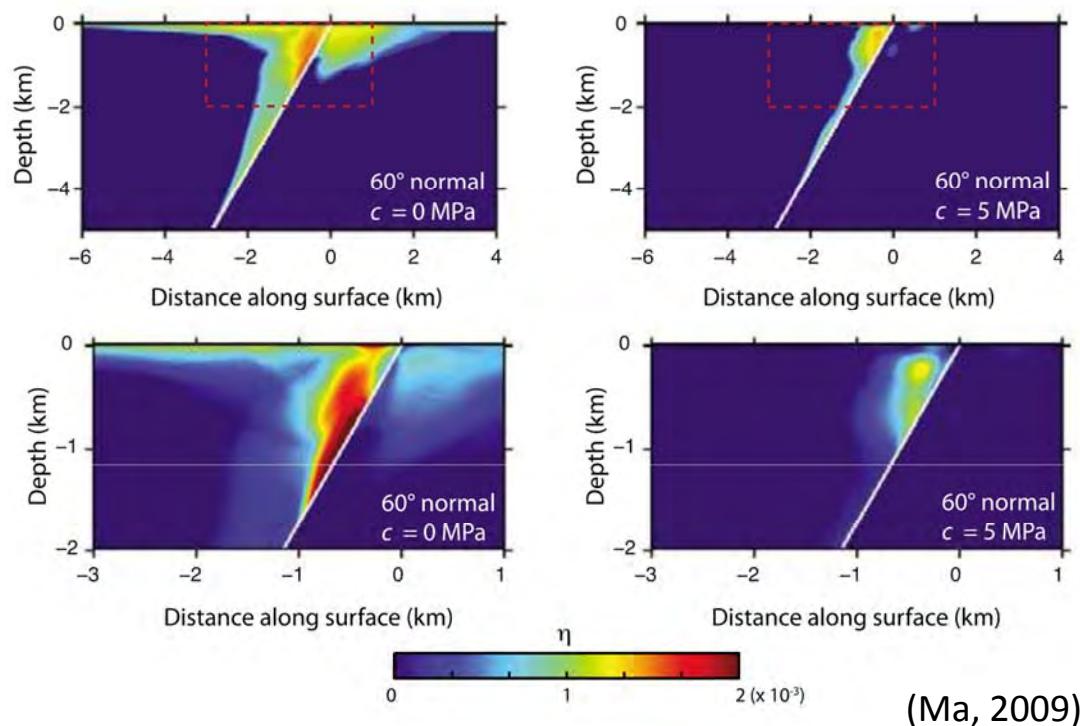


Oglesby et. al., 2000



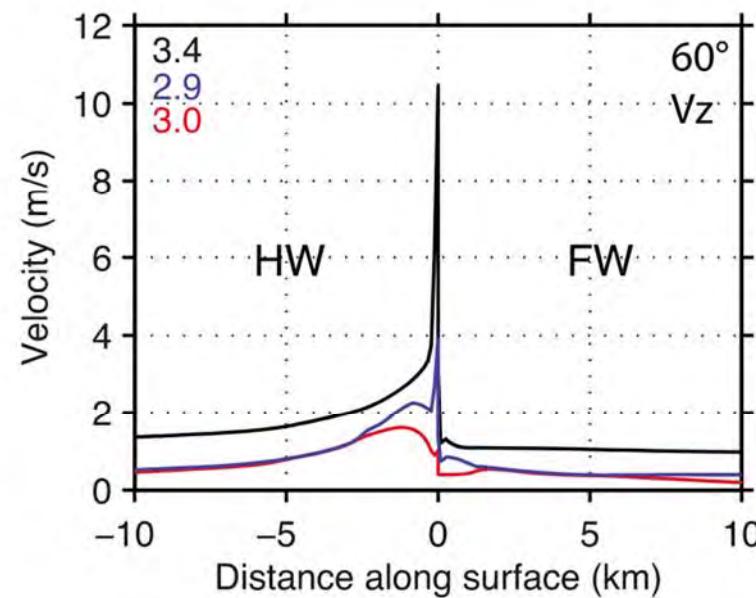
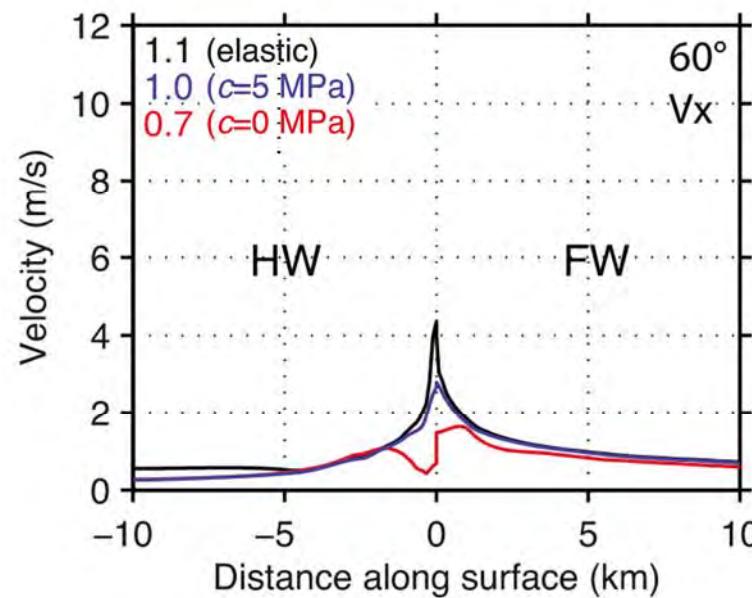
Asymmetry in rupture-induced inelastic strain across dipping faults

- Inelastic strain is larger and broader in the HW compared to the FW, leading to reduced asymmetry in ground motion across the HW and FW (compared to elastic solutions)



Asymmetry in rupture-induced inelastic strain across dipping faults

- Inelastic strain is larger and broader in the HW compared to the FW, leading to reduced asymmetry in ground motion across the HW and FW (compared to elastic solutions)

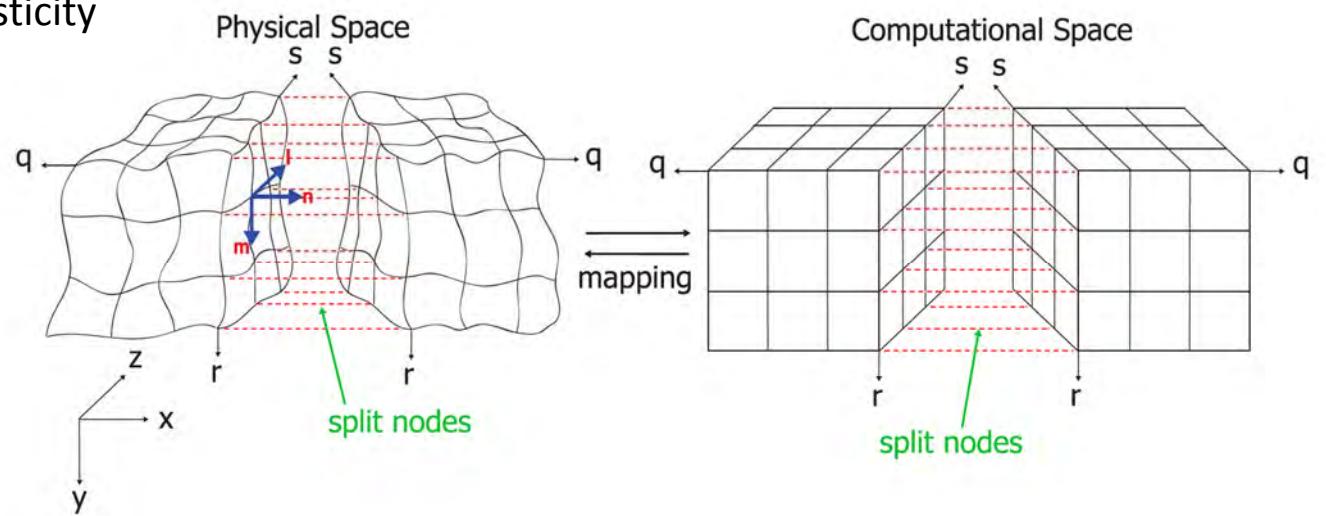


(Ma, 2009)

Waveqlab3D (Finite Difference Quake and Wave Laboratory)

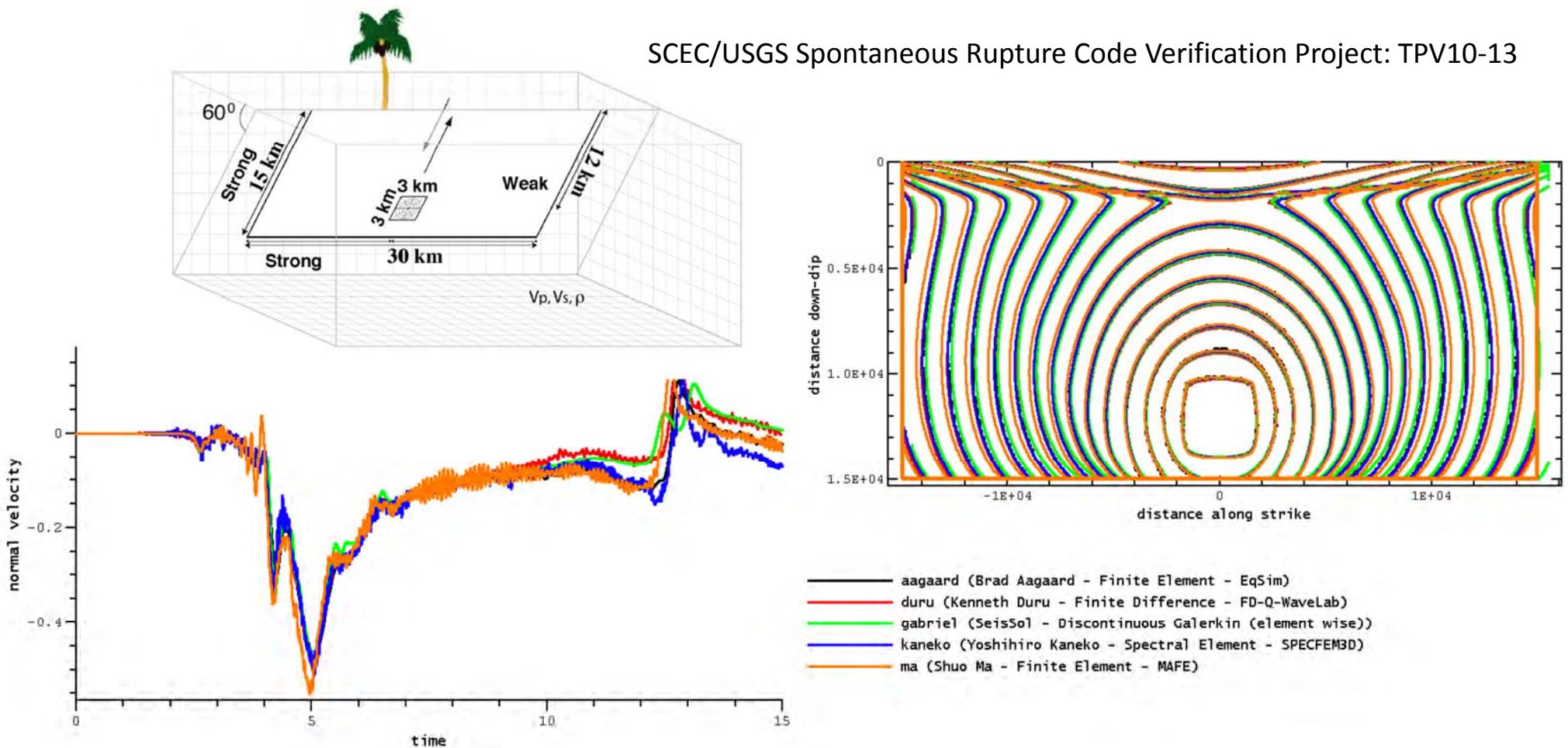
- Finite difference summation-by-parts dynamic rupture (and wave-propagation) code can handle

- complex fault geometry (both short and long-wavelength variations)
- nonlinearity, i.e. off-fault plasticity
- 3D media heterogeneity
- anelastic attenuation, $Q(f)$
- free-surface topography

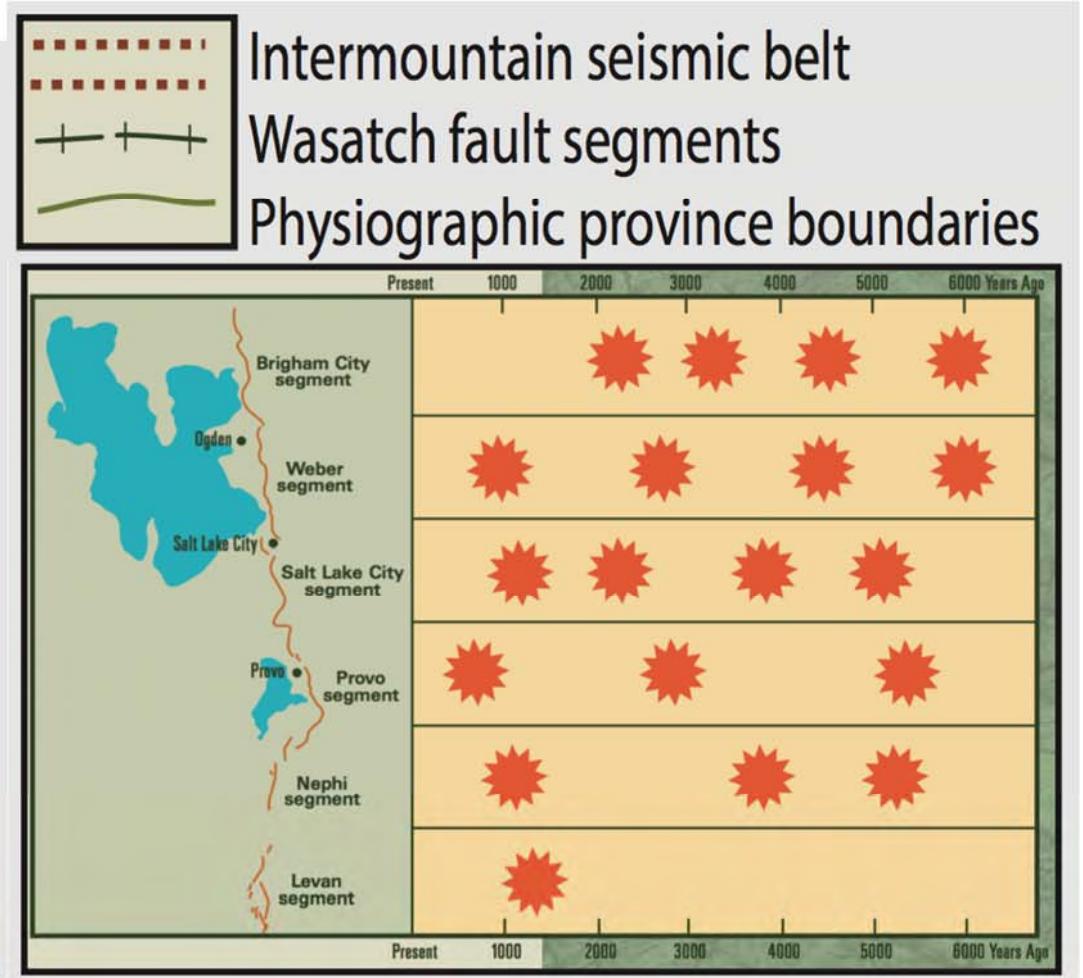
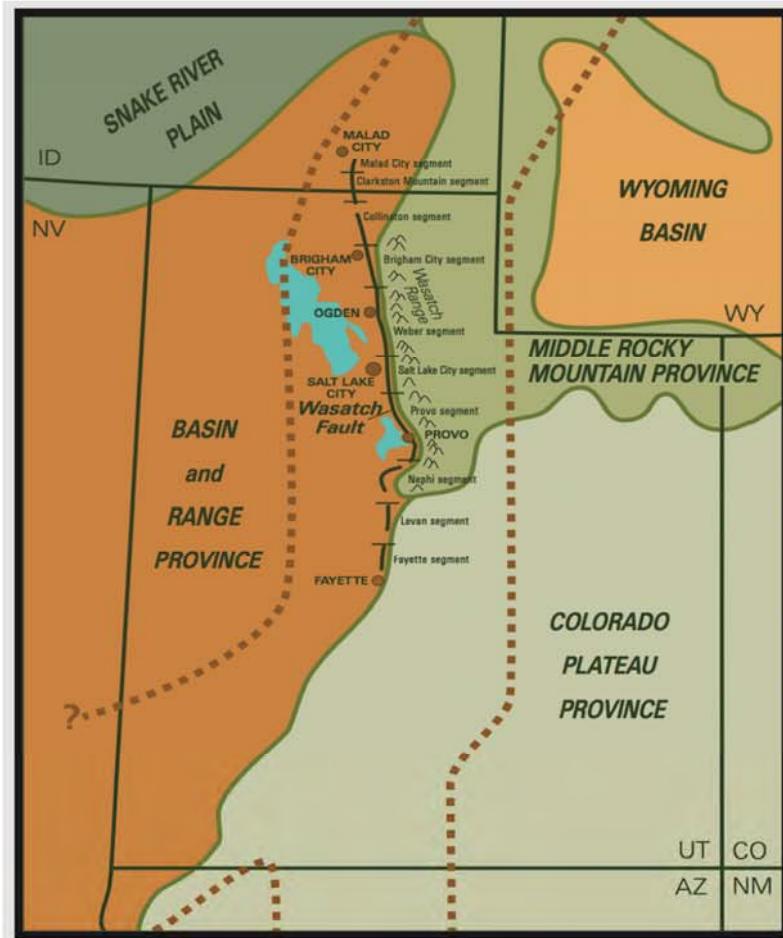


Duru and Dunham, 2016

Dynamic Rupture Validation along a Dipping Fault

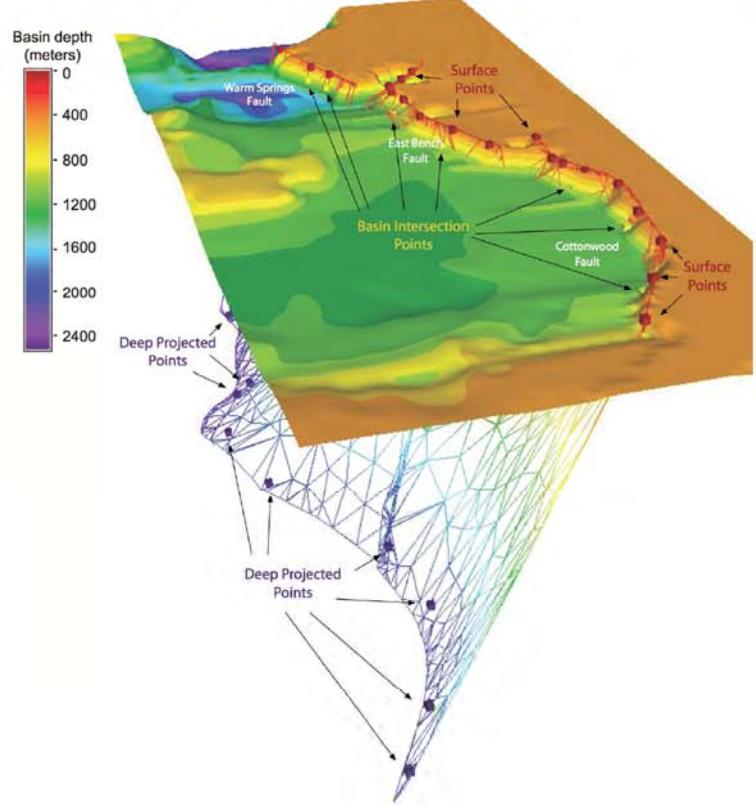


Study Area: Wasatch Fault Zone

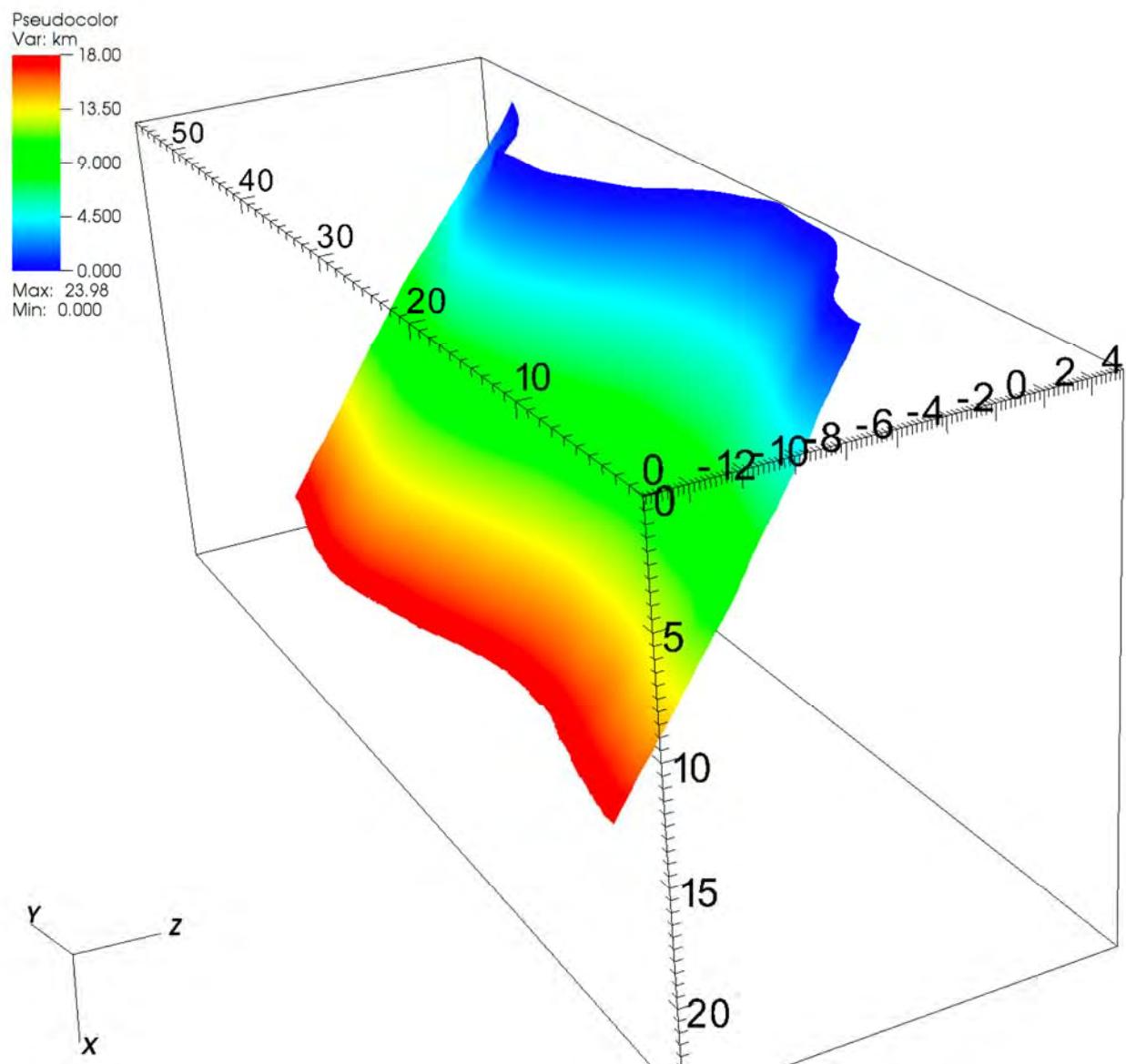


Extracted from "Utah Geological Survey Public Information Series 40: The Wasatch Fault."

Fault Geometry

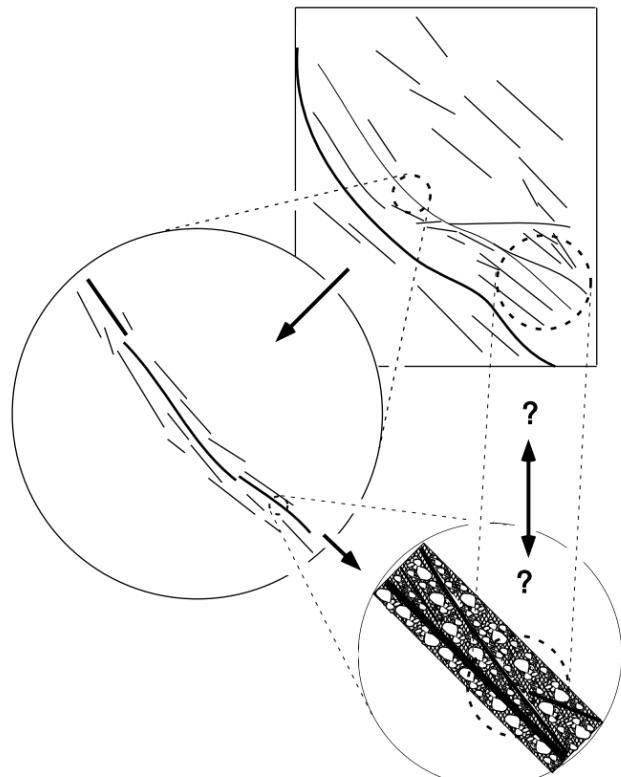


(Moschetti, 2017)

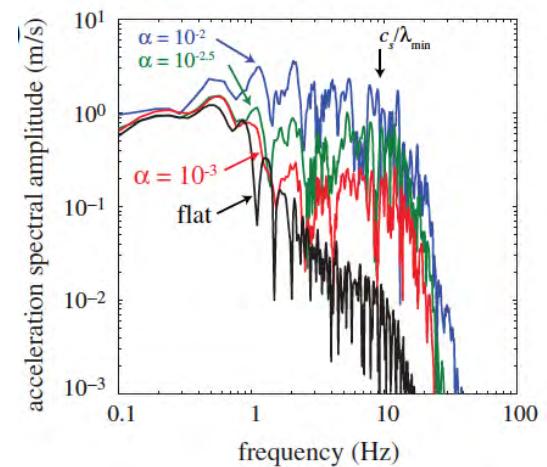


Rough Faults

- Roughness is observed at all scales

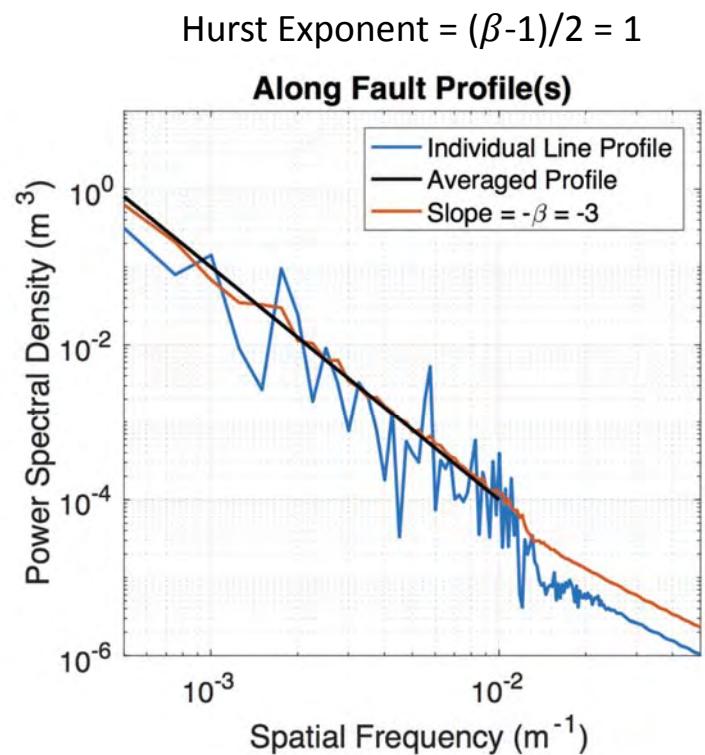
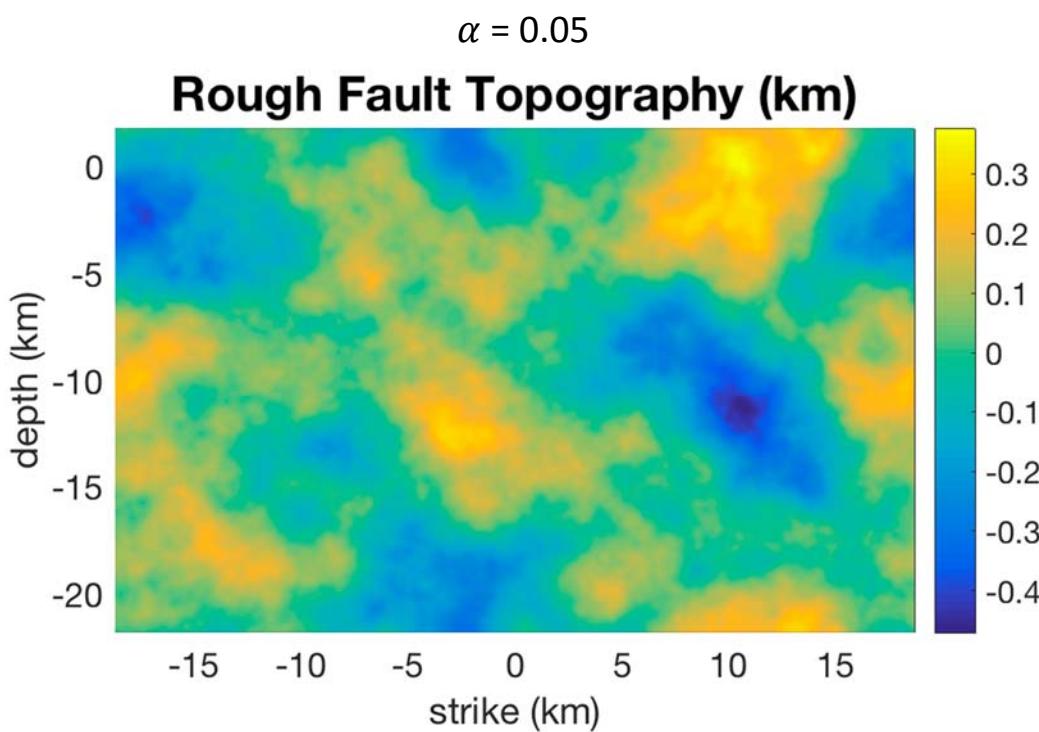


(Ben-Zion, 2003)

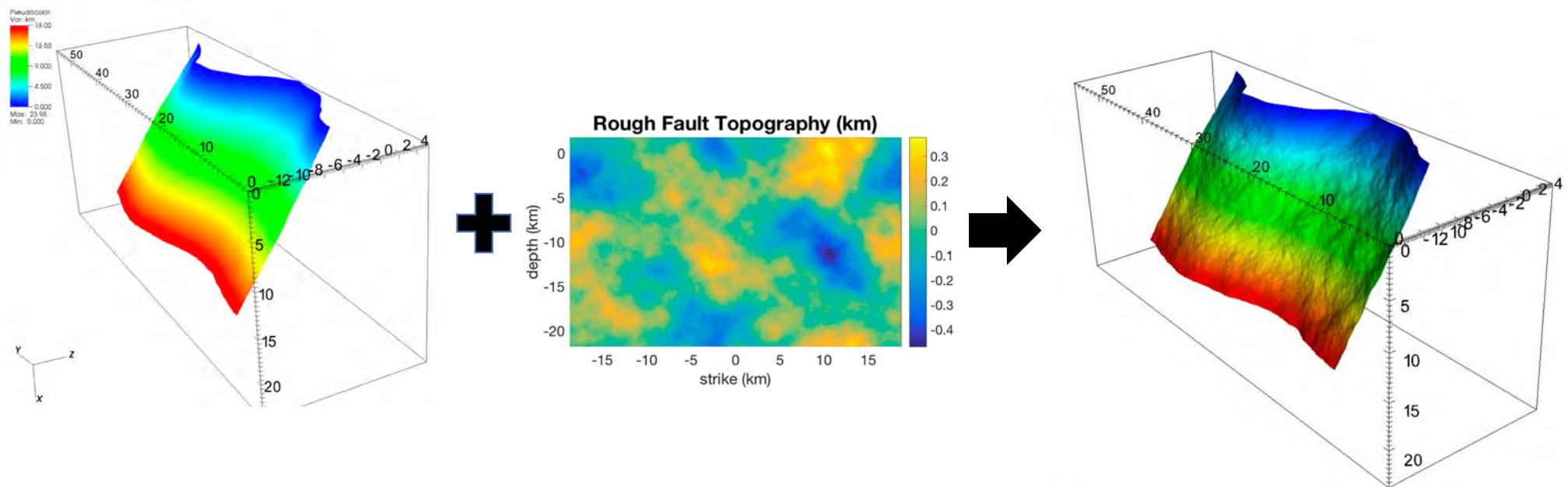


(Dunham, 2011)

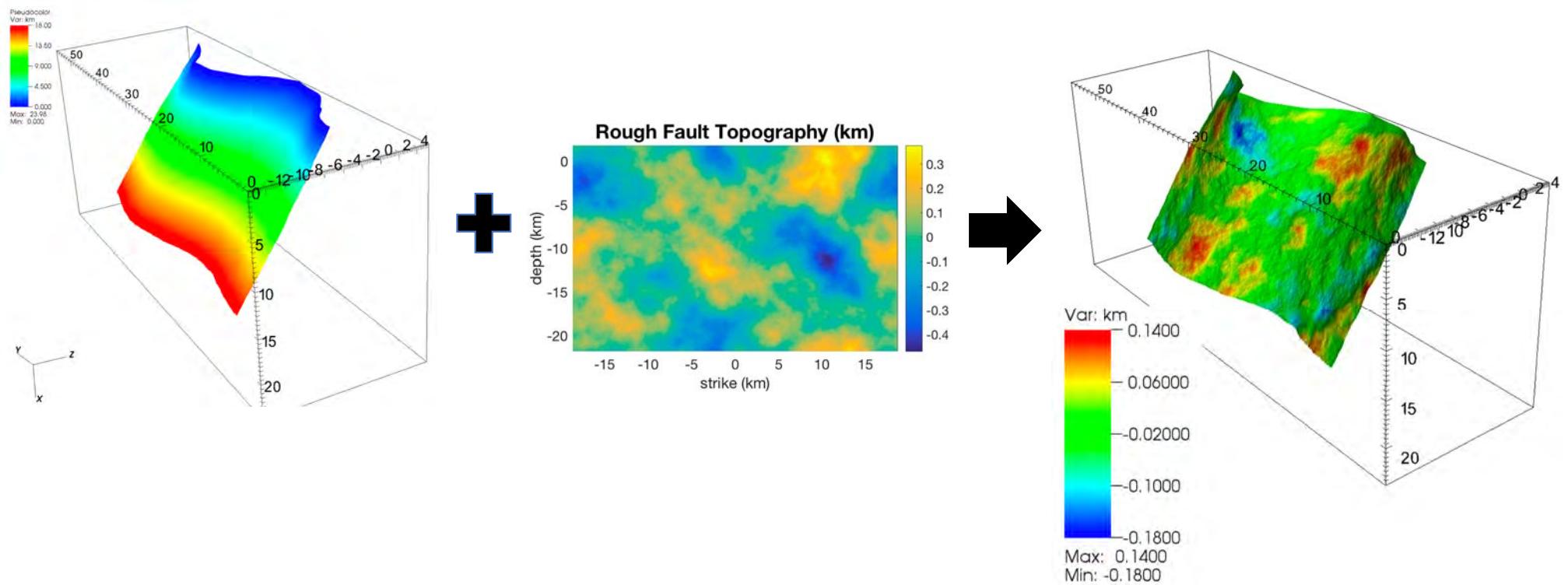
Rough Fault Complexity



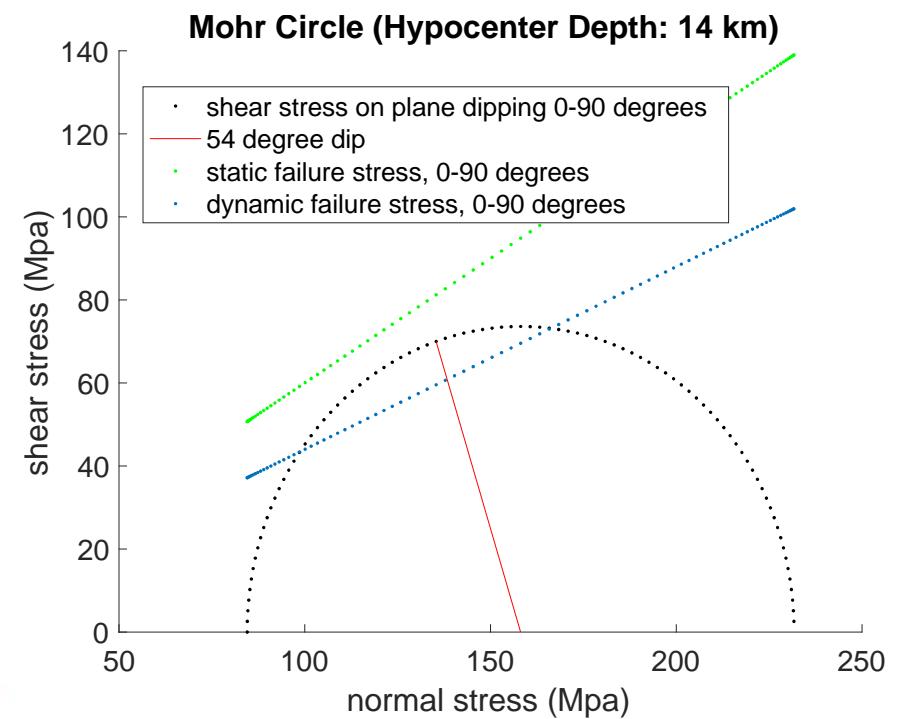
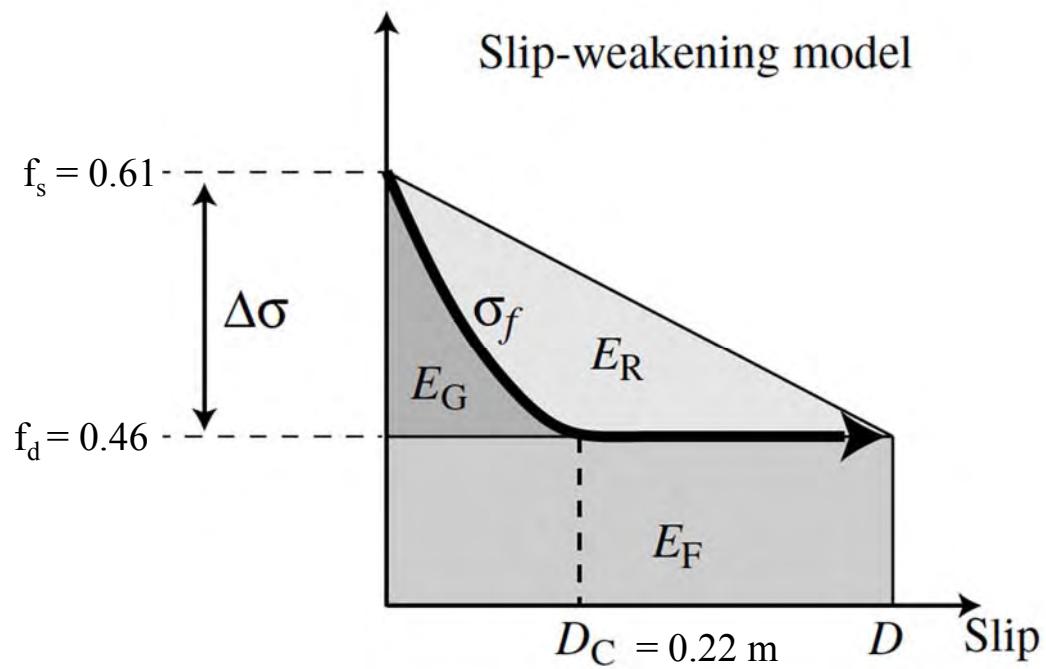
Superimposing Fault Roughness



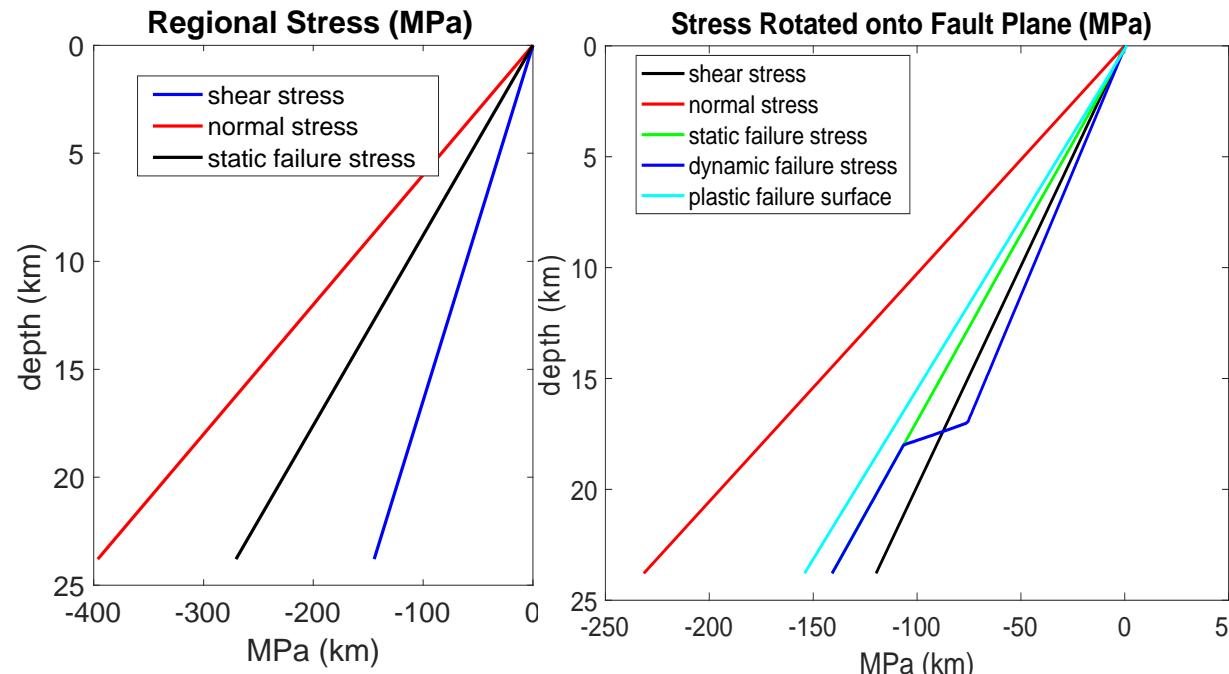
Superimposing Fault Roughness (Difference)



Friction Parameters

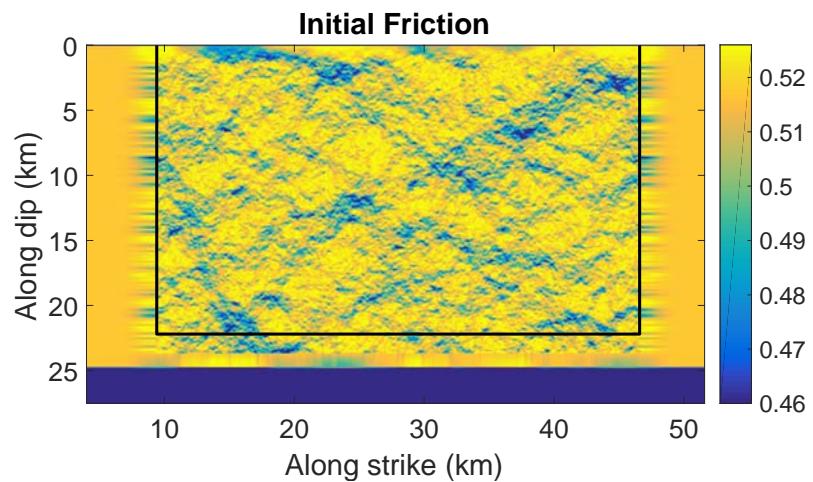


Initial Stress Conditions

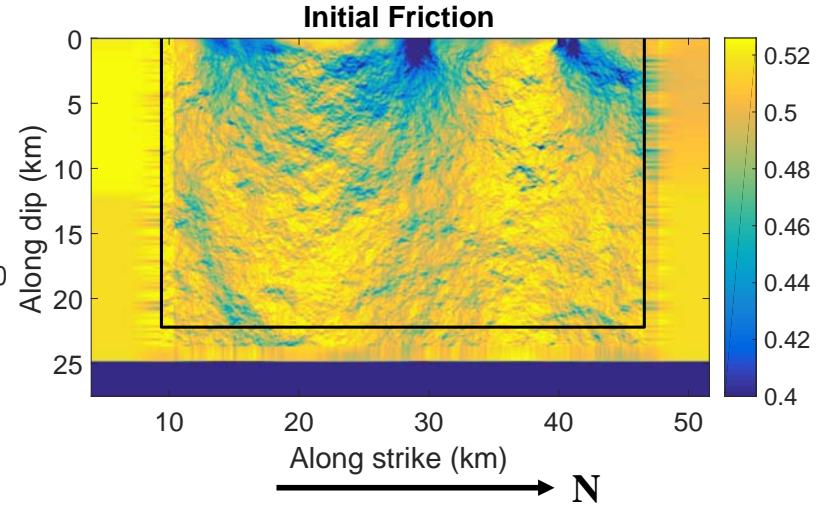


Plastic Parameters:
 cohesion = 1.18 MPa
 $\phi = 0.7$

Background Planar + Roughness

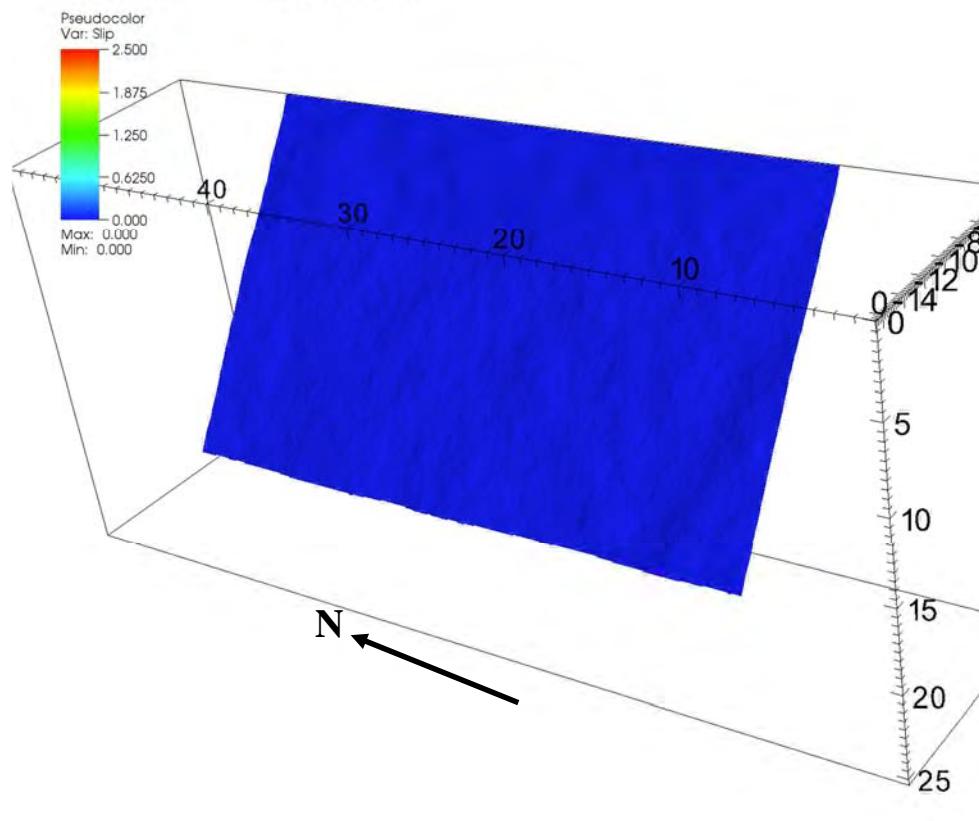


Long-Wavelength + Roughness

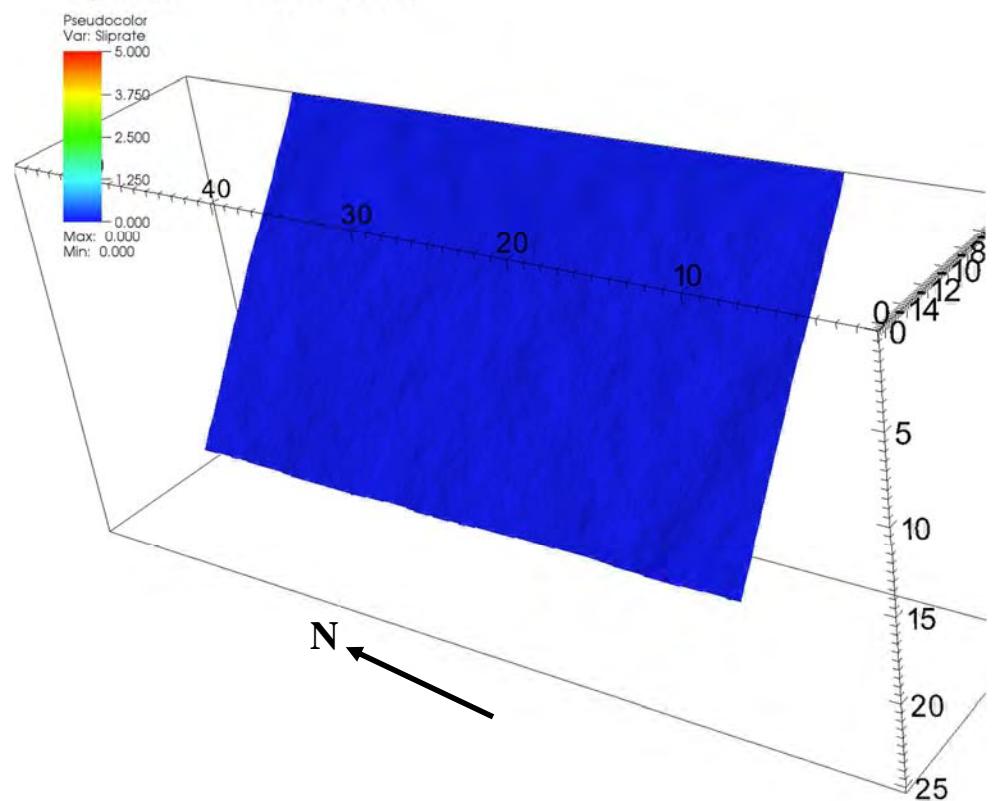


Animations of Slip and Slip-rate

DB: slipfault*.vtk database
Cycle: 6 Time:0.1165

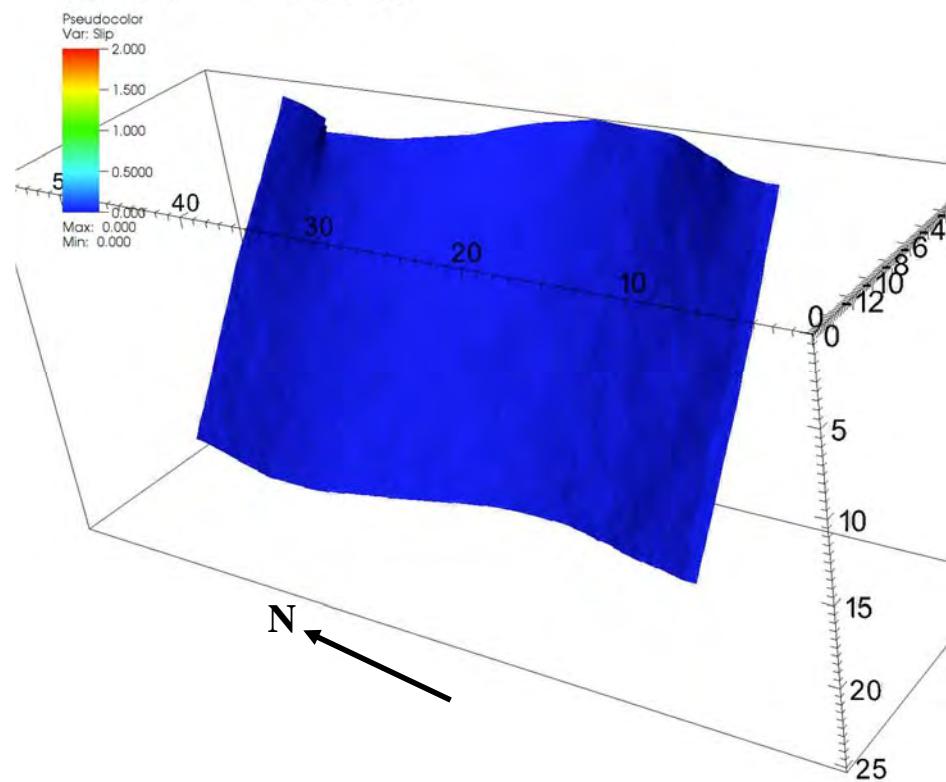


DB: slipratefault*.vtk database
Cycle: 6 Time:0.1165

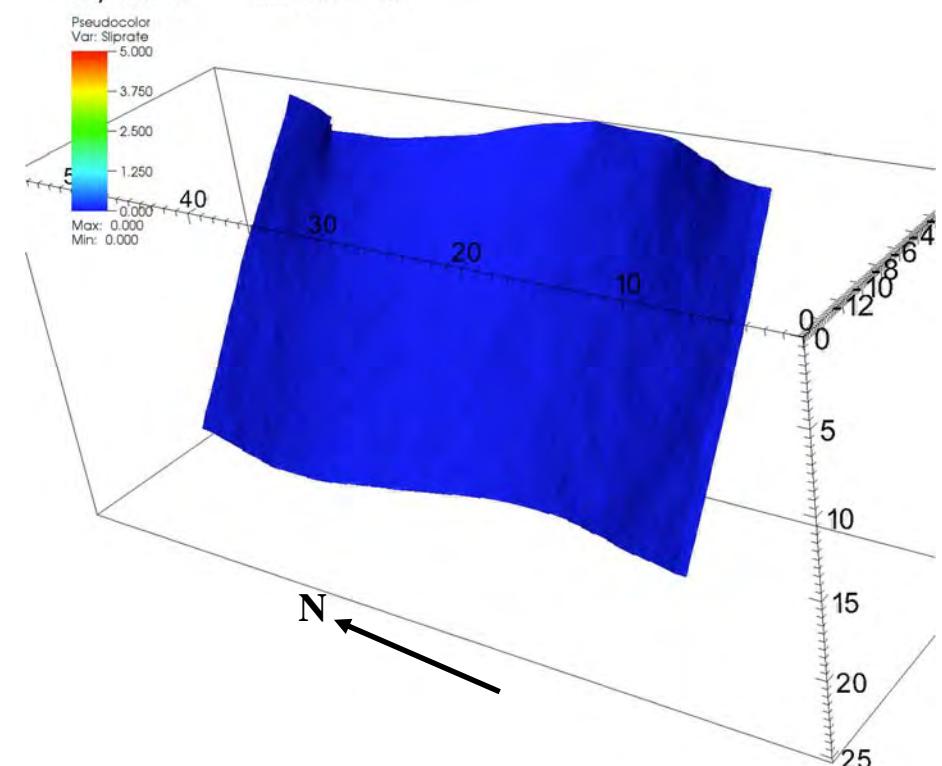


Animations of Slip and Slip-rate

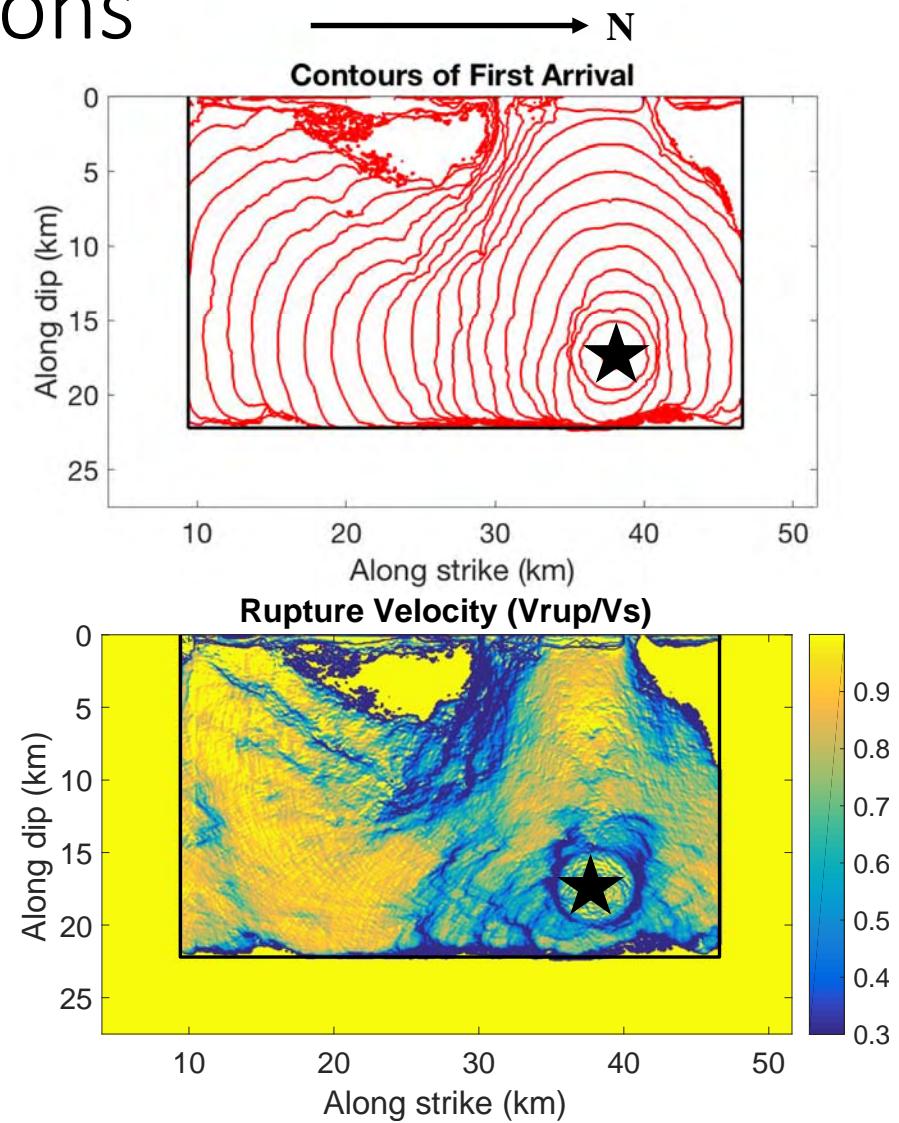
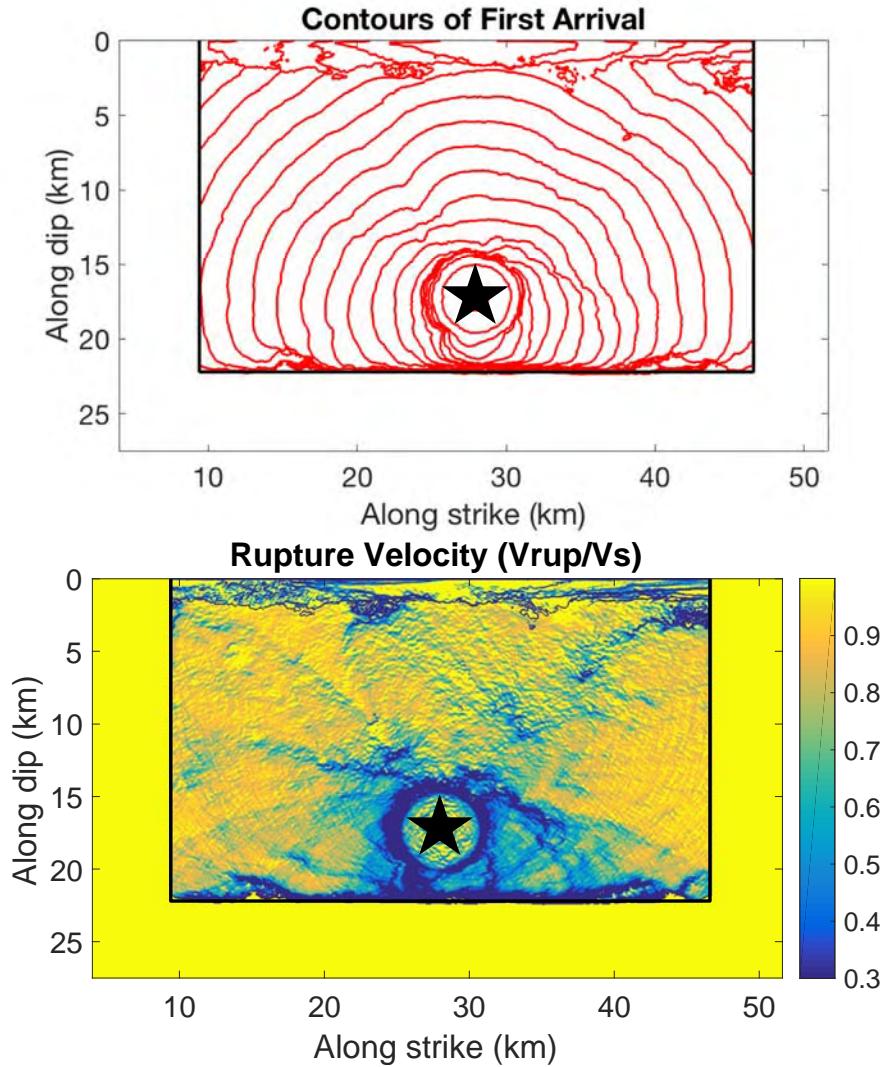
DB: slipfaultt*.vtk database
Cycle: 6 Time:0.1165

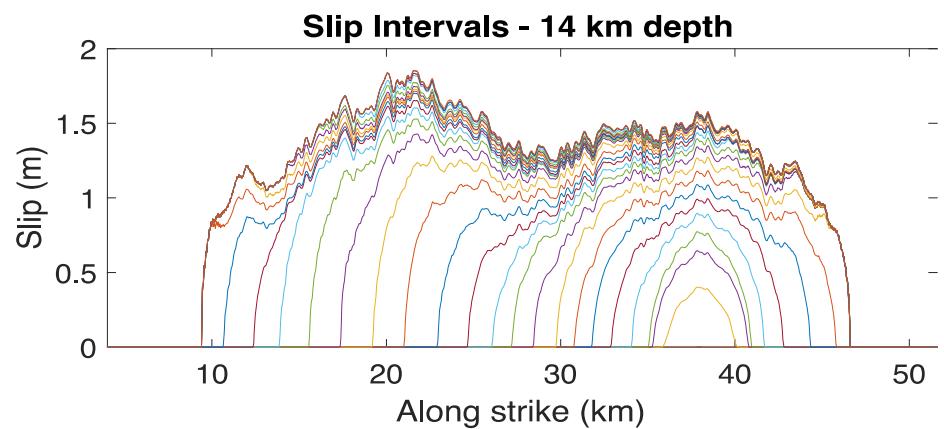
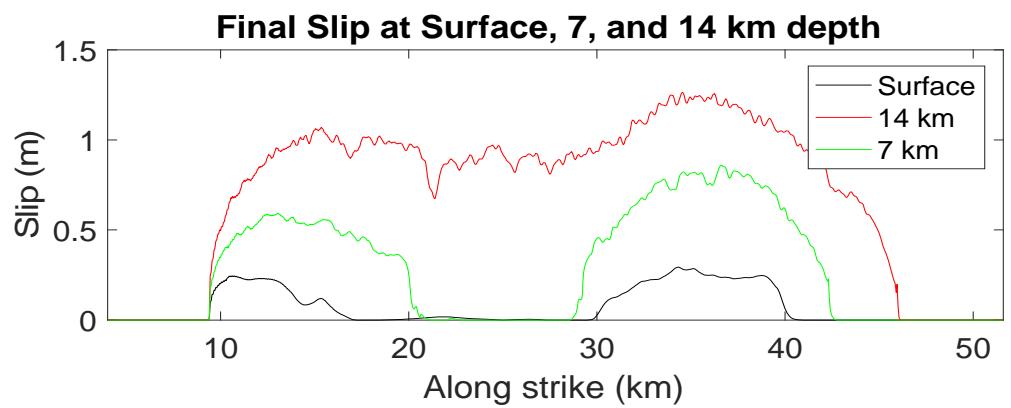
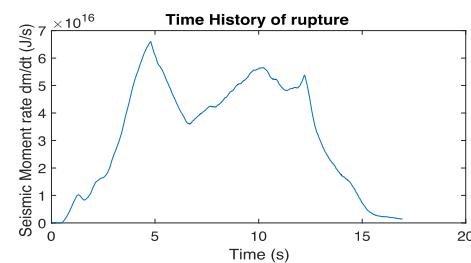
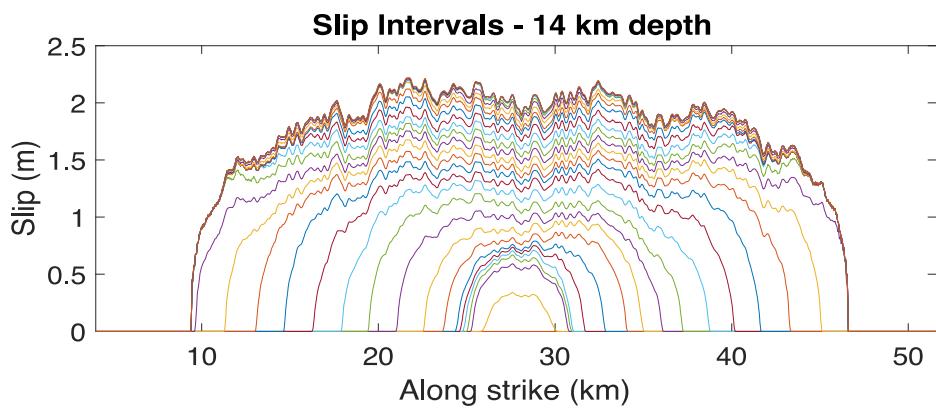
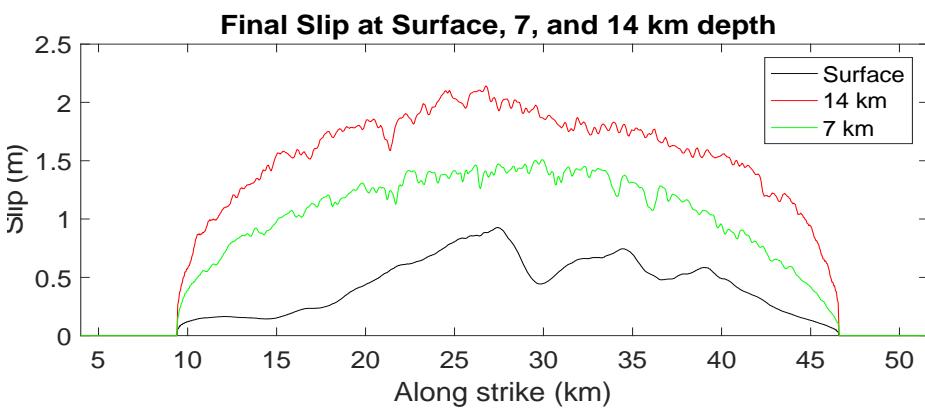
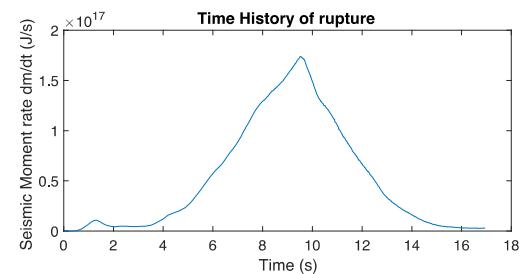


DB: sliratefaultt*.vtk database
Cycle: 6 Time:0.1165

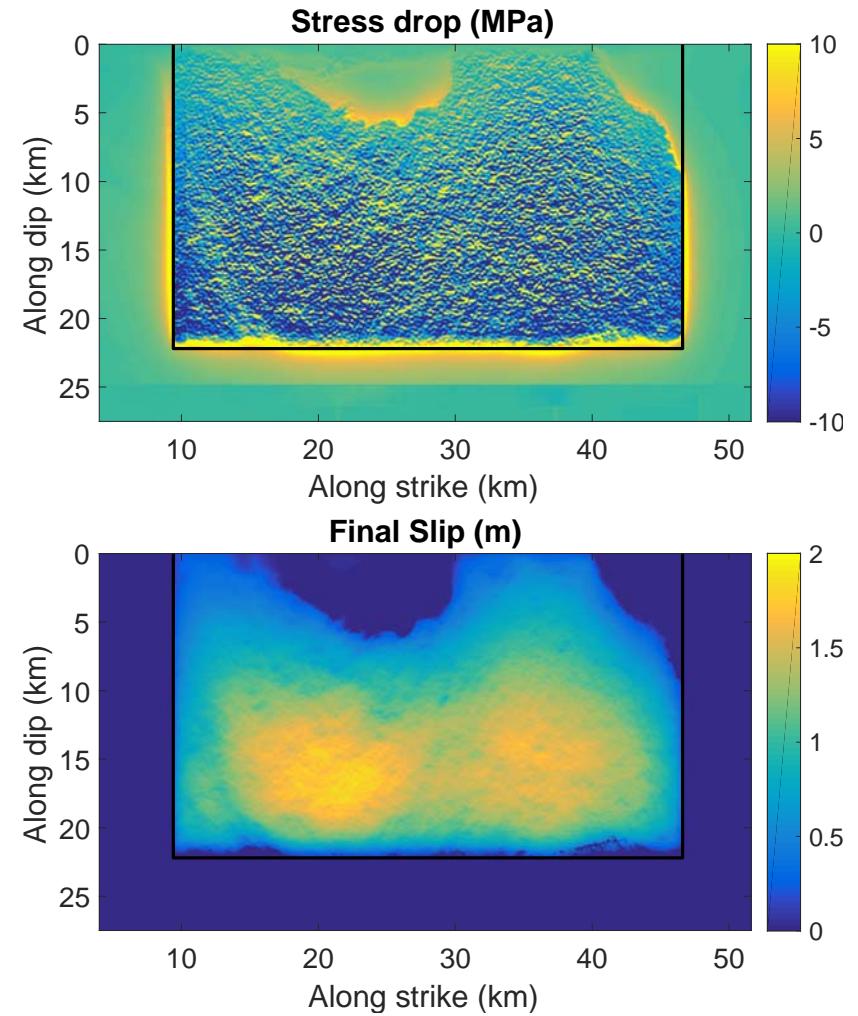
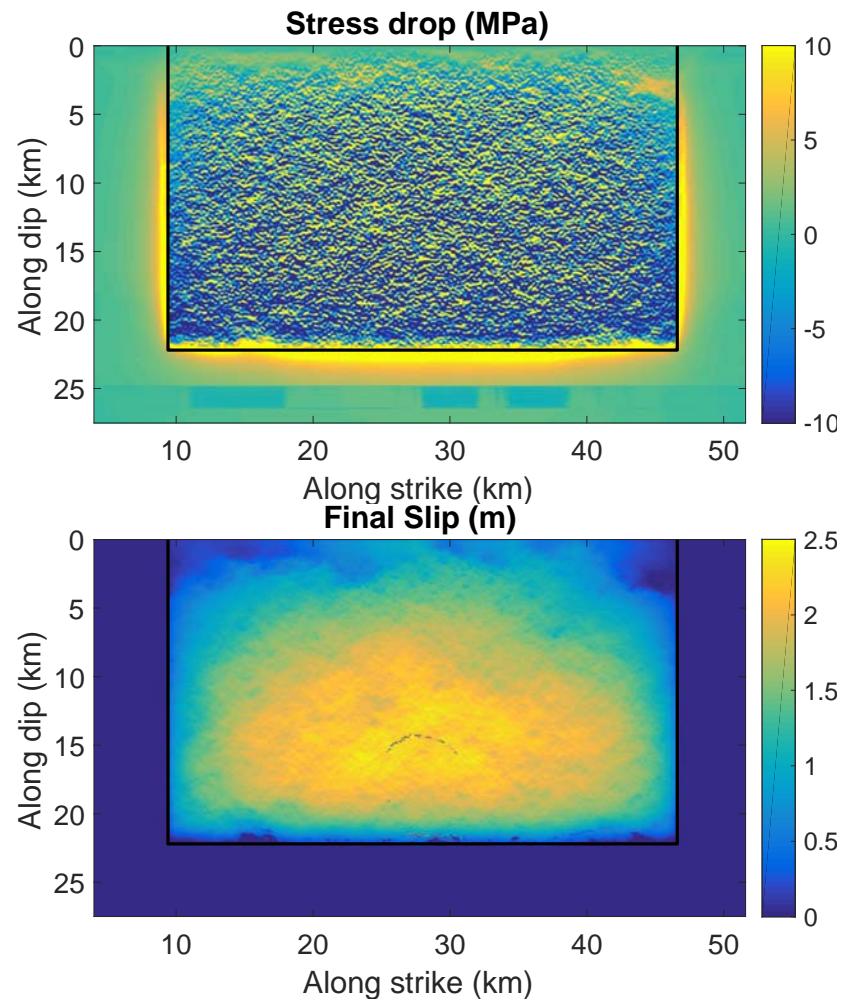


Dynamic Rupture Simulations

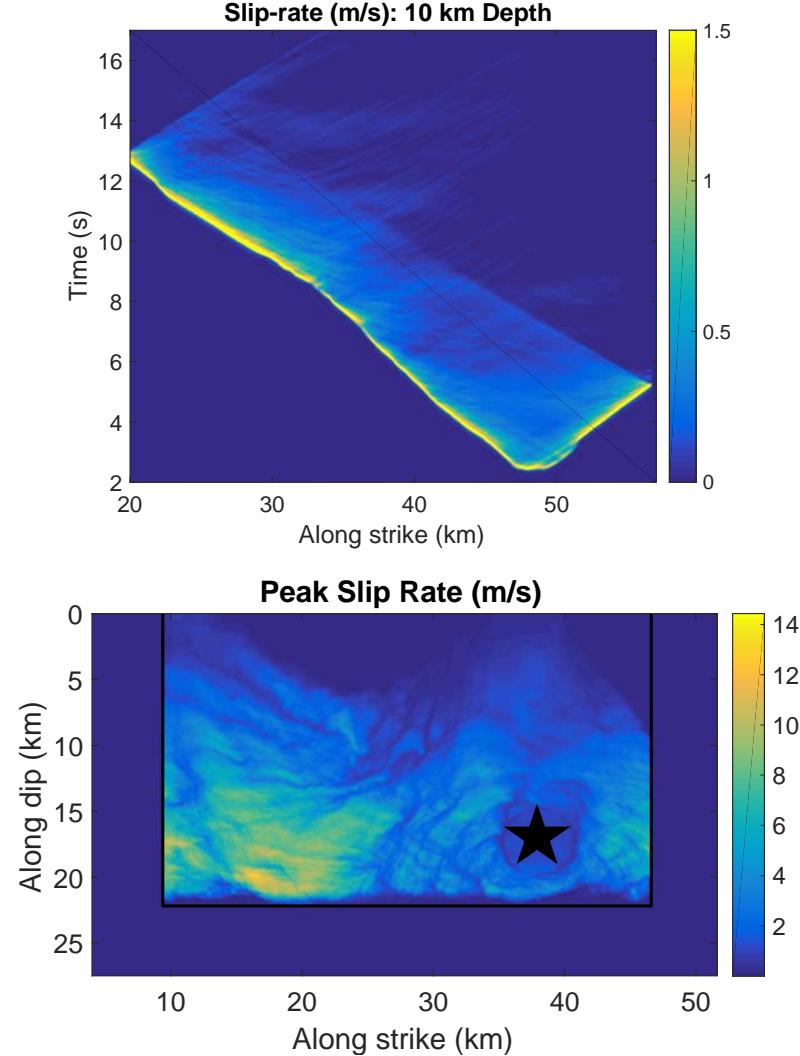
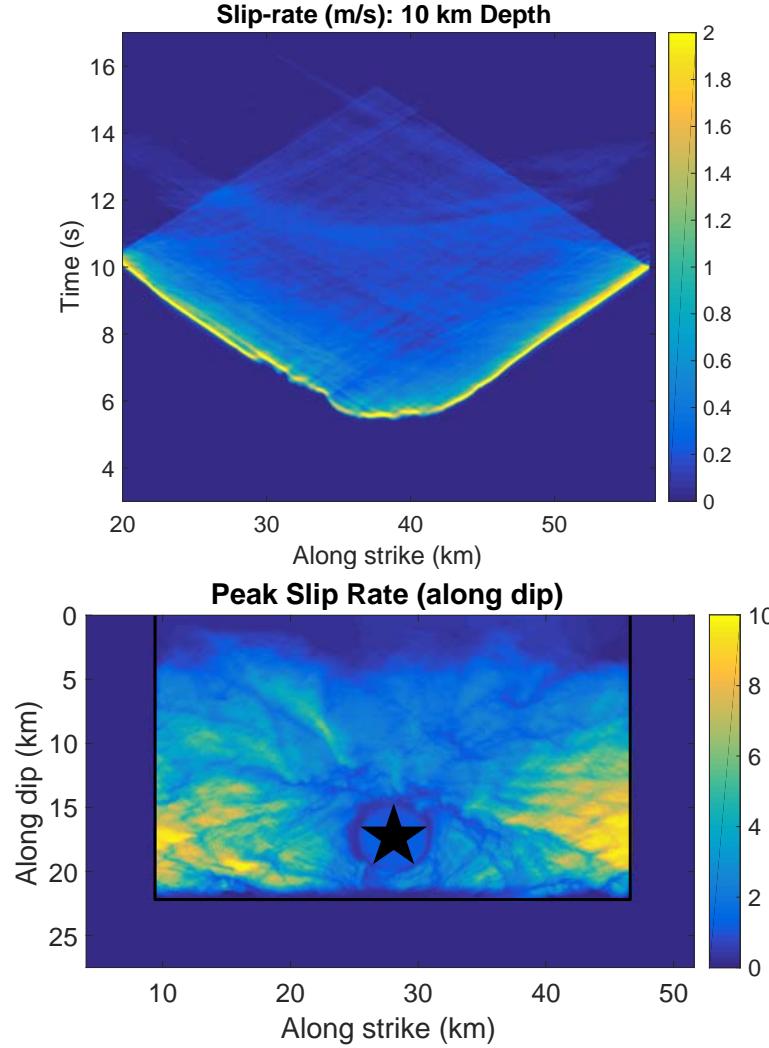


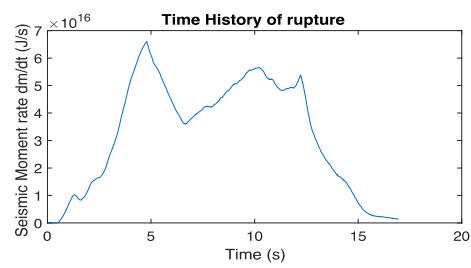
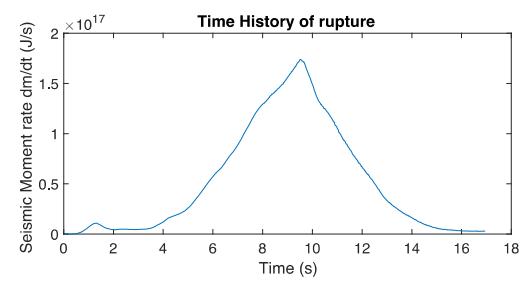


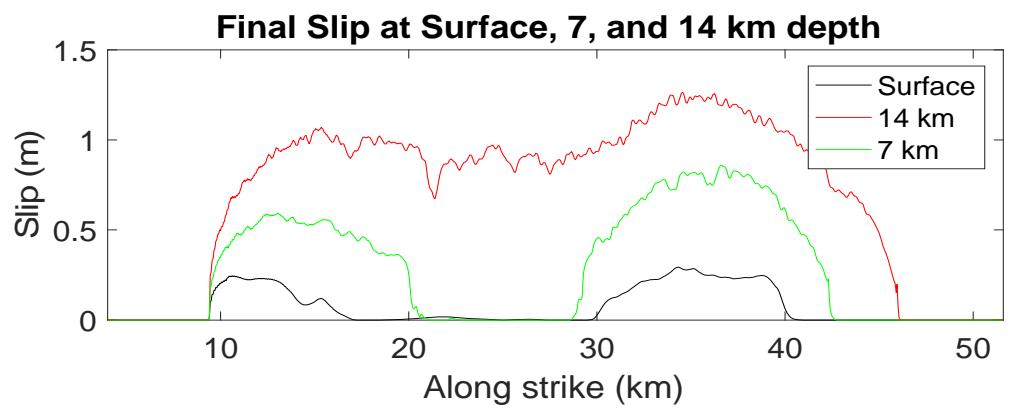
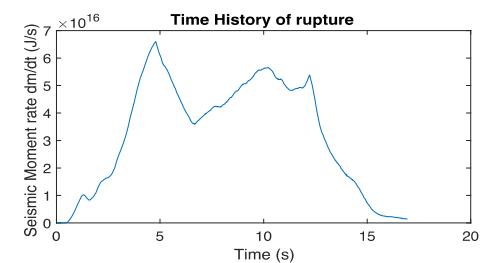
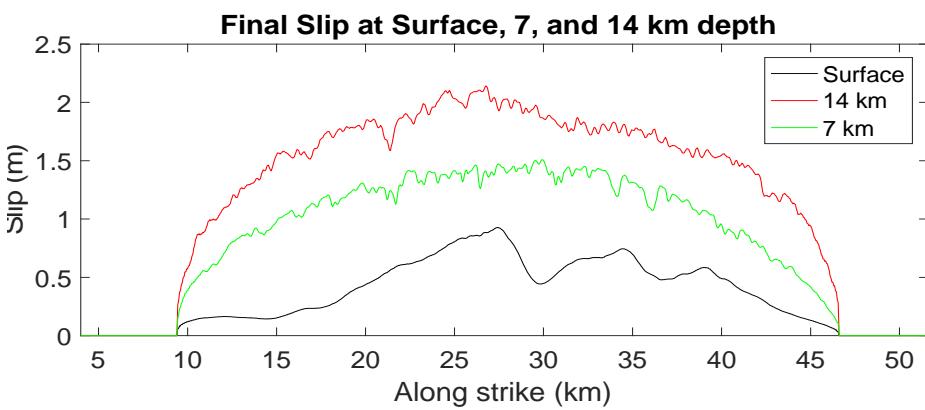
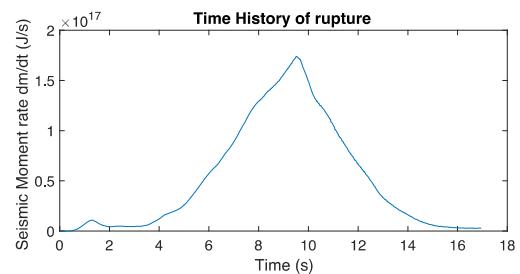
Dynamic Rupture Simulations

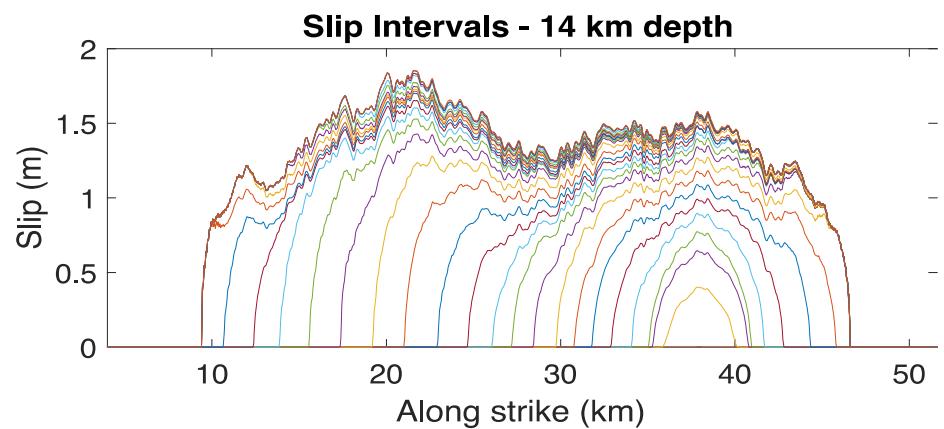
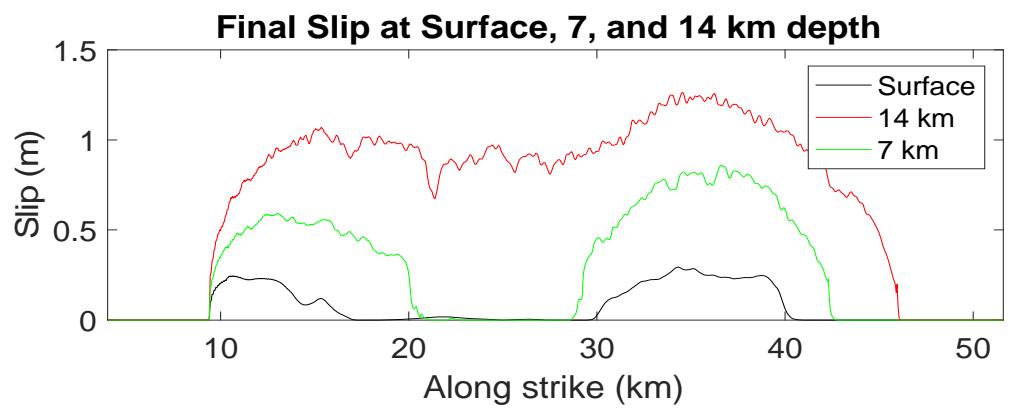
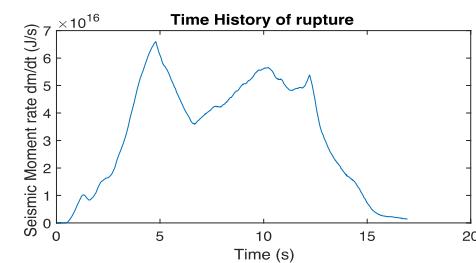
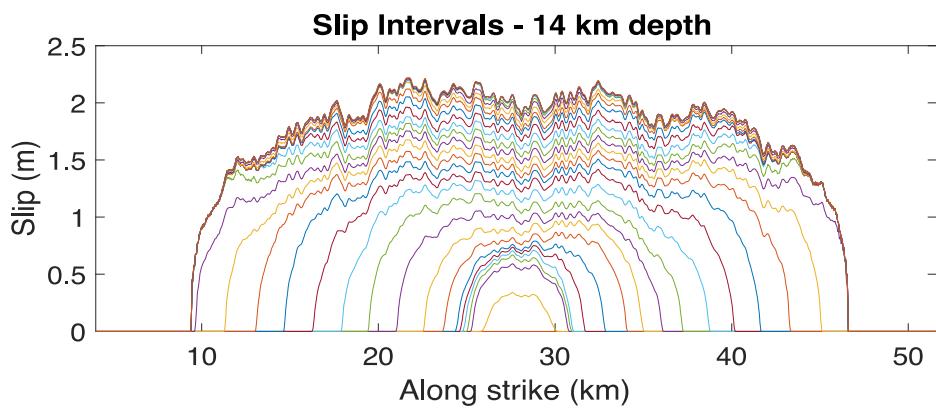
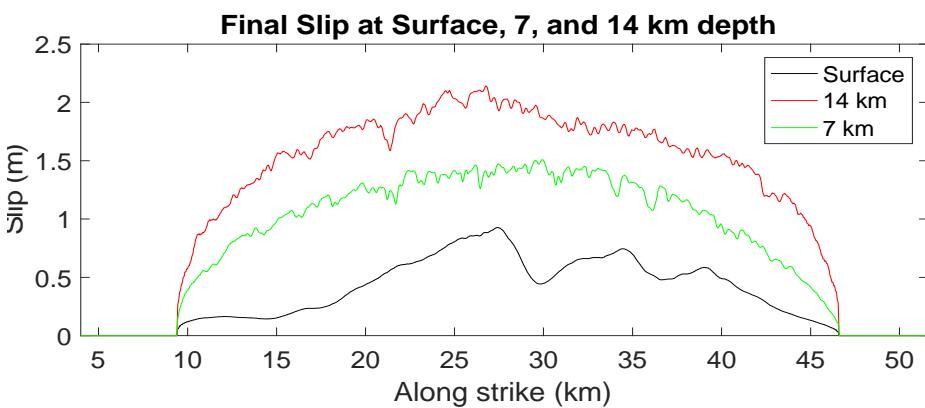
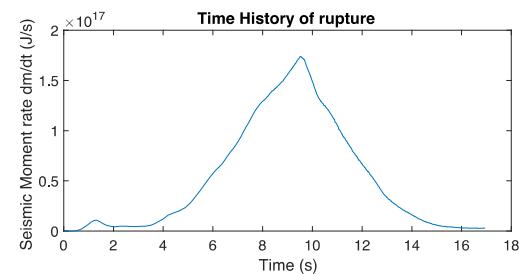


Dynamic Rupture Simulations

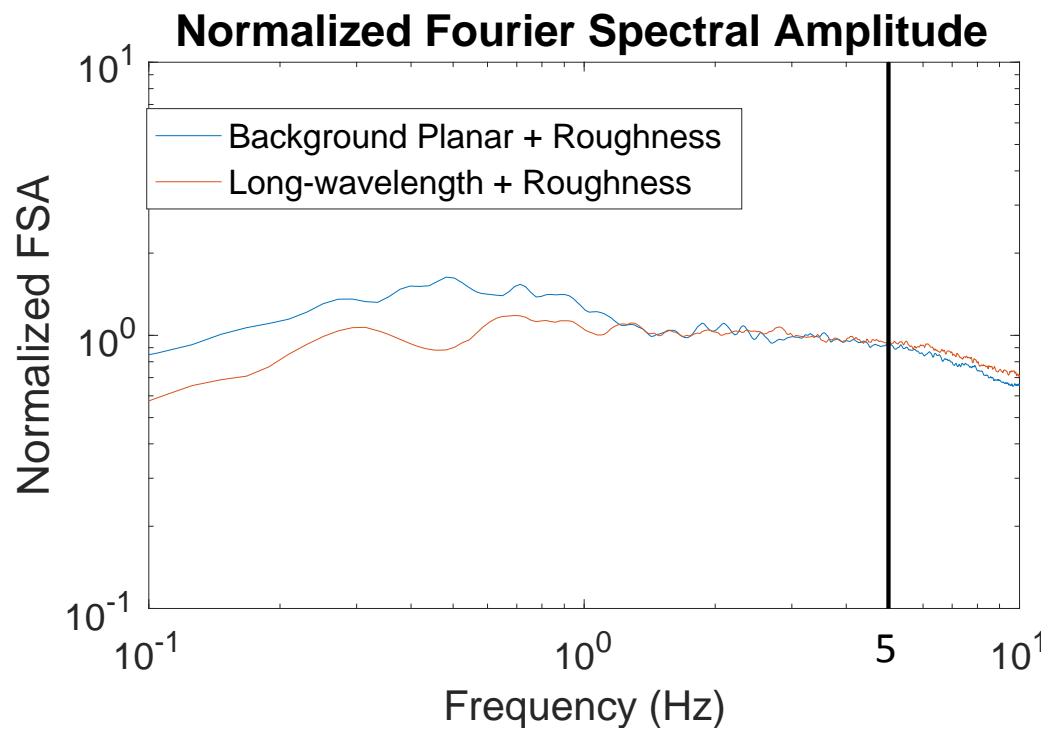
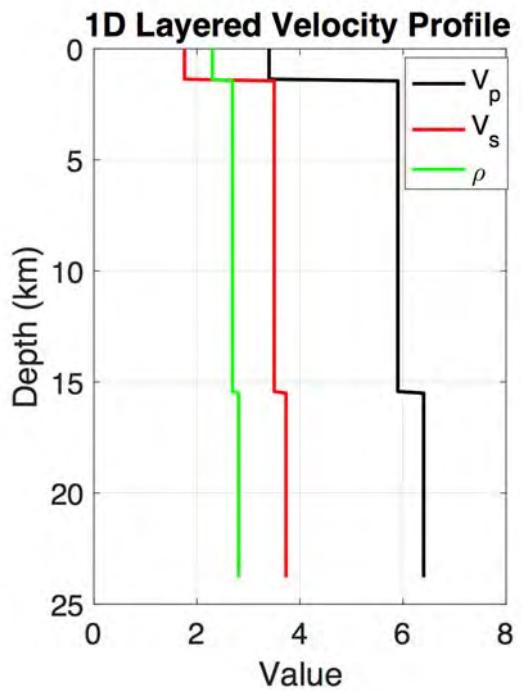






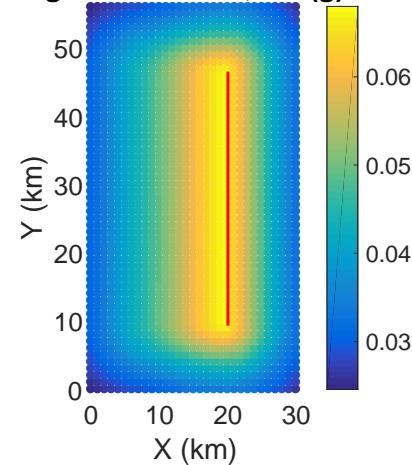


Ground Motion

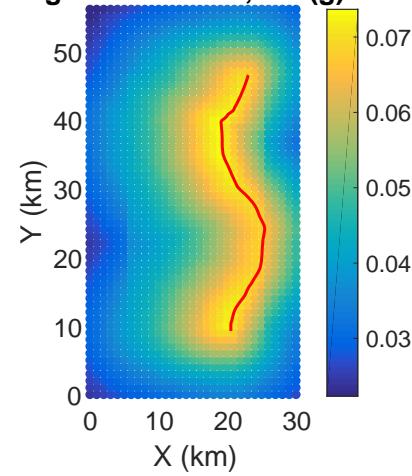


Ground Motion

Average of 4 GMPEs, SA (g) = 3 s

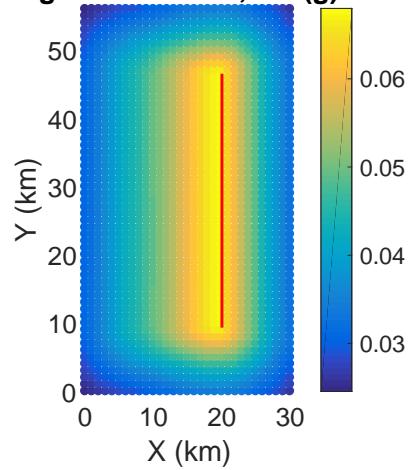


Average of 4 GMPEs, SA (g) = 3 s

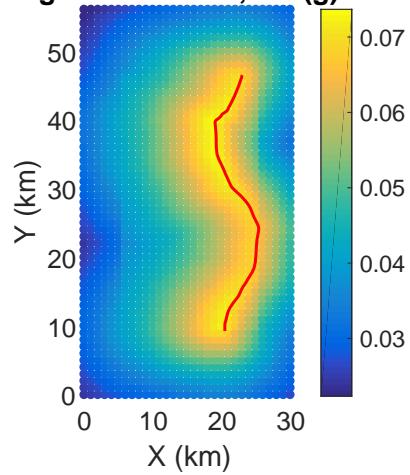


Ground Motion

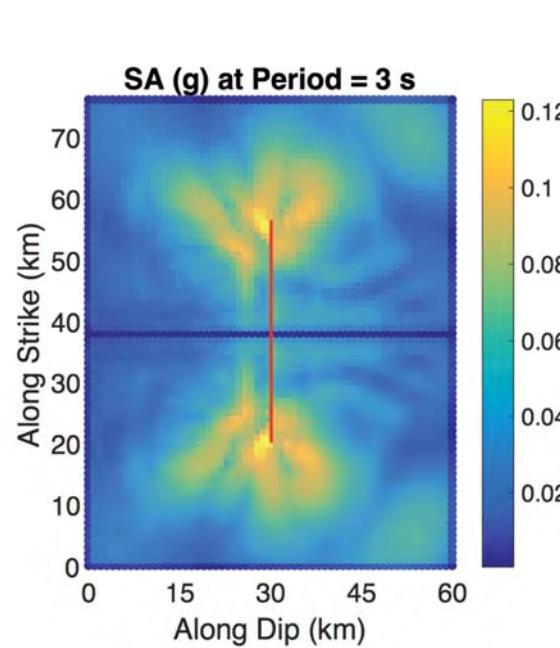
Average of 4 GMPEs, SA (g) = 3 s



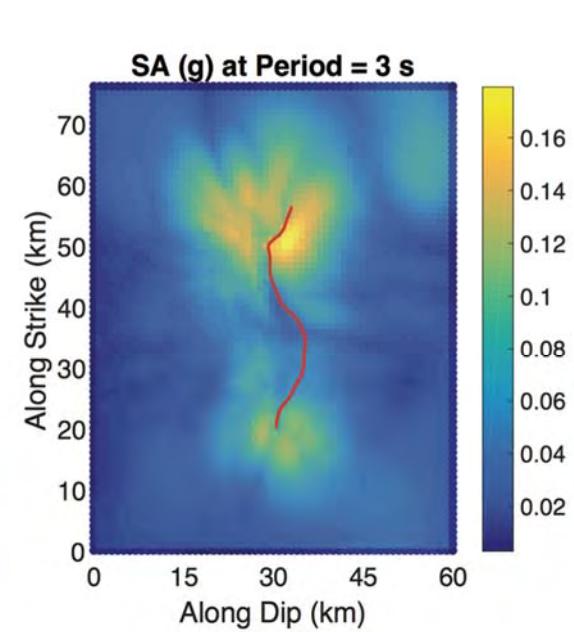
Average of 4 GMPEs, SA (g) = 3 s



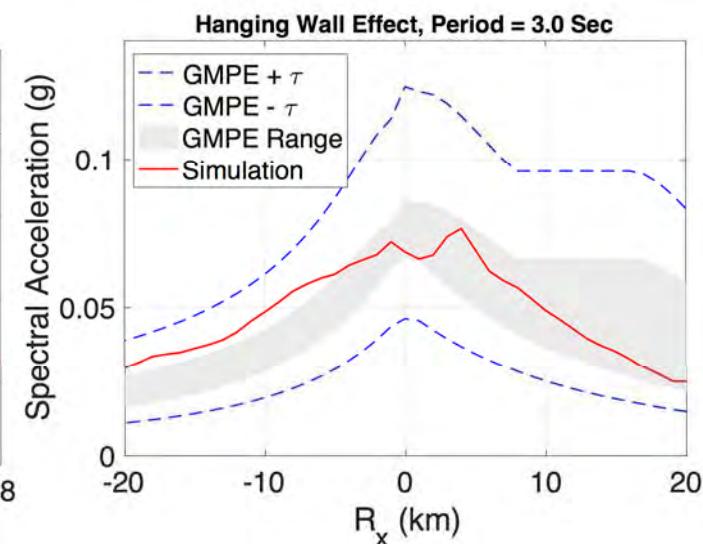
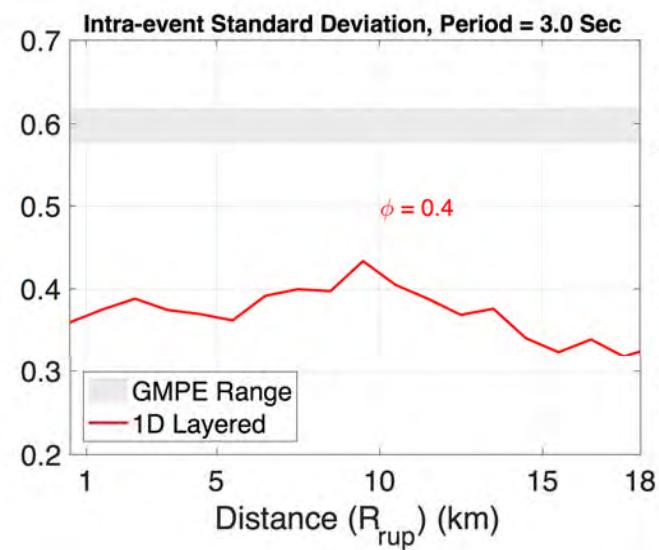
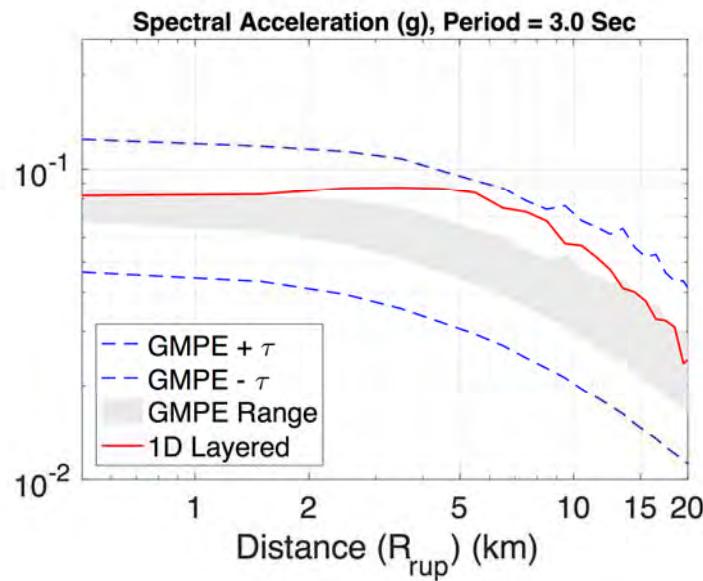
SA (g) at Period = 3 s



SA (g) at Period = 3 s



Ground Motion: Long-Wavelength + Roughness



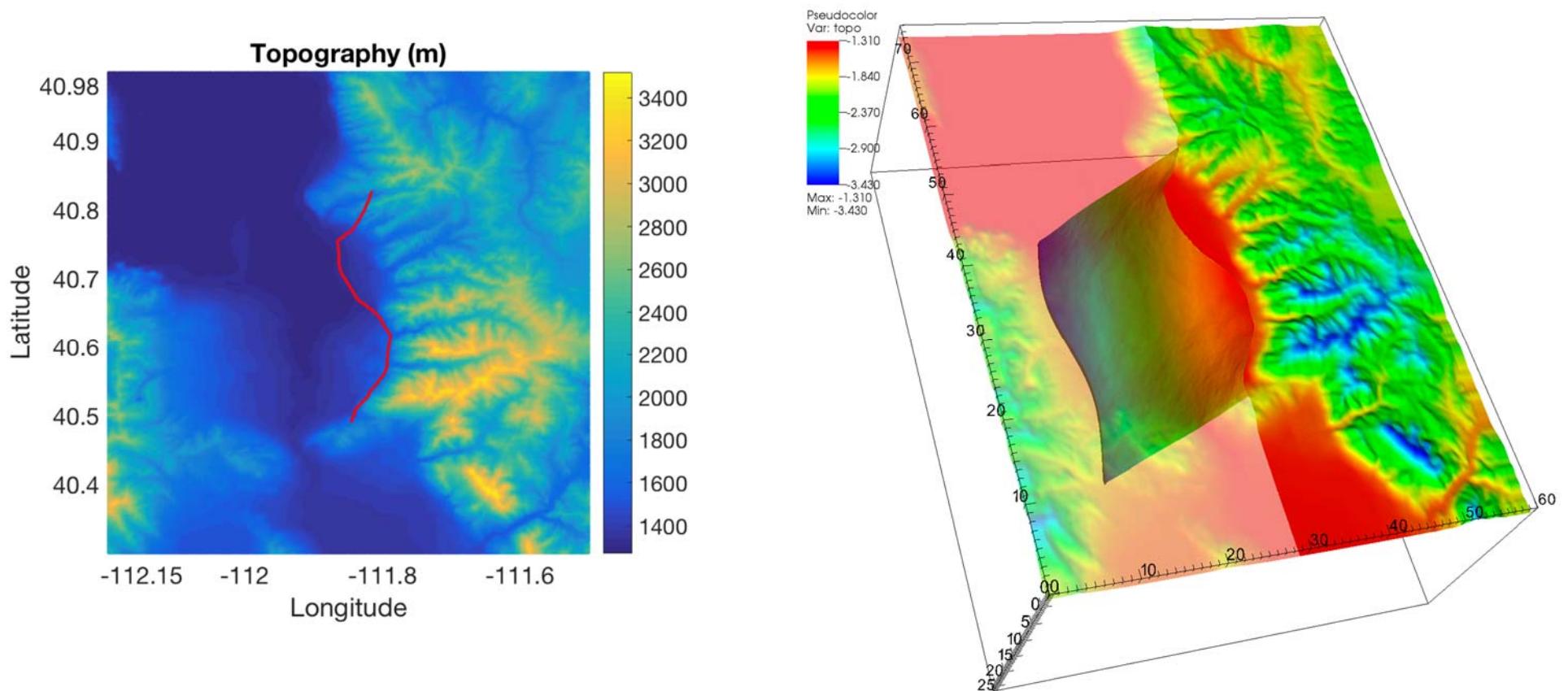
Conclusions

- Ran spontaneous rupture simulations along dipping faults, with characteristics matching that of Salt Lake City segment of Wasatch Fault
- Both short and long-wavelength geometrical complexity along the fault generates complex rupture features
- Rough-fault geometry generates comparable spectral energy to that of observations
- Initial comparison of synthetics with leading GMPEs show good fits

Future Work

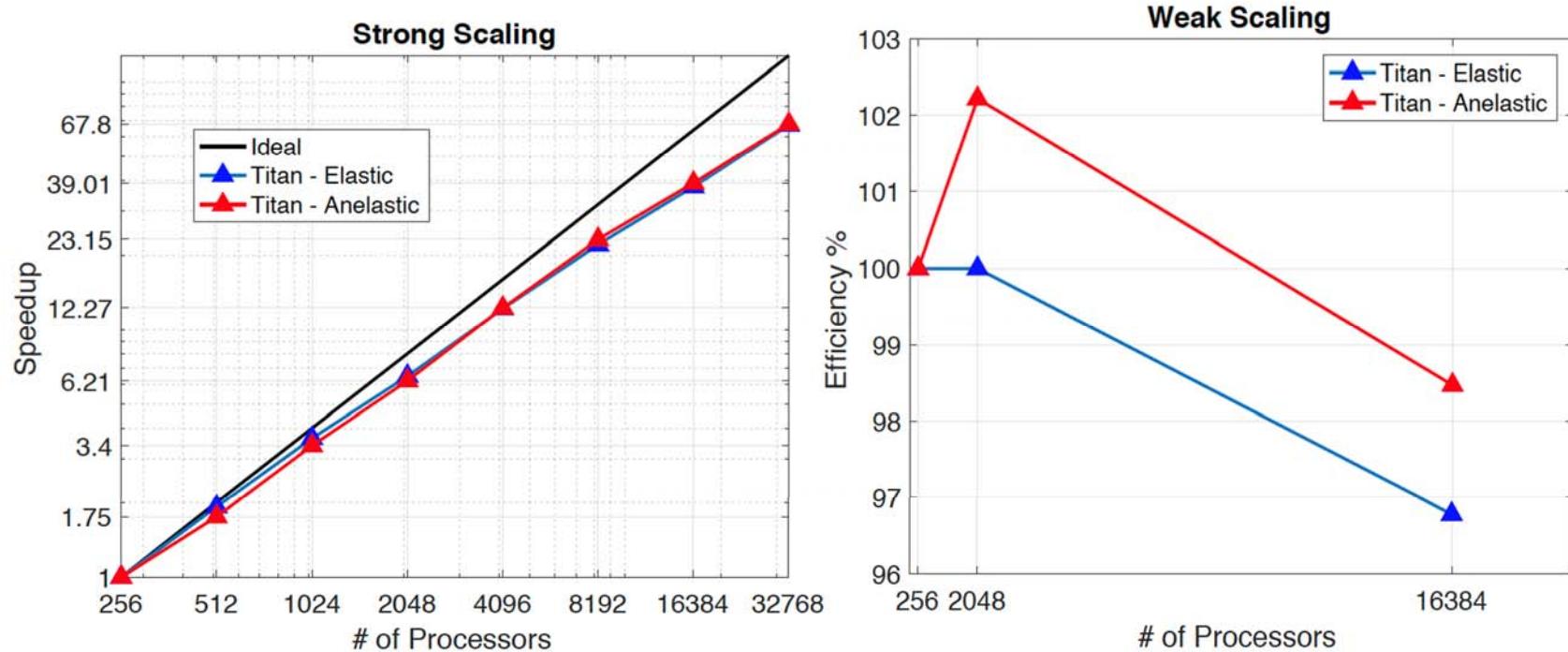
- Additional dynamic rupture simulations with varying hypocenter locations, rough fault topographies, stress conditions, etc...
- Correlation of ground motions (spatially/frequency)?
- Path vs. site effects (affecting uncertainty)
- Stress transfer to other parts of Wasatch fault
- Multi-segment rupture

Free-surface Topography



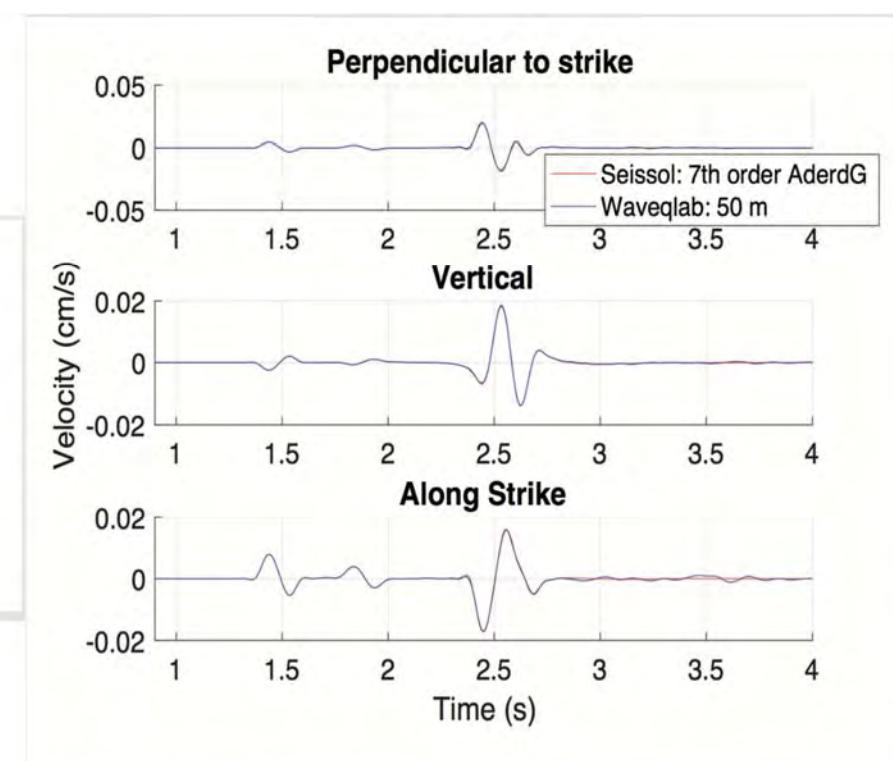
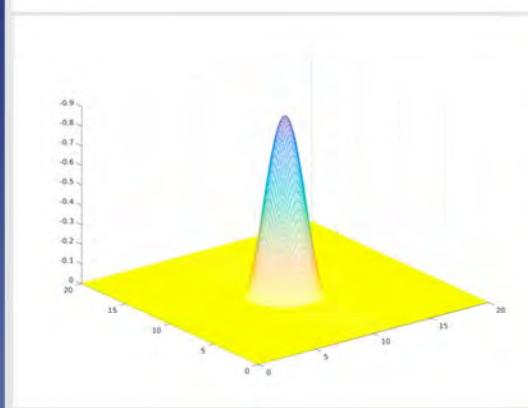
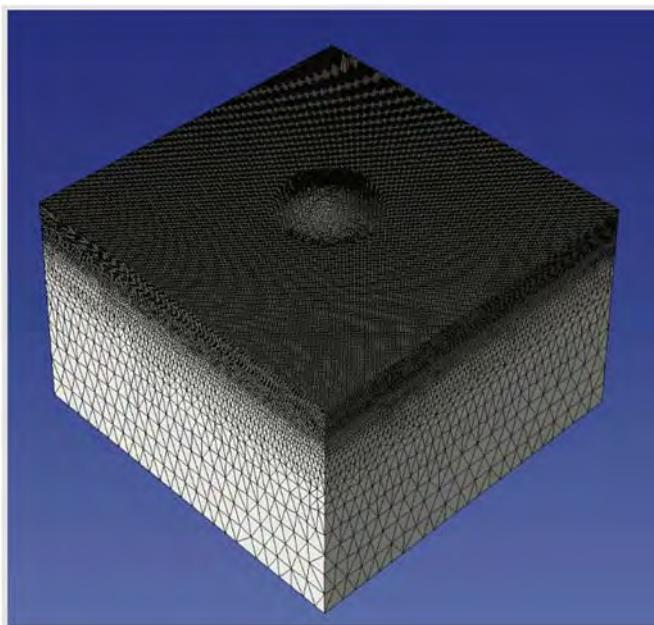
Additional Slides

Strong and Weak Scaling

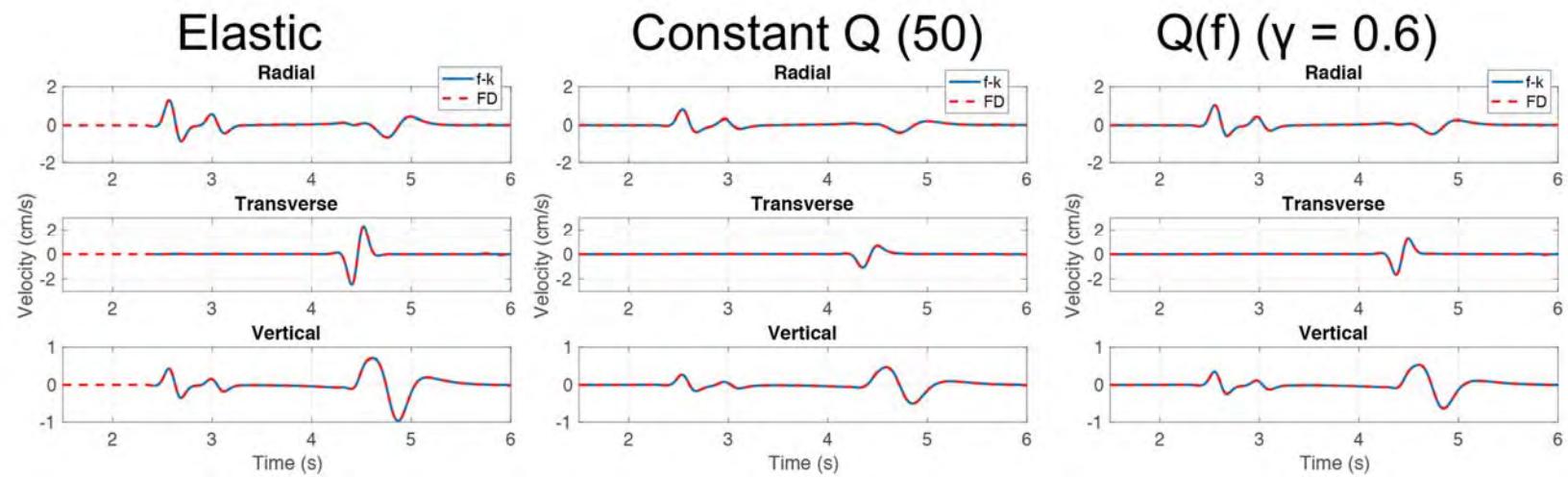
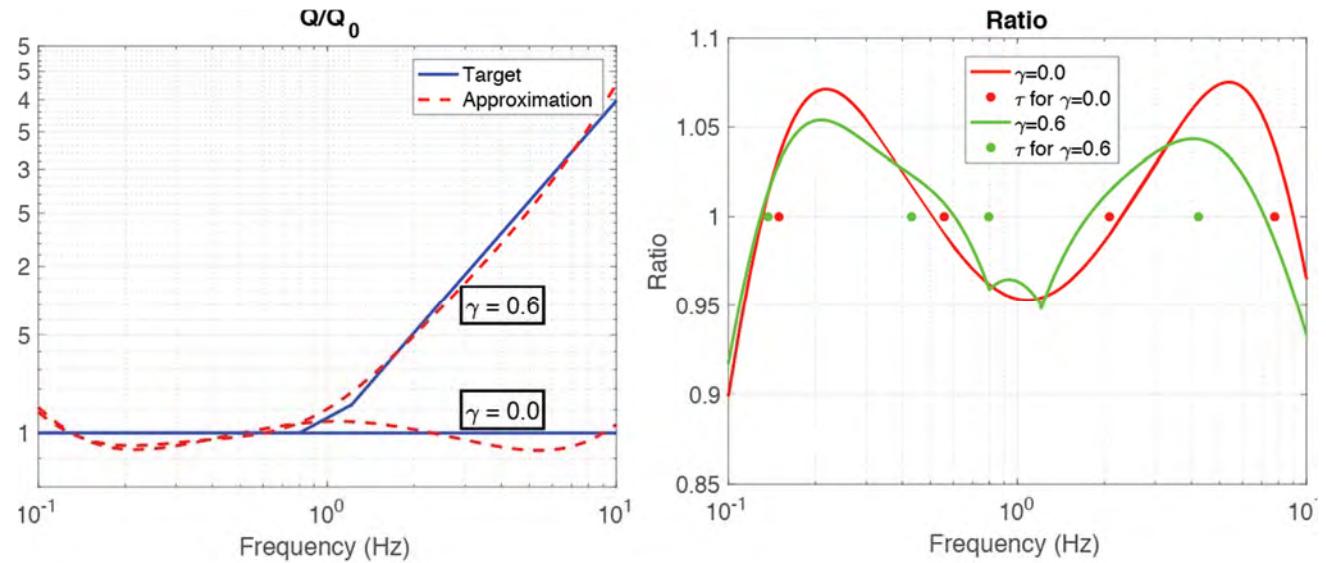


Free-surface Topography Validation

- Simple Gaussian Hill Model, comparison with Seissol



$Q(f)$ Validation



Implementation of WUS Sedimentary Basin Effects into the 2018 NSHM

Case Study: Wasatch Front

Mark Petersen

USGS, Golden, CO

2018 Utah Earthquake Working Groups Meeting

Tuesday, February 13th, 2018



Background

- In the 2014 NSHM, we accounted for average sedimentary basin effects in the WUS by using default basin depths calculated from NGA-West2 GMMs
- These default Z_x terms have been shown to underestimate the hazard at long periods ($T \geq 1$ s) in areas of the WUS with deep basins, maybe not for shallow basins
- As part of the development of the 2018 NSHM we show the sensitivity of hazard to basin depths derived from three different methods.

2014 NSHM: Default Zx Terms

Default Basin Depths (km) Calculated from NGA-West2 GMMs

Site Class	V _{s30} (m/s)	ASK14(Z _{1.0})	BSSA14(Z _{1.0})	CB14(Z _{2.5})	CY14(Z _{1.0})
A	2000	0.000	0.000	0.201	0.000
A/B	1500	0.000	0.001	0.279	0.001
B	1080	0.005	0.005	0.406	0.005
B/C	760	0.048	0.041	0.607	0.041
C	530	0.213	0.194	0.917	0.194
C/D	365	0.401	0.397	1.40	0.400
D	260	0.475	0.486	2.07	0.485
D/E	185	0.497	0.513	3.06	0.513
E	150	0.502	0.519	3.88	0.519

Methods

- Method #1: LOCAL For 4 regions in the WUS (LA Basin, Bay Area, Wasatch Front, and Seattle) from published local seismic velocity models.
- Method #2: VS30 For the entire WUS, from the USGS V_{s30} database (Yong *et al.*, 2016)
- Method #3: COMPOSITE For the entire WUS, a composite basin depth model based on published regional and national velocity models. The composite model is a weighted average where the weights are dependent on the ability of the GMMs and basin model to reduce the variance of observed intra-event ground motion residuals in the NGA-West2 GMMs for the WUS (Boyd *et al.*, 2018).

Method 1: Z_x Terms from Local Seismic Velocity Models

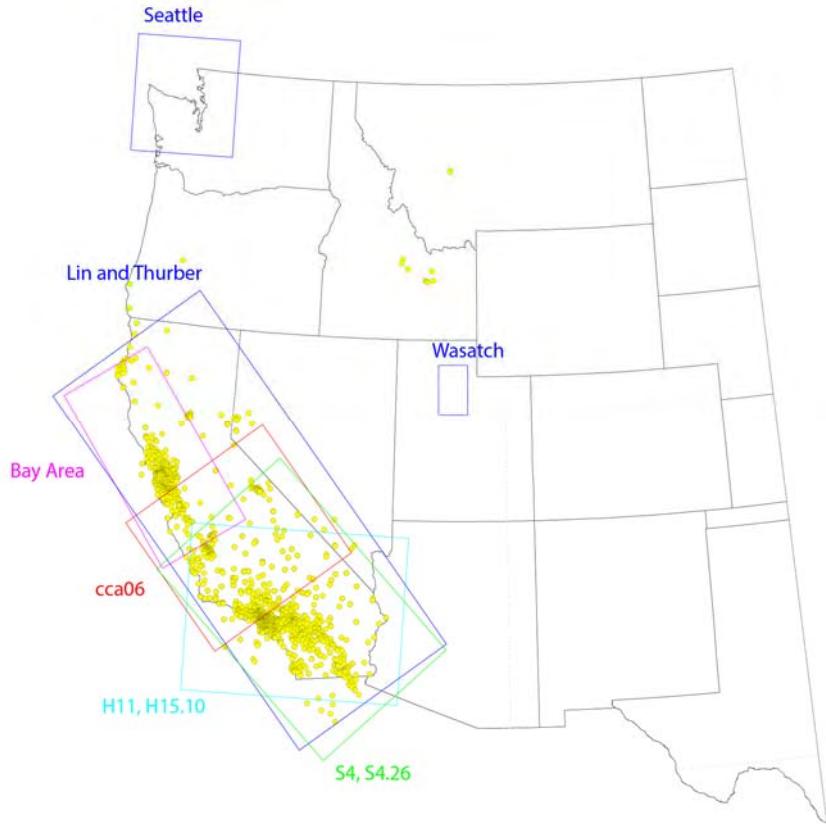


Figure 2 (from Boyd *et al.*, 2018). NGA-W2 station locations (circles) and outlines of the regional velocity models. The national models cover the entire region.

1. Uniform V_{s30} hazard maps are run for each region using Z_x terms from local seismic velocity models for 0.02 degree grids.

Velocity Models	
BayArea10	(Aagaard <i>et al.</i> , 2010)
S4.26m01	(Lee <i>et al.</i> , 2014)
Seattle07	(Stephenson, 2007)
Wasatch08	(Magistrale <i>et al.</i> , 2008)

Site Class	V_{s30} (m/s)
A	2000
A/B	1500
B	1080
B/C	760
C	530
C/D	365
D	260
D/E	185
E	150

Method 2: Z_x Terms Calculated from USGS V_{s30} Database

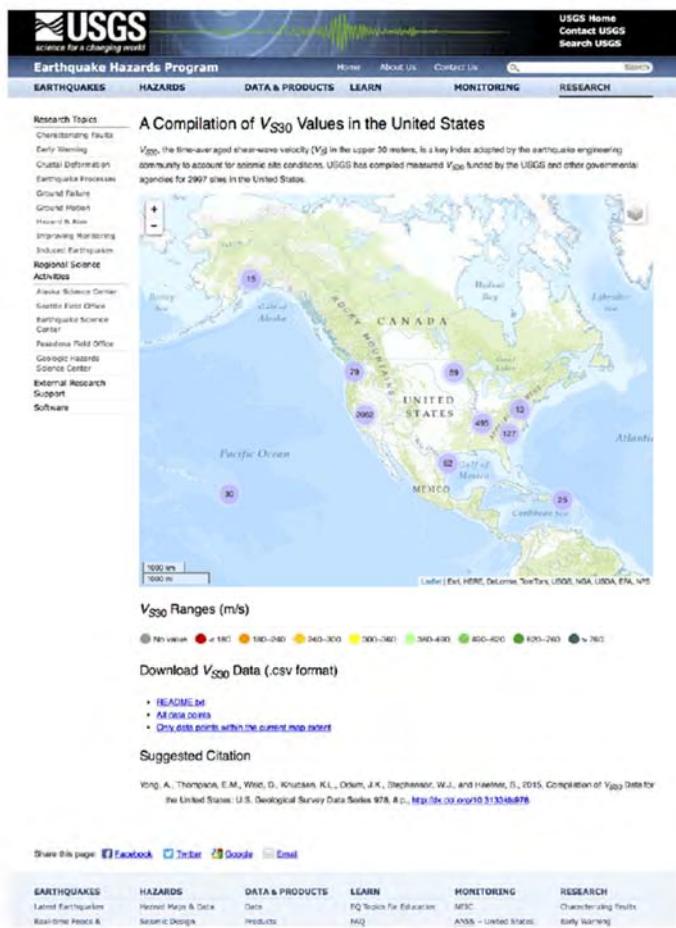


Figure 1. Screenshot of the U.S. Geological Survey Web site for data about V_{s30} (time-averaged shear-wave velocity to a depth of 30 meters; <http://earthquake.usgs.gov/research/vs30/>).

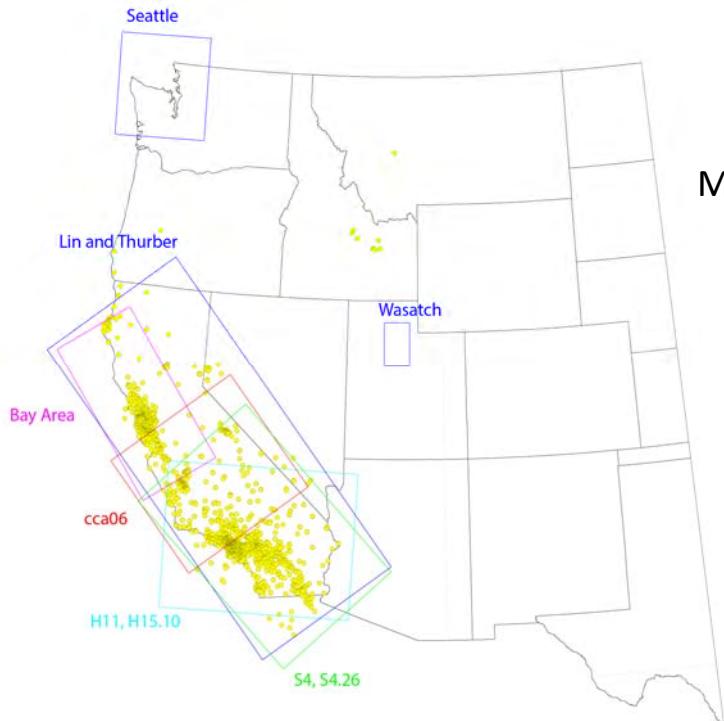
1. Using V_{s30} value from the USGS V_{s30} Database, calculate $Z_{1.0}$ (using CY14 GMM) and $Z_{2.5}$ (using CB14 GMM) for a 0.1 degree grid over the entire WUS.
2. Uniform V_{s30} hazard maps are run using calculated $Z_{1.0}$ and $Z_{2.5}$ values.

Site Class	V_{s30} (m/s)
A	2000
A/B	1500
B	1080
B/C	760
C	530
C/D	365
D	260
D/E	185
E	150

Figure 1 (from Yong *et al.*, 2016)

METHOD 1: LOCAL

Velocity Models
BayArea10 (Aagaard *et al.*, 2010)
S4.26m01 (Lee *et al.*, 2014)
Seattle07 (Stephenson, 2007)
Wasatch08(Magistrale *et al.*, 2008)



Method 1-3

METHOD 2: VS30



METHOD 3: COMPOSITE

Velocity Models
SR16 (national)
SL15 (national)
BayArea10
H15.10
S4
S4.26
S4.26m01
cca06
LinCA10
Seattle07
Wasatch08

Figure 1 (from Yong *et al.*, 2016)

Amplification Factors

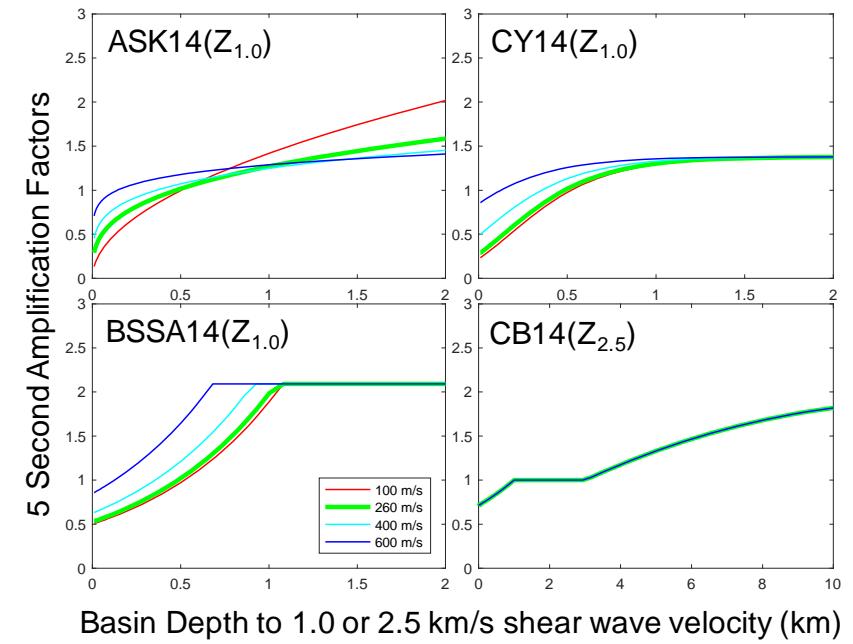
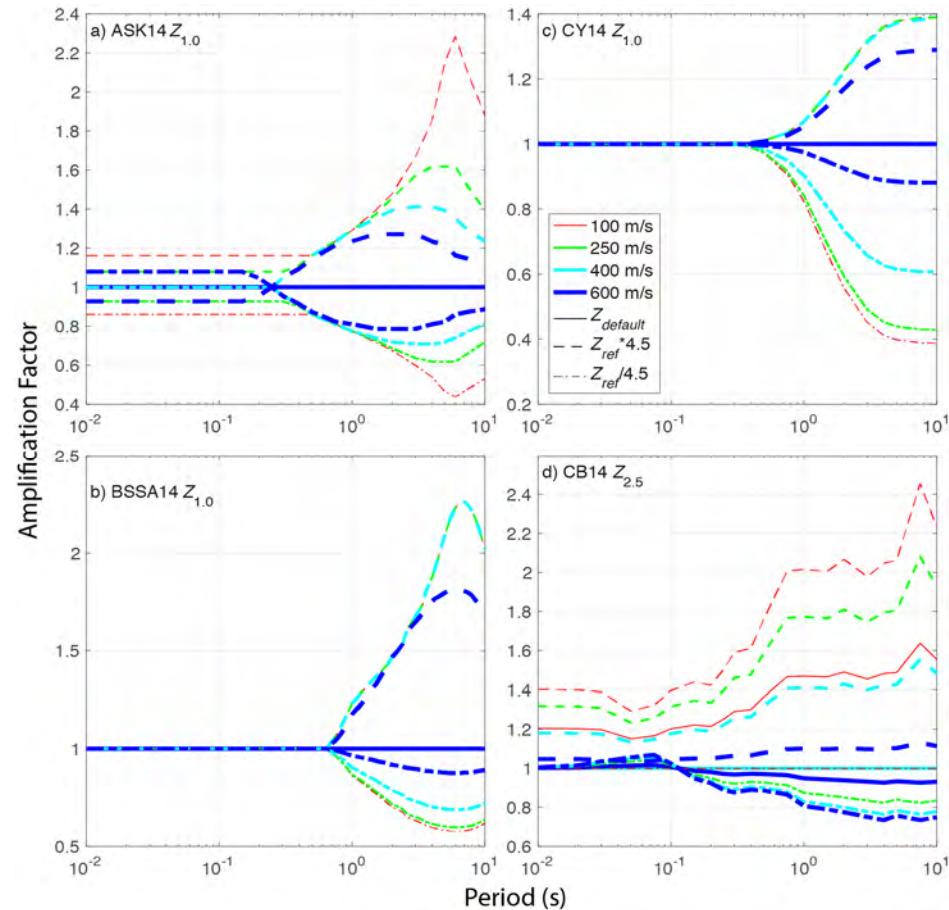
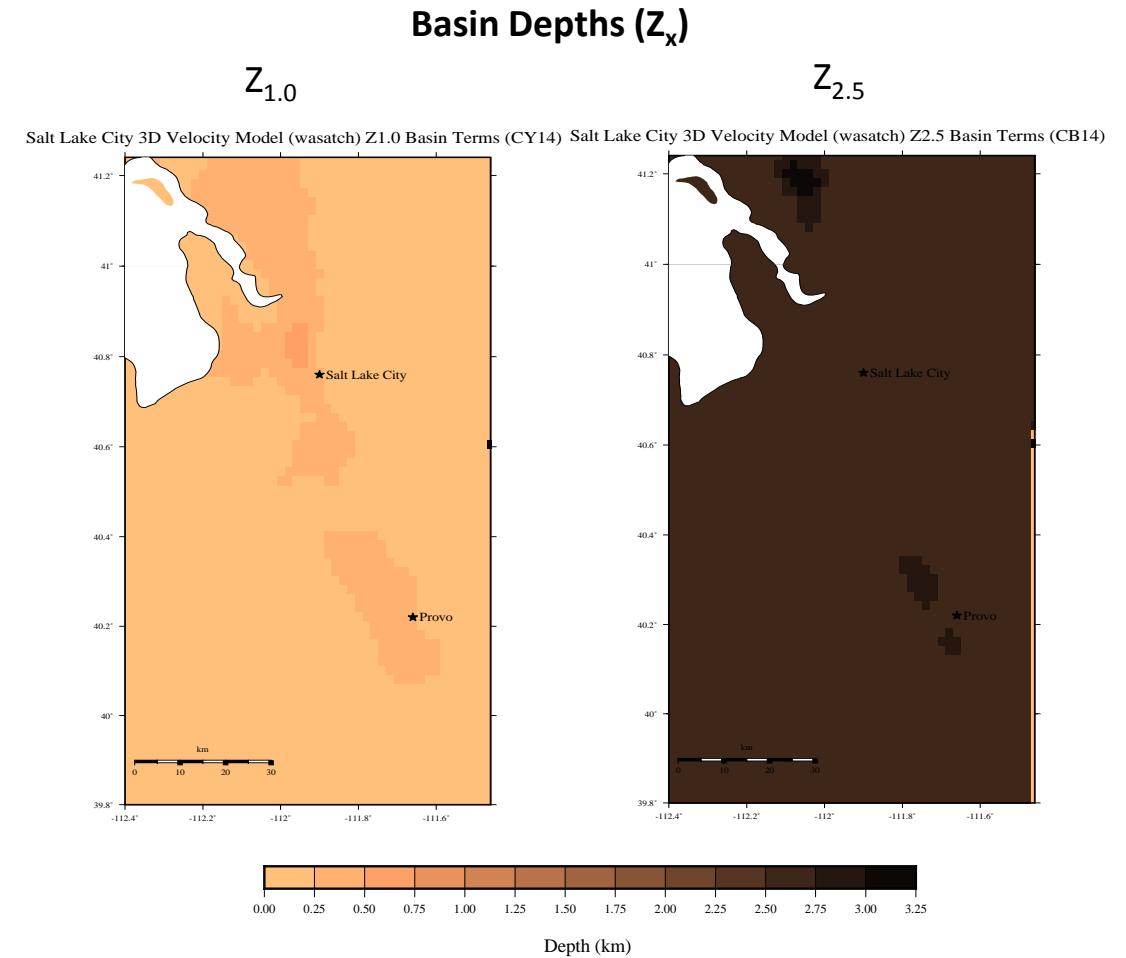
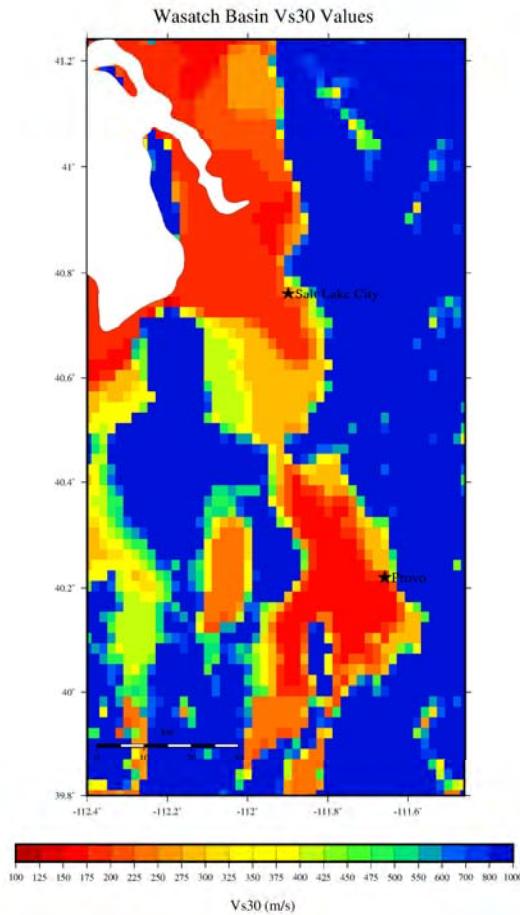


Figure 1 (from Boyd *et al.*, 2018). Amplification factors for the NGA-West2 GMMs used in the 2014 NSHM. The thickest lines are for a V_{S30} of 600 m/s and the thinnest for 100 m/s. Solid lines are for a Z_X value equal to the default value. Dashed lines are for a Z_X value equal to 4.5 times the reference value and dashed-dot lines are for 1/4.5 of the reference value.

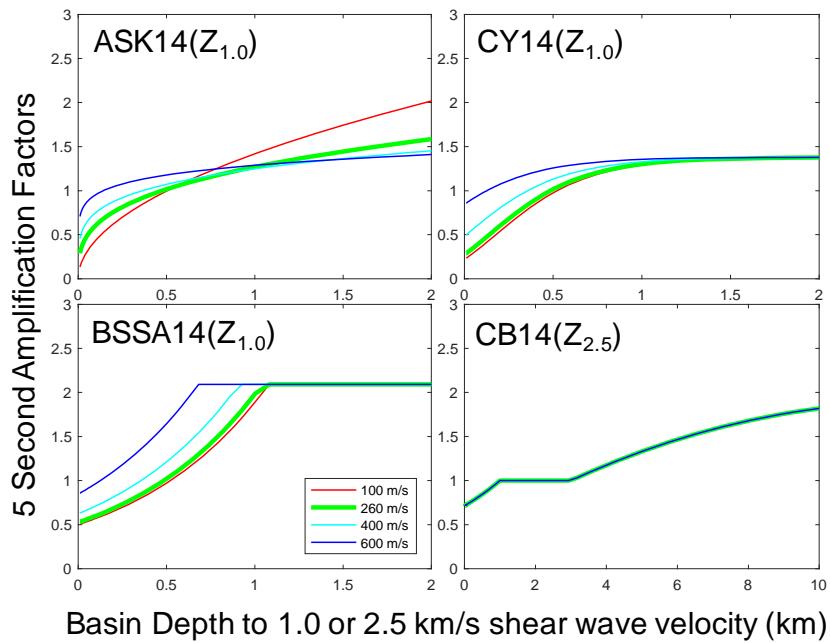
Wasatch Front

Local Seismic Velocity Model*



*Local seismic velocity model is Wasatch08 (Magistrale *et al.*, 2008)

5 Second Amplification Factors from NGA-West2 GMMs

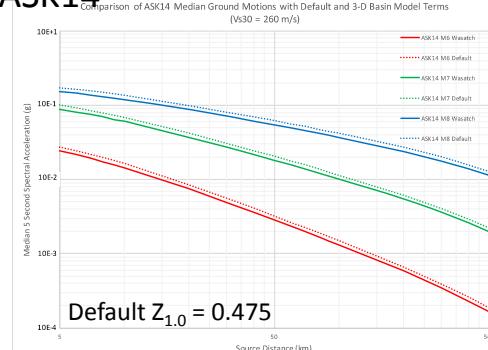


Note: $Z_{1.0}$ is 0.315 km at SLC, therefore, ground motions are deamplified for GMMs that use $Z_{1.0}$. $Z_{2.5}$ is 2.71 km, therefore, CB14 ground motions do not change.

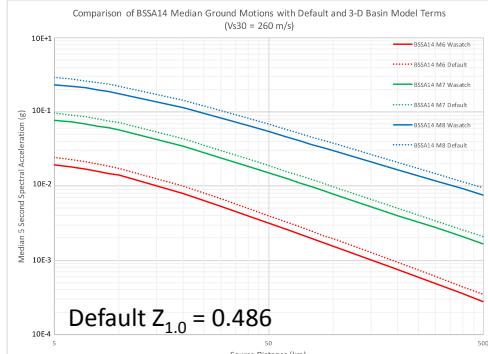
5 Second Median Ground Motions for NGA-West2 GMMs at Salt Lake City, UT (40.76, -111.9), $V_{s30} = 260$ m/s, 2% in 50 Years PE

Local Seismic Velocity Model*: $V_{s30} = 230$ m/s, $Z_{1.0} = 0.315$ km, $Z_{2.5} = 2.71$ km

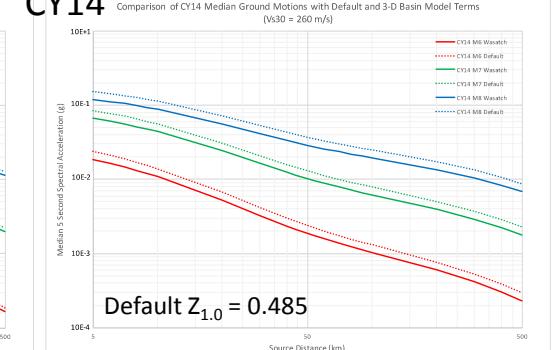
ASK14



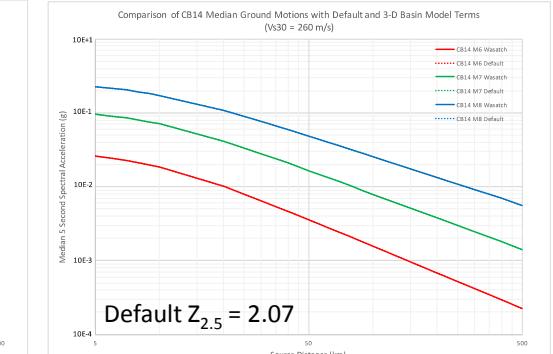
BSSA14



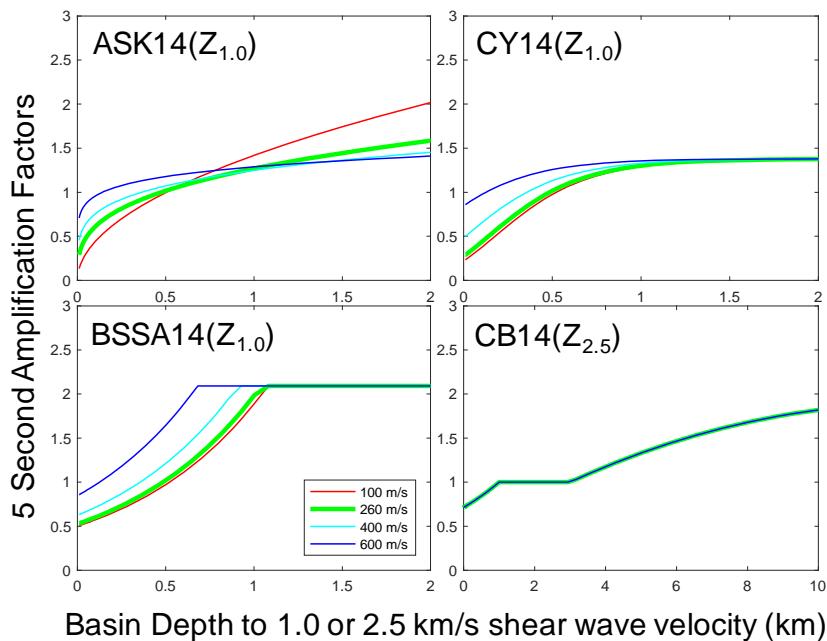
CY14



CB14



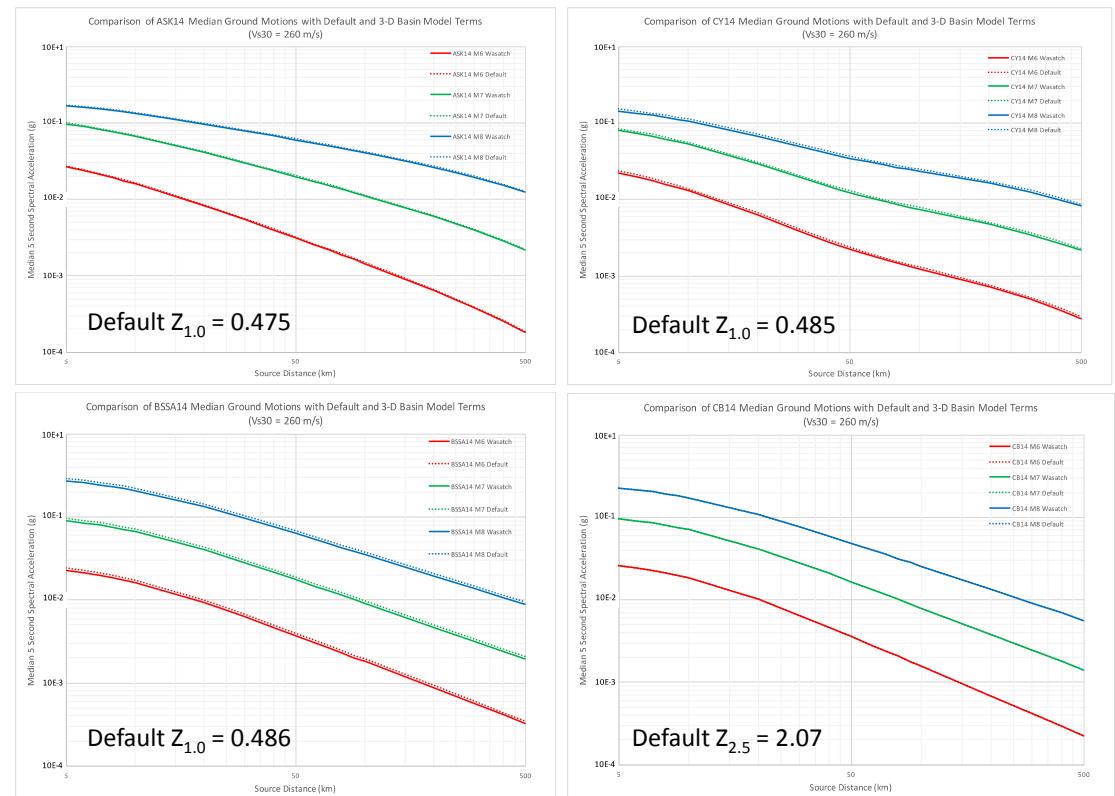
5 Second Amplification Factors from NGA-West2 GMMs

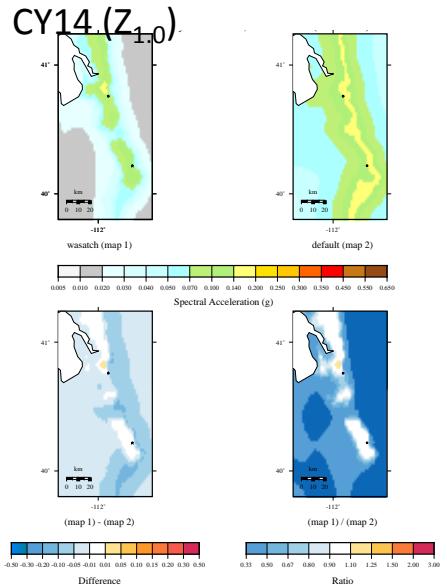
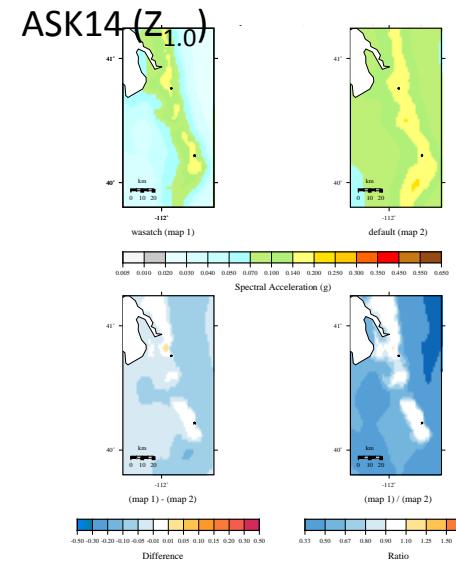


Note: $Z_{1.0}$ is 0.434 km at Provo, therefore, ground motions are deamplified for GMMs that use $Z_{1.0}$. $Z_{2.5}$ is 2.71 km, therefore, CB14 ground motions do not change.

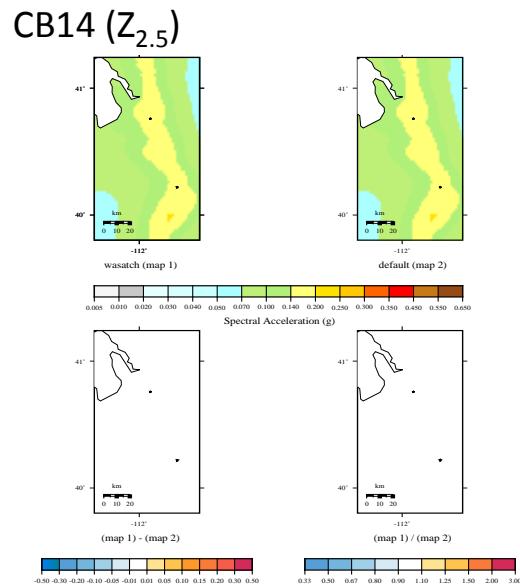
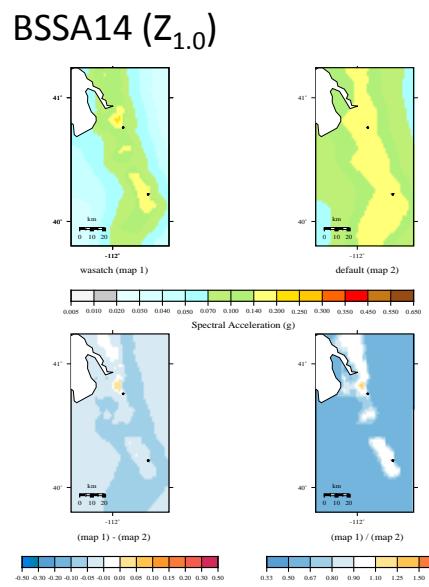
5 Second Median Ground Motions for NGA-West2 GMMs at Provo, UT (40.22, -111.66), $V_{s30} = 260$ m/s, 2% in 50 Years PE

Local Seismic Velocity Model*: $V_{s30} = 186$ m/s, $Z_{1.0} = 0.434$ km, $Z_{2.5} = 2.71$ km





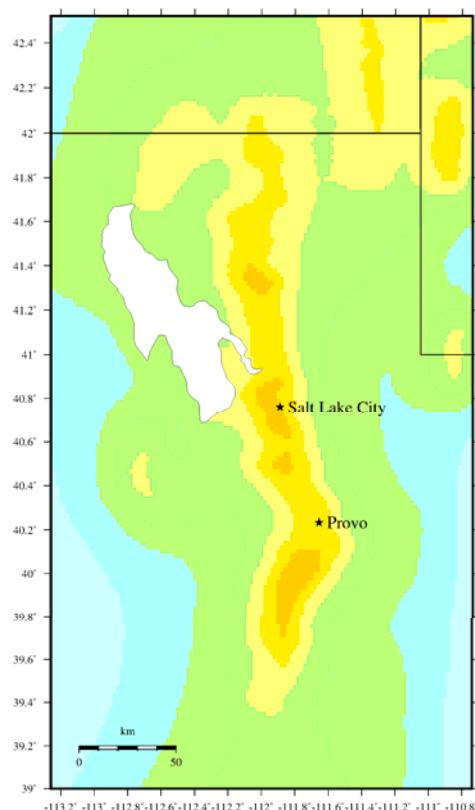
5 Second Hazard from NGA-West2 GMMs, 2% $V_{S30} = 260 \text{ m/s}, 2\% \text{ in 50 Years PE}$



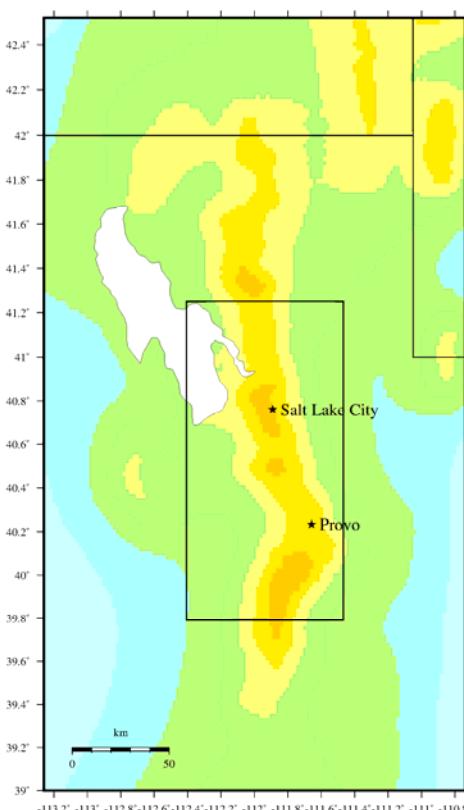
Comparison of PGA Total Mean Hazard

$V_{s30} = 760 \text{ m/s}$, 2% in 50 Years PE

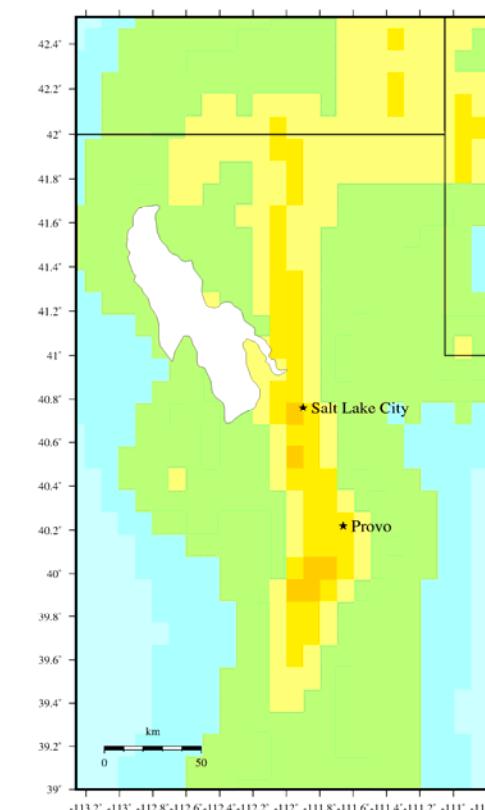
Default



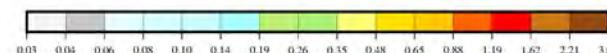
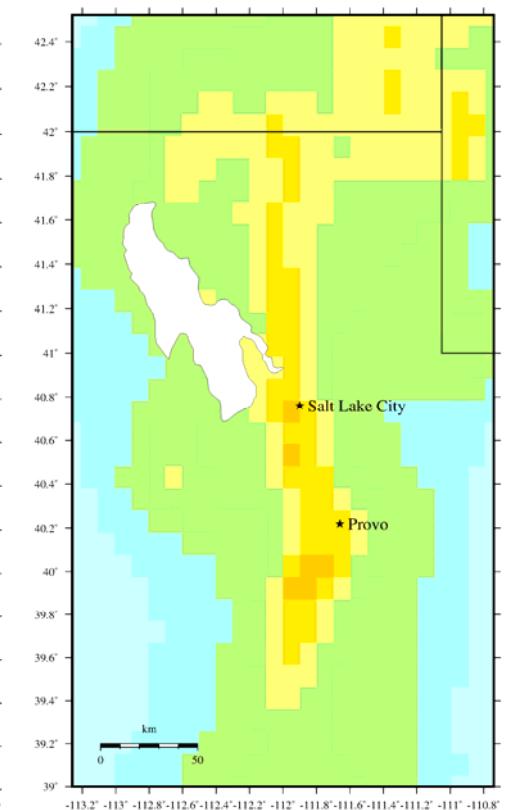
Local*



V_{s30}



Composite



Note: Black box is boundary of basin depths (Z_x terms) calculated from local seismic velocity model.

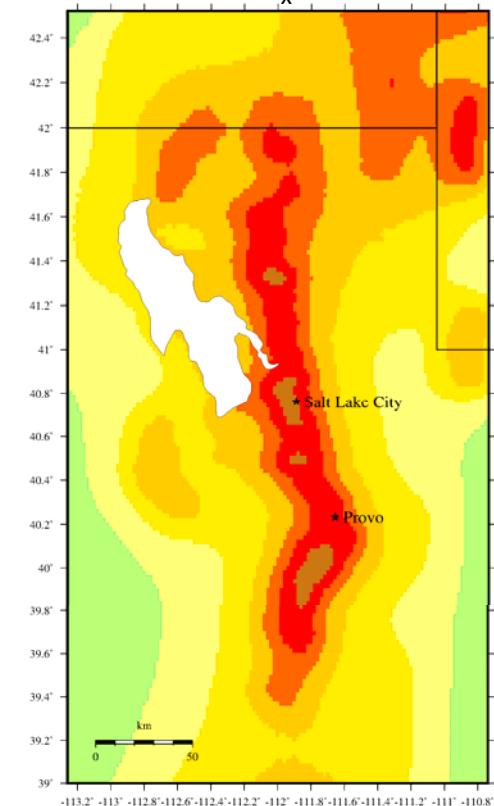
Peak Ground Acceleration (g)

*Local seismic velocity model is Wasatch08 (Magistrale *et al.*, 2008)

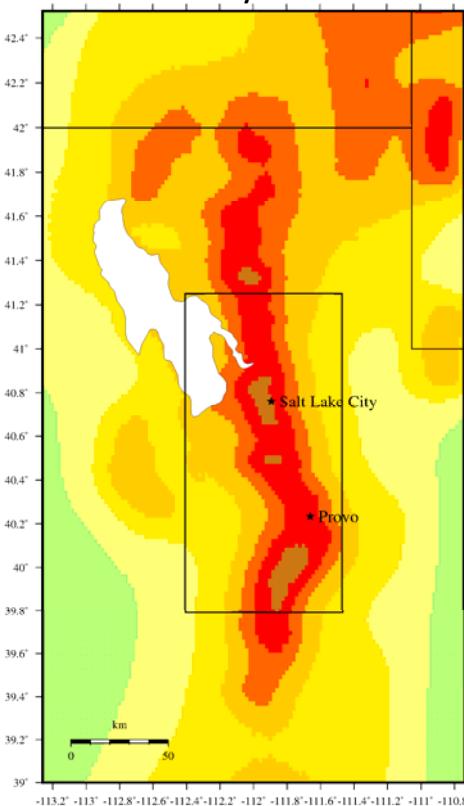
Comparison of 0.2 Second Total Mean Hazard

$V_{s30} = 760 \text{ m/s}, 2\% \text{ in 50 Years PE}$

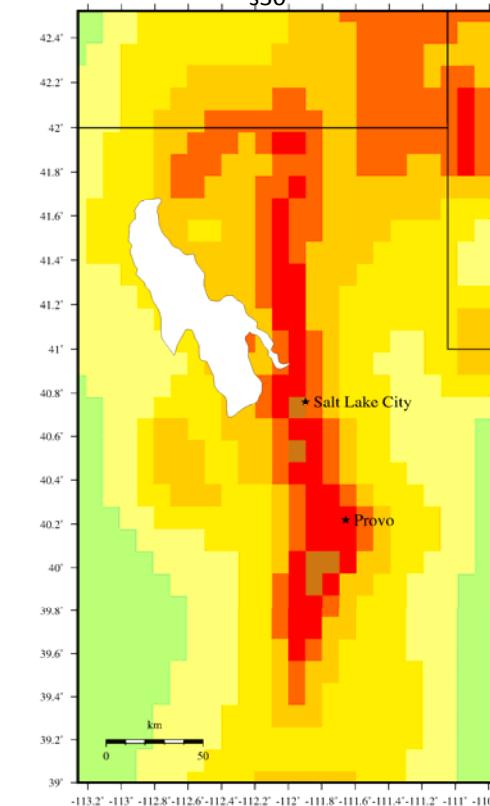
Default Z_x Terms



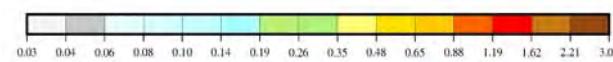
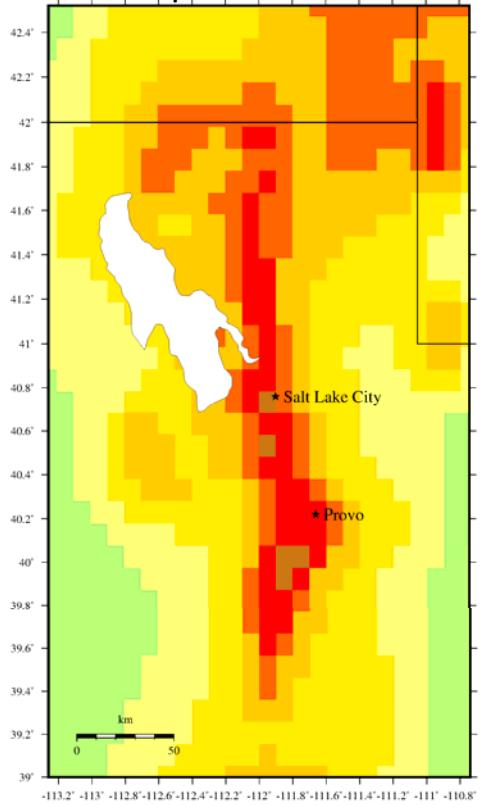
Z_x Terms from Local Seismic Velocity Model*



Z_x Terms Calculated from USGS V_{s30} Database



Z_x Terms from Composite Model



Note: Black box is boundary of basin depths (Z_x terms) calculated from local seismic velocity model.

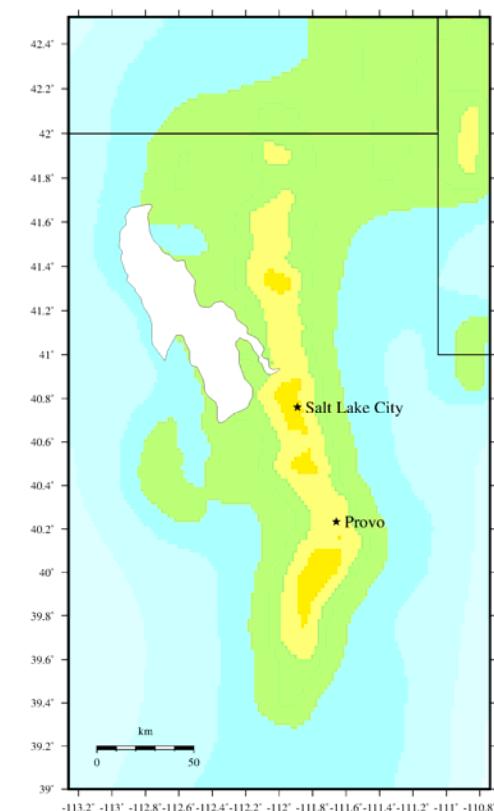
0.2 Second Spectral Acceleration (g)

*Local seismic velocity model is Wasatch08 (Magistrale *et al.*, 2008)

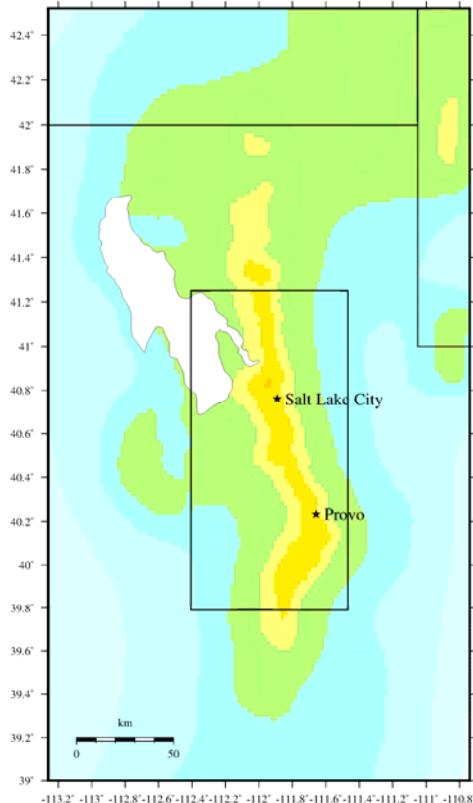
Comparison of 1 Second Total Mean Hazard

$V_{s30} = 760 \text{ m/s}, 2\% \text{ in 50 Years PE}$

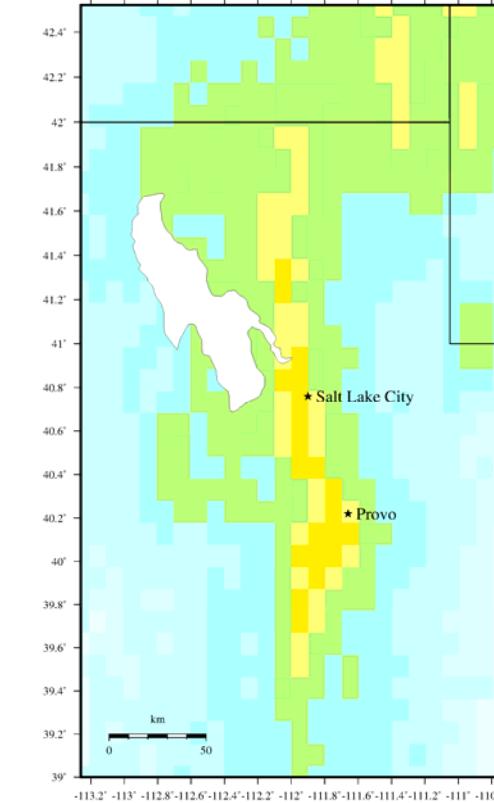
Default Z_x Terms



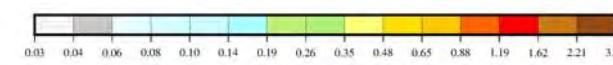
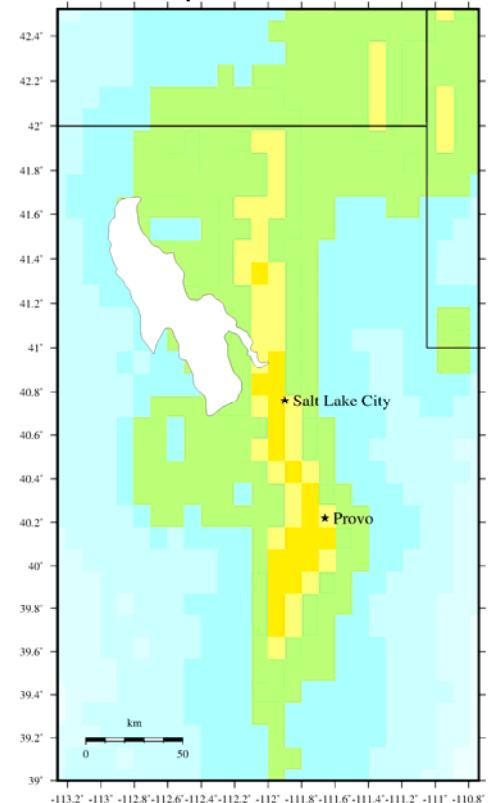
Z_x Terms from Local Seismic Velocity Model*



Z_x Terms Calculated from USGS V_{s30} Database



Z_x Terms from Composite Model



Note: Black box is boundary of basin depths (Z_x terms) calculated from local seismic velocity model.

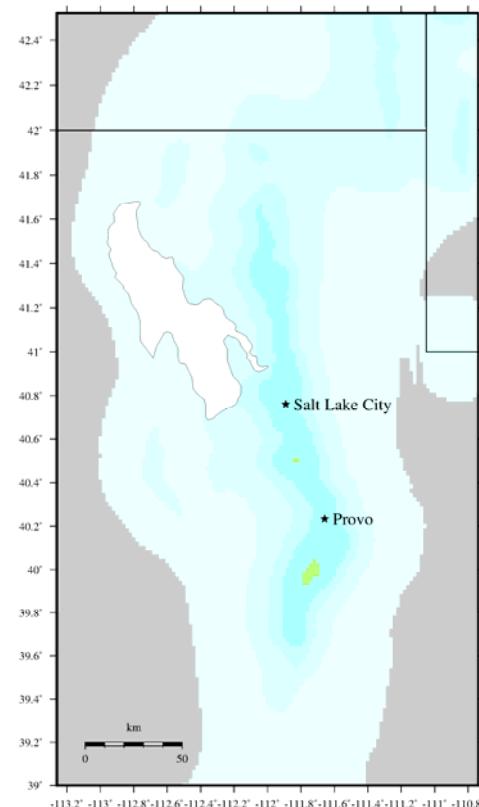
1 Second Spectral Acceleration (g)

*Local seismic velocity model is Wasatch08 (Magistrale *et al.*, 2008)

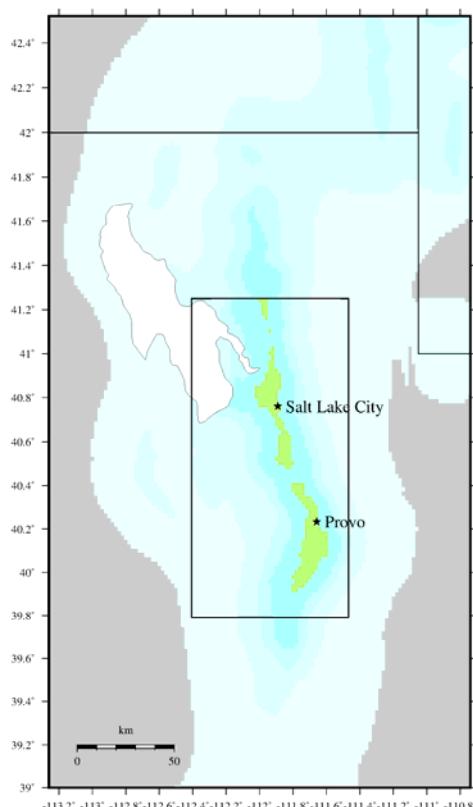
Comparison of 5 Second Total Mean Hazard

$V_{s30} = 760 \text{ m/s}$, 2% in 50 Years PE

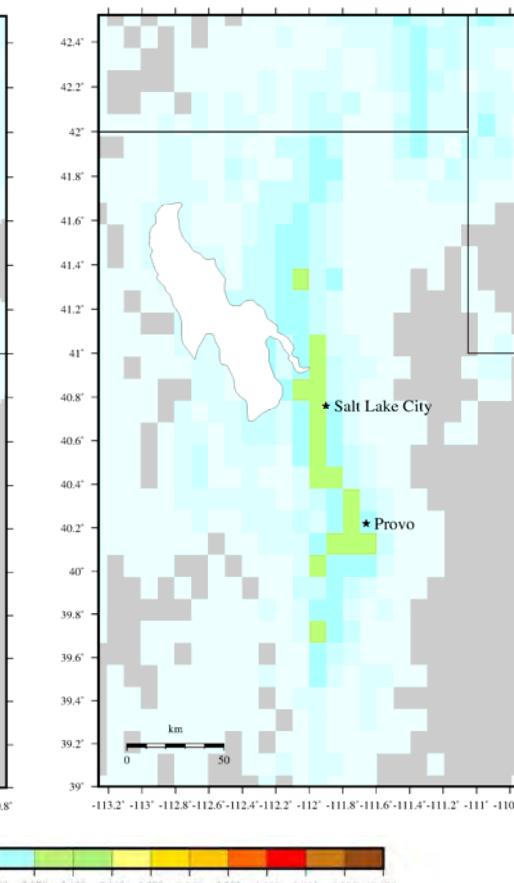
Default



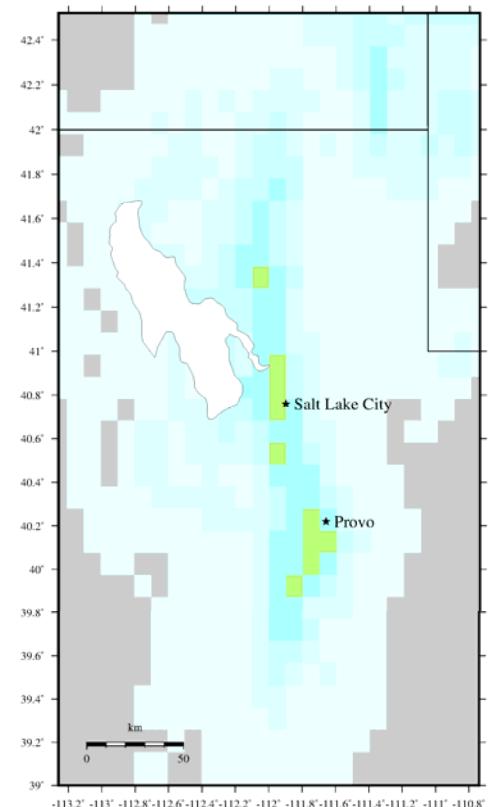
Local*



V_{s30}



Composite



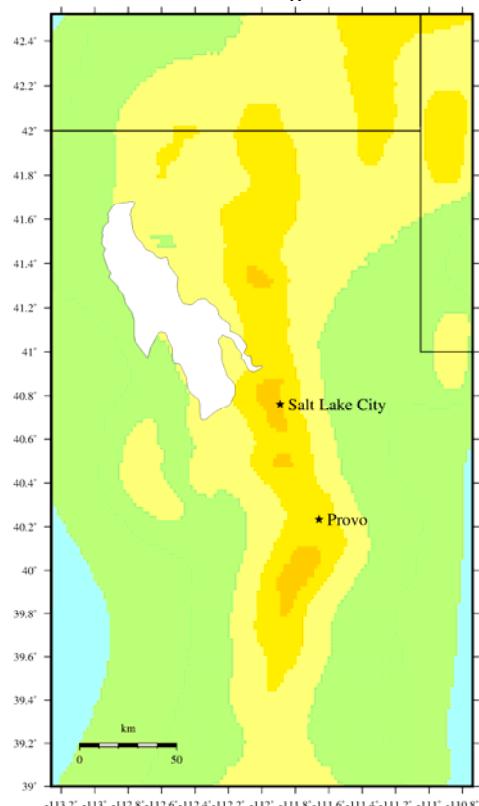
*Local seismic velocity model is Wasatch08 (Magistrale *et al.*, 2008)

5 Second Spectral Acceleration (g)

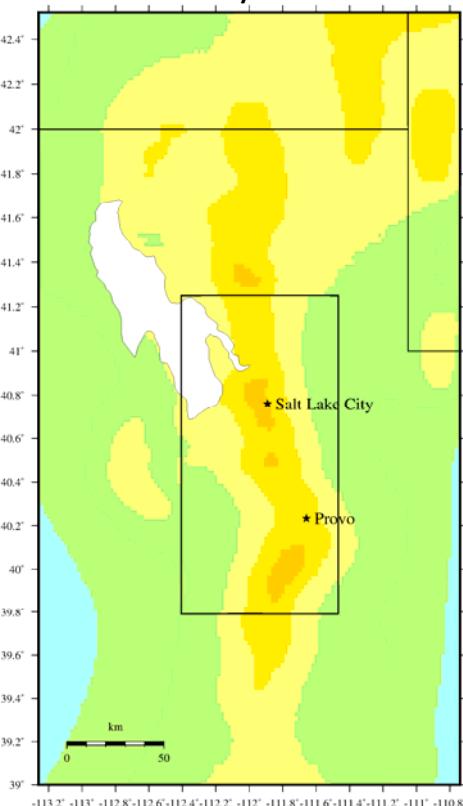
Comparison of PGA Total Mean Hazard

$V_{s30} = 260 \text{ m/s}, 2\% \text{ in 50 Years PE}$

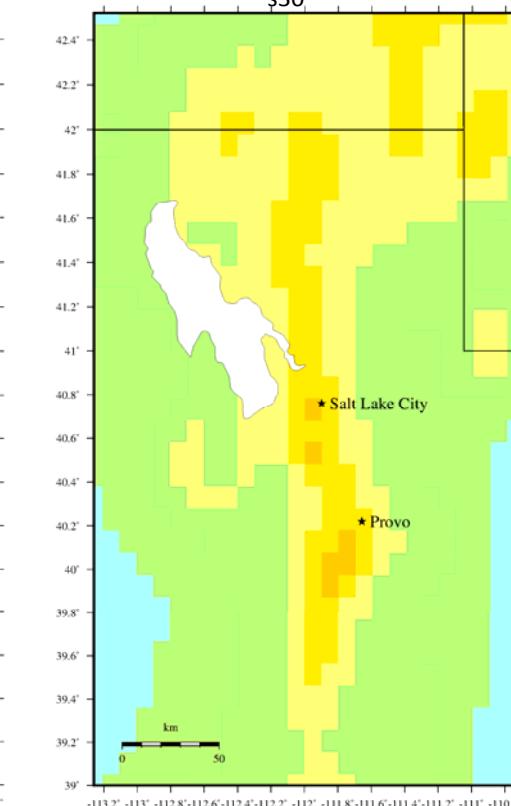
Default Z_x Terms



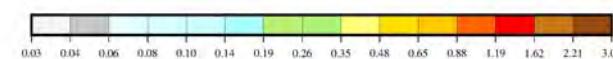
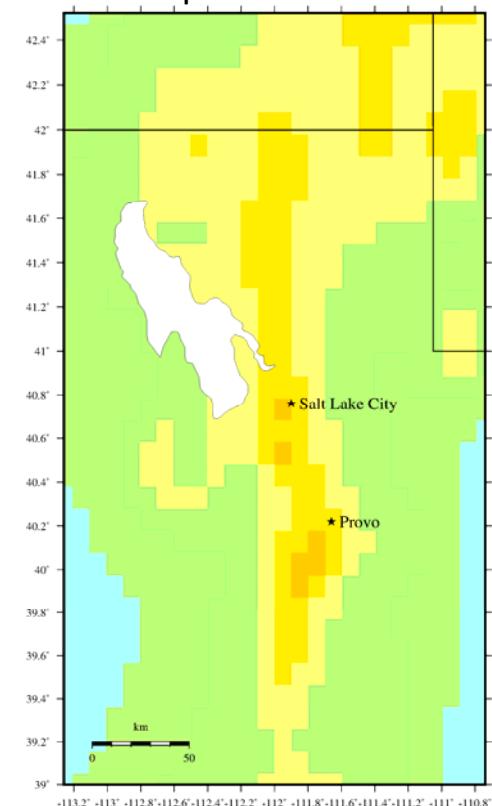
Z_x Terms from Local Seismic Velocity Model*



Z_x Terms Calculated from USGS V_{s30} Database



Z_x Terms from Composite Model



Note: Black box is boundary of basin depths (Z_x terms) calculated from local seismic velocity model.

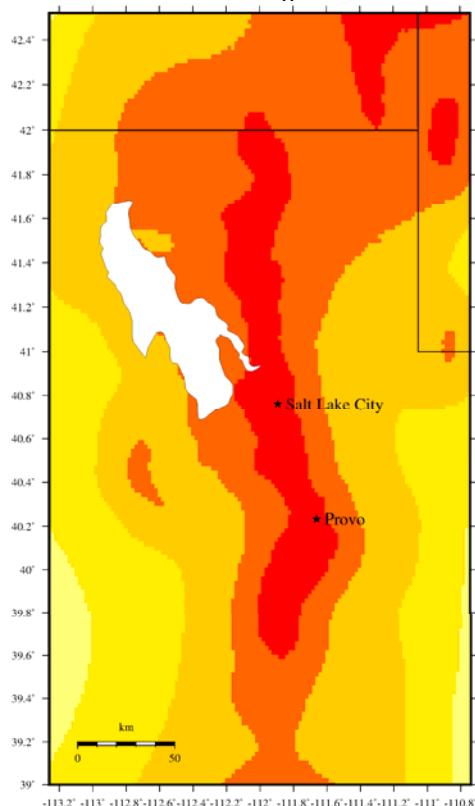
Peak Ground Acceleration (g)

*Local seismic velocity model is Wasatch08 (Magistrale *et al.*, 2008)

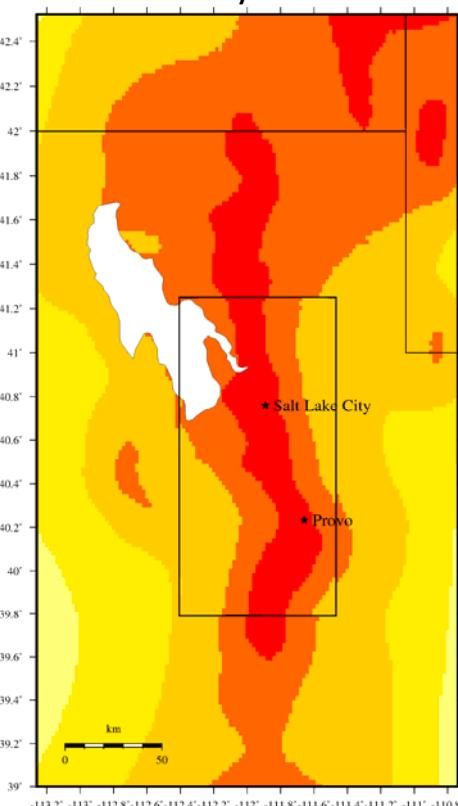
Comparison of 0.2 Second Total Mean Hazard

$V_{s30} = 260 \text{ m/s}$, 2% in 50 Years PE

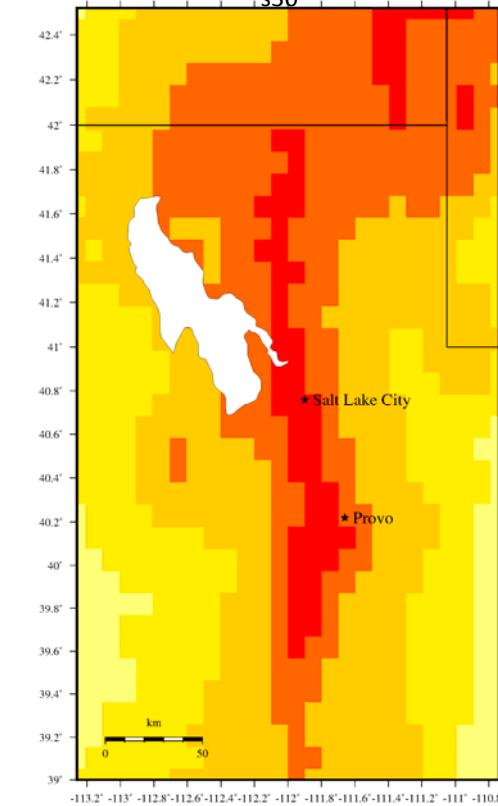
Default Z_x Terms



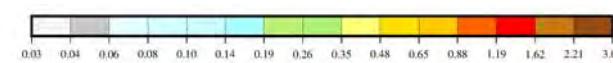
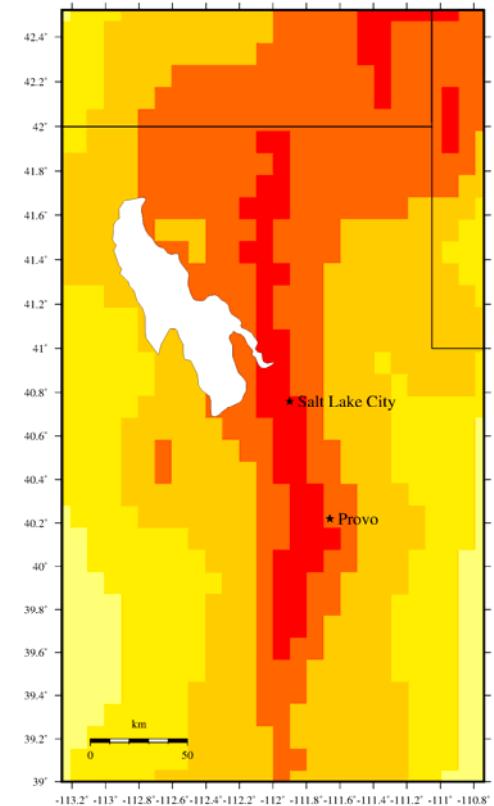
Z_x Terms from Local Seismic Velocity Model*



Z_x Terms Calculated from USGS V_{s30} Database



Z_x Terms from Composite Model



Note: Black box is boundary of basin depths (Z_x terms) calculated from local seismic velocity model.

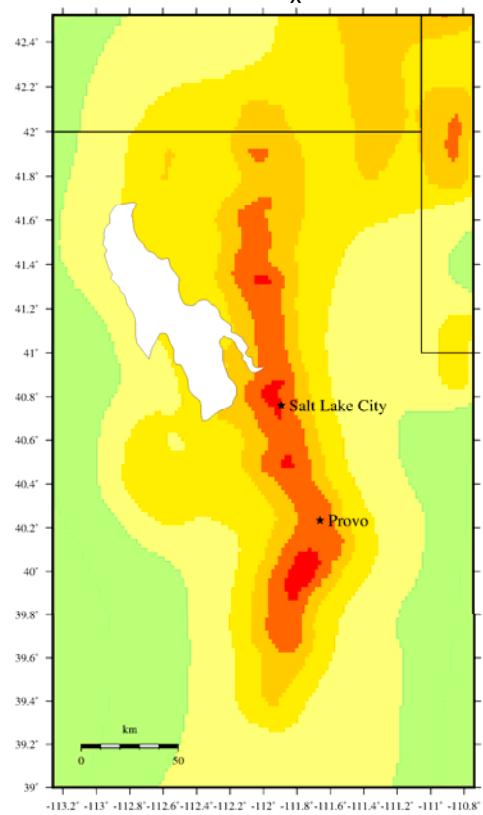
0.2 Second Spectral Acceleration (g)

*Local seismic velocity model is Wasatch08 (Magistrale *et al.*, 2008)

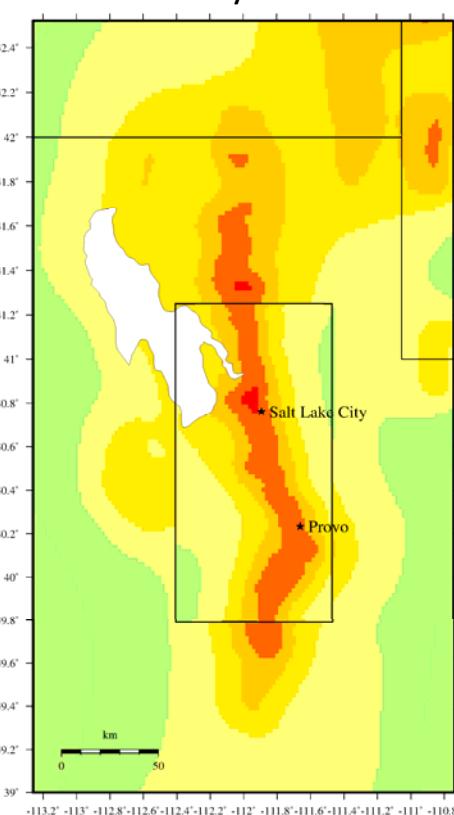
Comparison of 1 Second Total Mean Hazard

$V_{s30} = 260 \text{ m/s}, 2\% \text{ in 50 Years PE}$

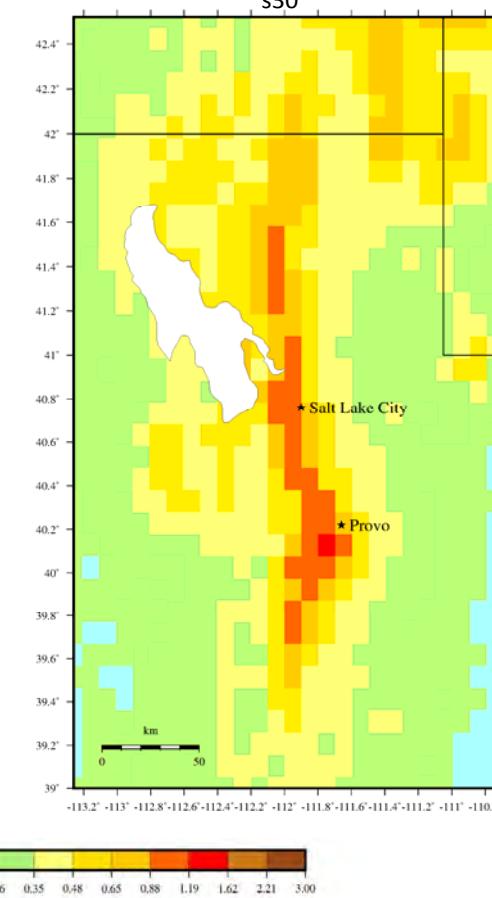
Default Z_x Terms



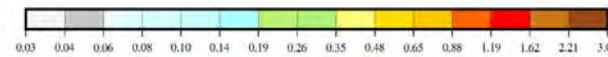
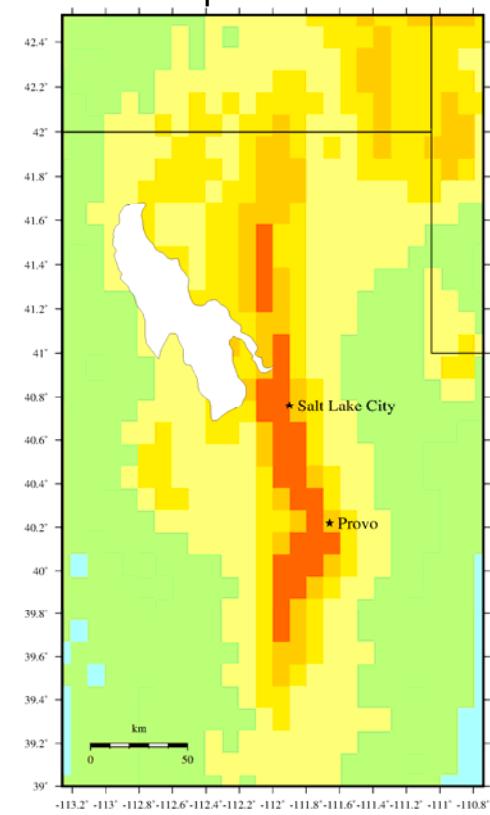
Z_x Terms from Local Seismic Velocity Model*



Z_x Terms Calculated from USGS V_{s30} Database



Z_x Terms from Composite Model



Note: Black box is boundary of basin depths (Z_x terms) calculated from local seismic velocity model.

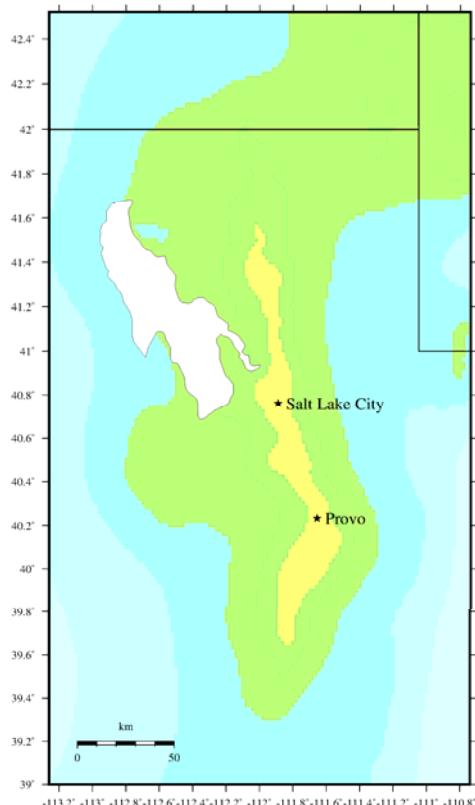
1 Second Spectral Acceleration (g)

*Local seismic velocity model is Wasatch08 (Magistrale *et al.*, 2008)

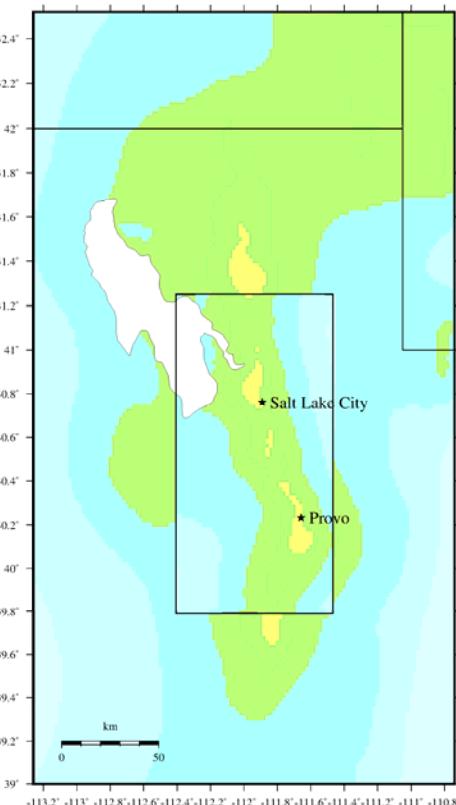
Comparison of 5 Second Total Mean Hazard

$V_{s30} = 260 \text{ m/s}, 2\% \text{ in 50 Years PE}$

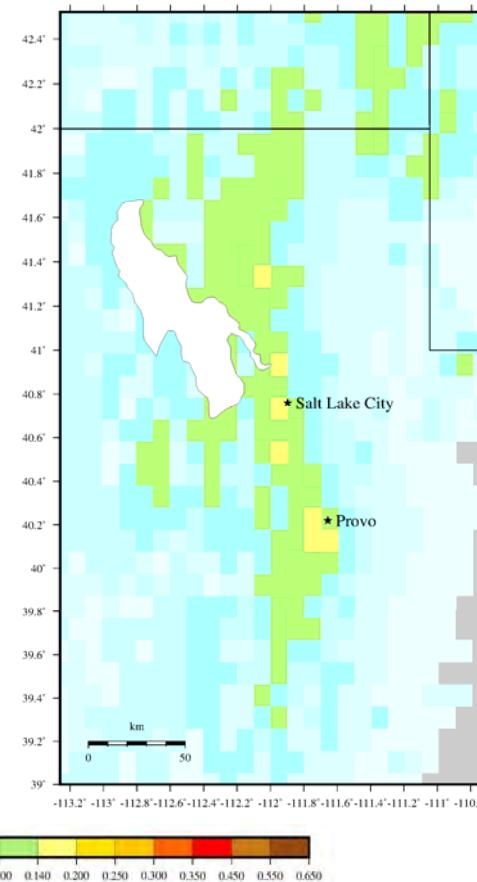
Default



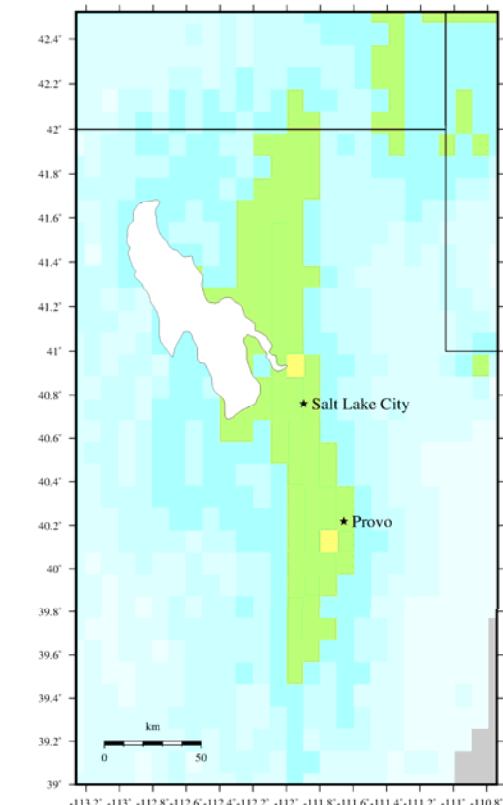
Local*



V_{s30}



Composite

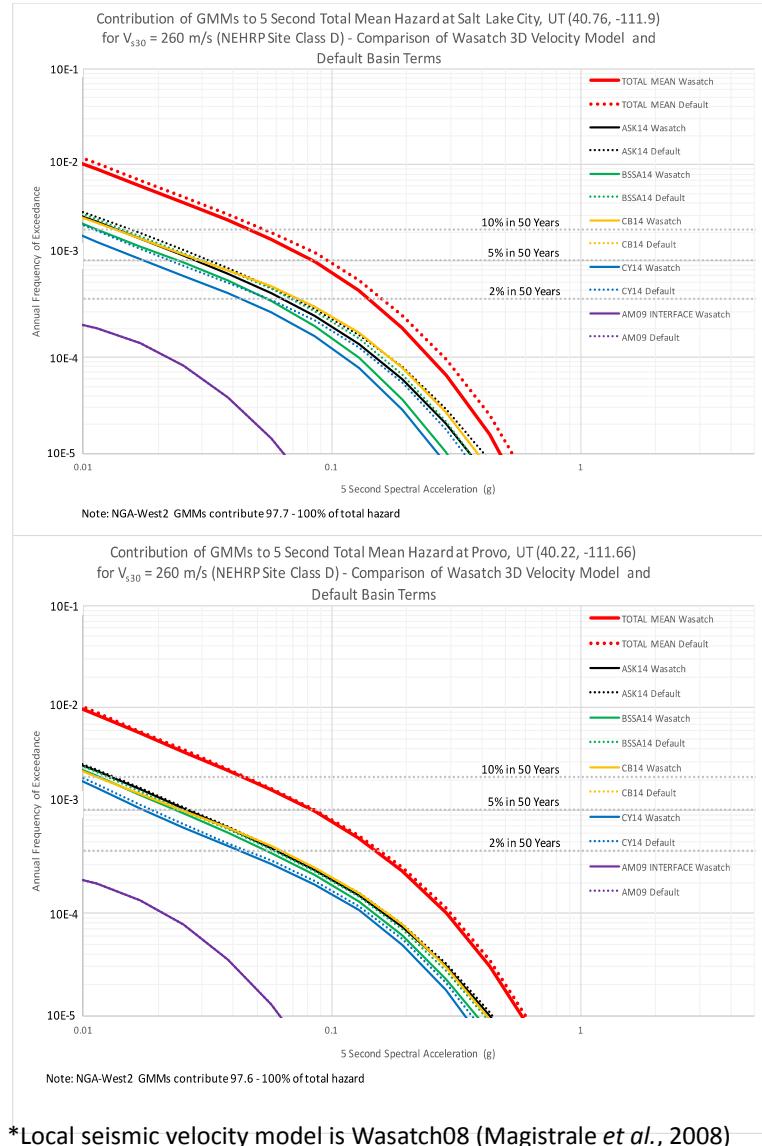
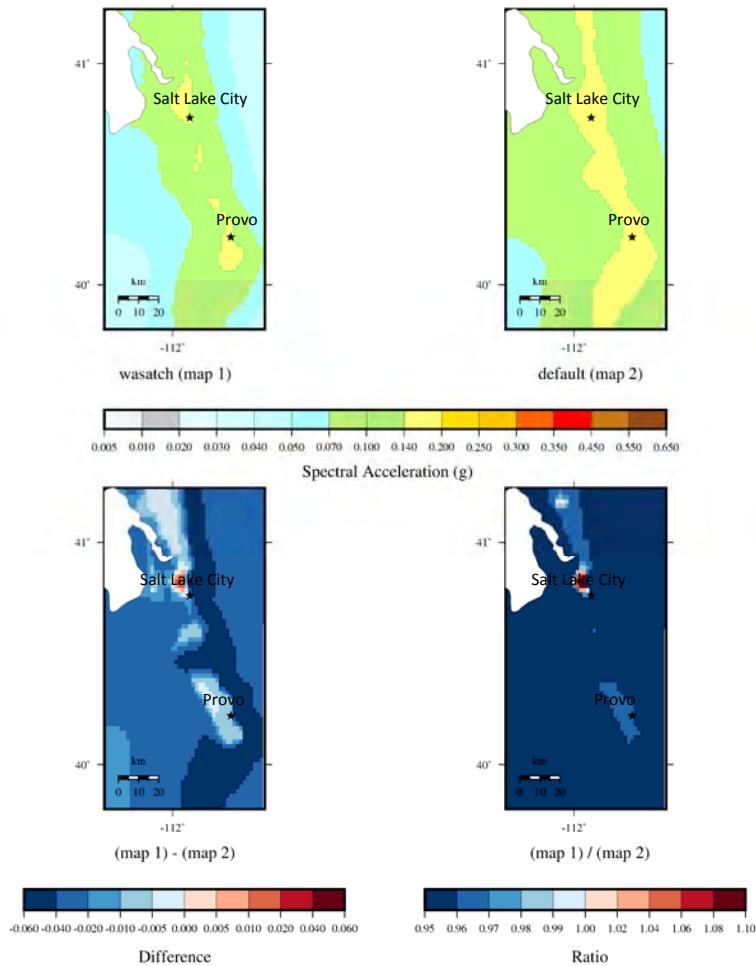


0.005 0.010 0.020 0.030 0.040 0.050 0.070
0.100 0.140 0.200 0.250 0.300 0.350 0.450 0.550 0.650
5 Second Spectral Acceleration (g)

*Local seismic velocity model is Wasatch08 (Magistrale *et al.*, 2008)

5 Second Spectral Acceleration (g)

**5 Second Total Mean Hazard,
 $V_{s30} = 260$ m/s, 2% in 50 Years PE**
Local* vs. Default

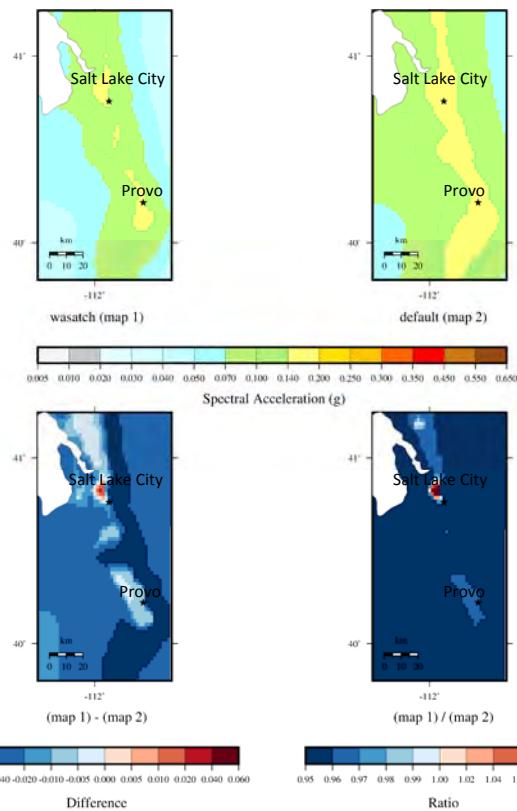


*Local seismic velocity model is Wasatch08 (Magistrale *et al.*, 2008)

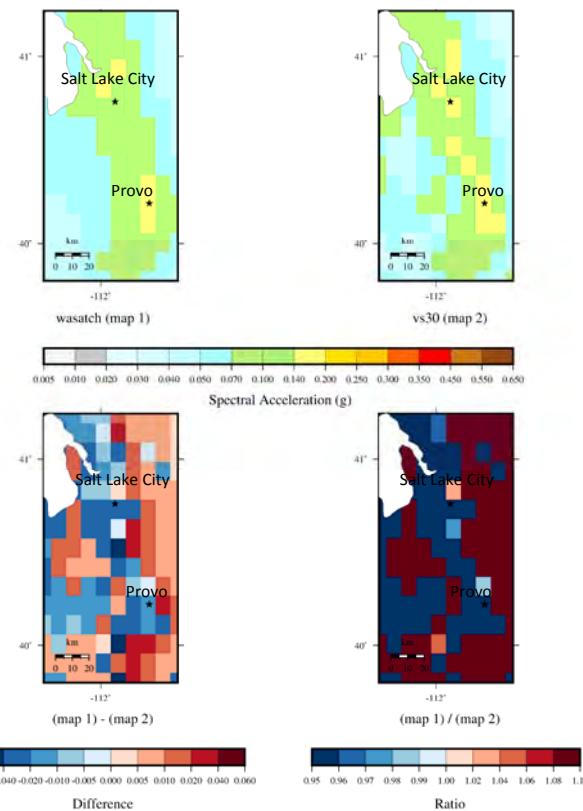
5 Second Total Mean Hazard

$V_{s30} = 260 \text{ m/s}$, 2% in 50 Years PE

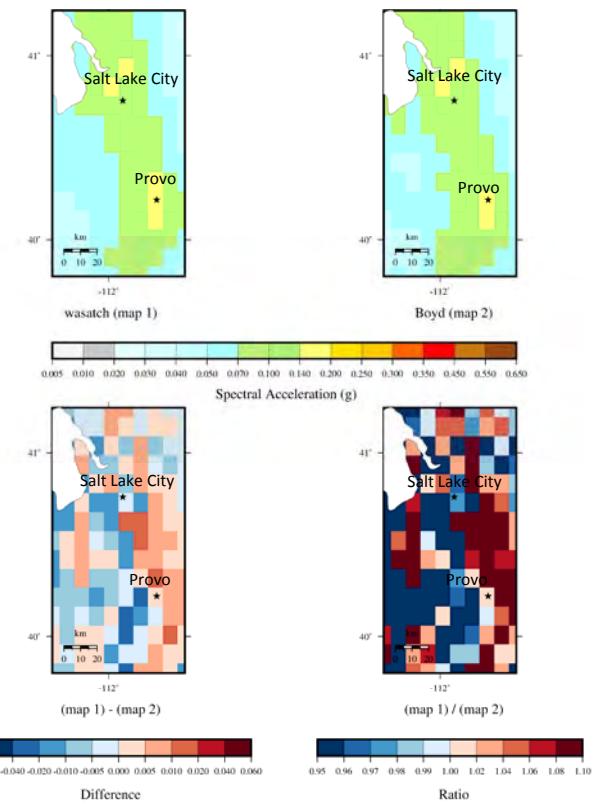
Local* vs. Default



Local* vs. V_{s30}

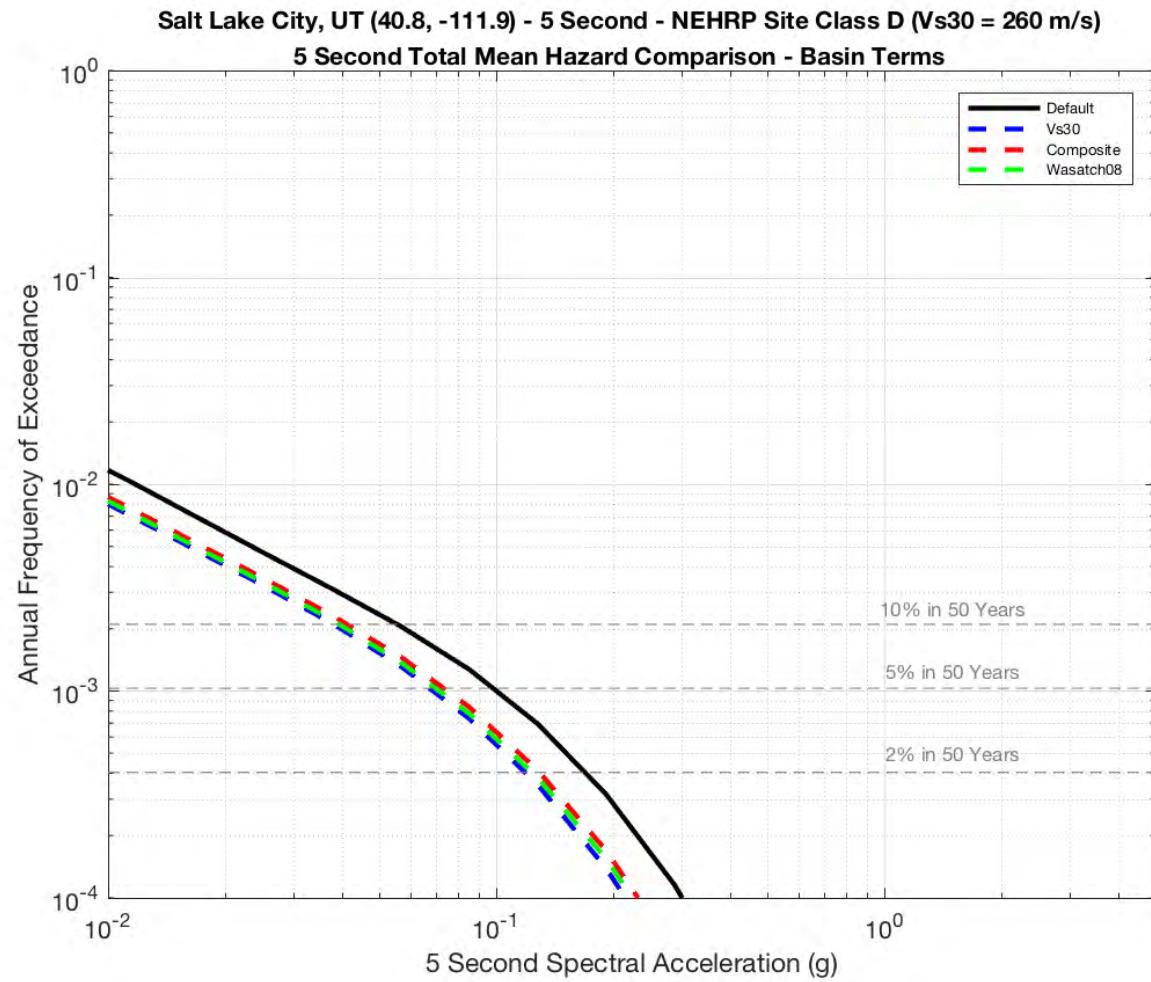


Local* vs. Composite

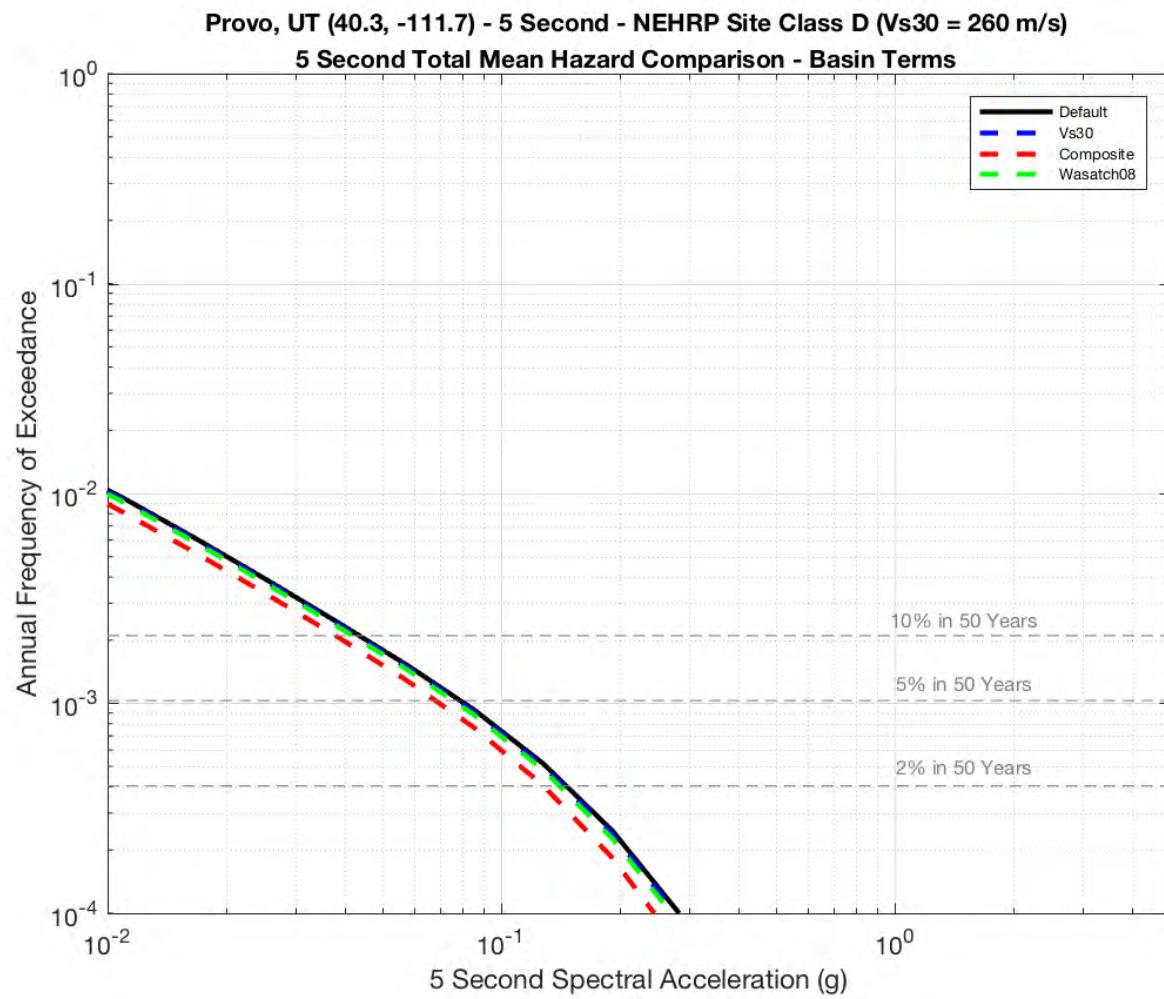


*Local seismic velocity model is Wasatch08 (Magistrale *et al.*, 2008)

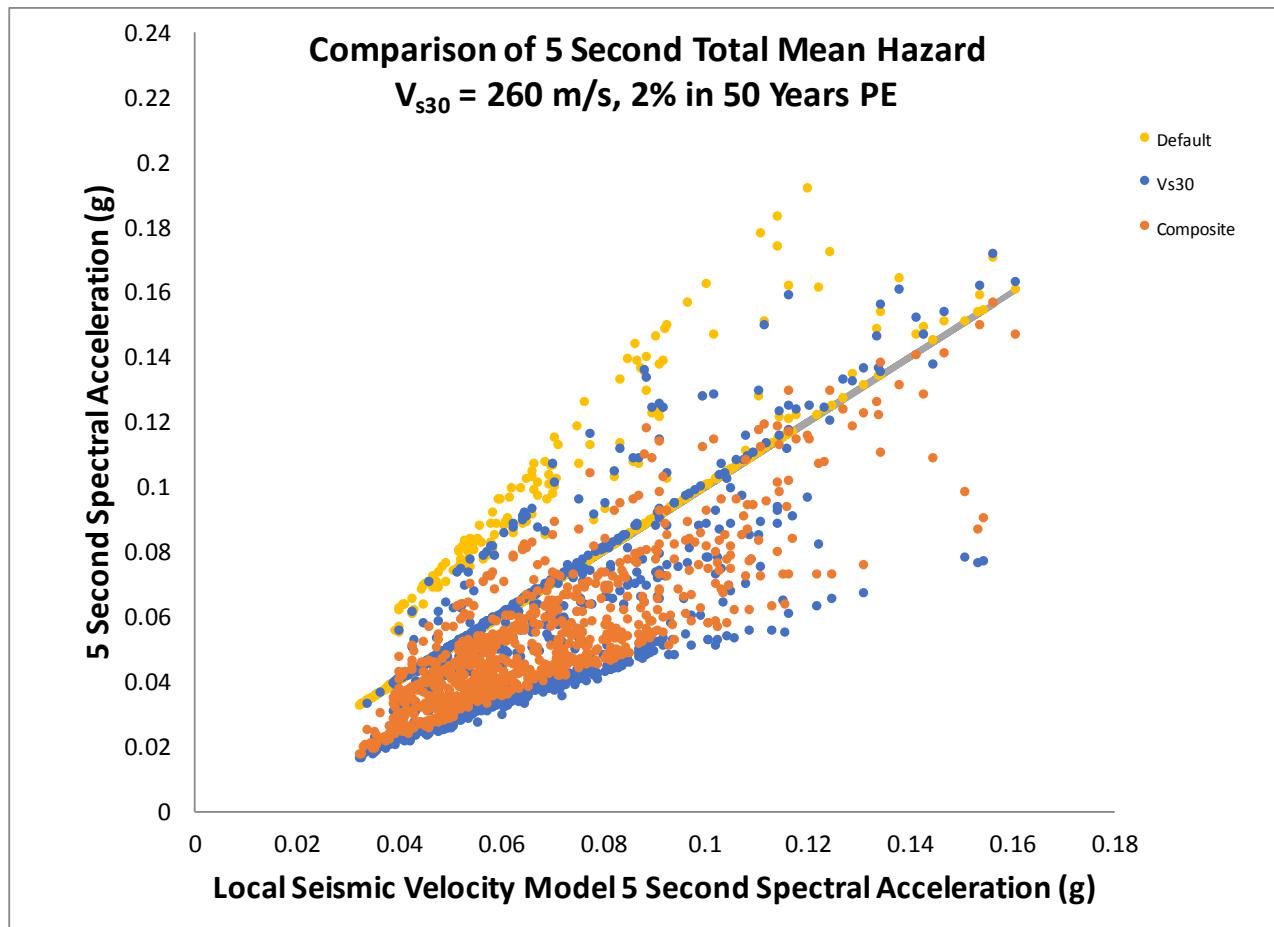
Hazard Curve Comparisons: Salt Lake City, UT



Hazard Curve Comparisons: Provo, UT

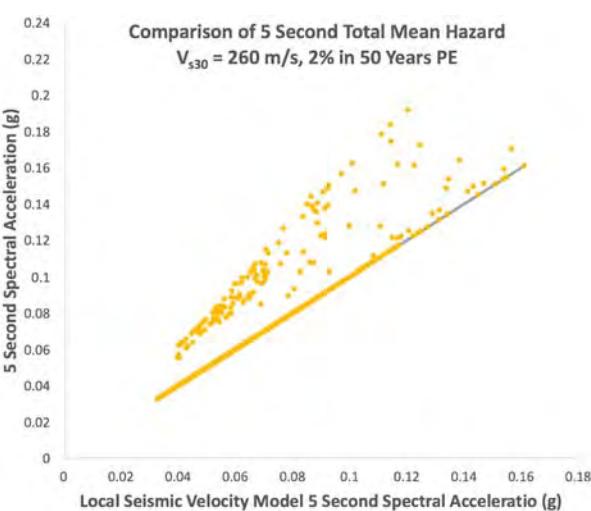


Summary Correlation Plot

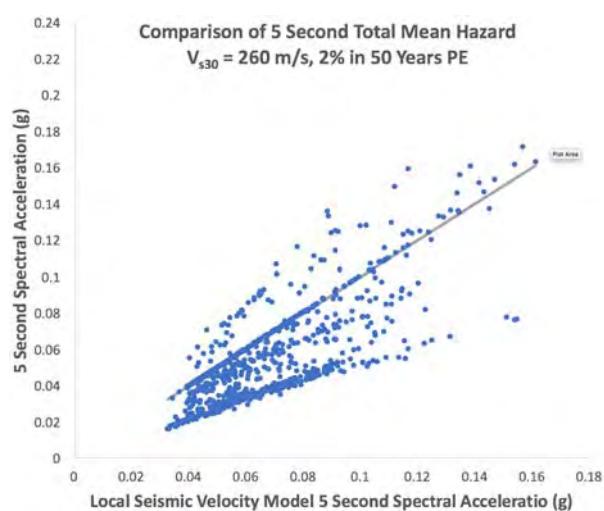


Individual Correlation Plots

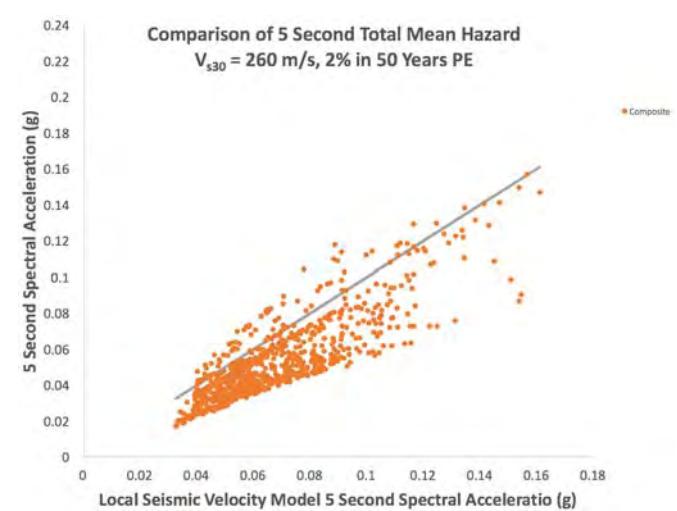
Default



V_{s30}



Composite



Correlation Coefficient = 0.90

Correlation Coefficient = 0.76

Correlation Coefficient = 0.85

A User's Perspective

How structural engineers use ground motions for building design.

By Eric Hoffman, PE



Proof of my qualifications-



ASCE 7-10 Seismic Design Process

Step 1 - Use the USGS website application to get risk-modified ground motion parameters, S_s and S_1 (MCE_R).

Step 2 - Modify MCE_R parameters for soil effects (Site Class A-F).

Step 3 - Multiply site-modified MCE_R ground motions parameters by 2/3 to get design spectral acceleration parameters (S_{DS} and S_{D1}).

Step 4 - Divide S_{DS} and S_{D1} by the ductility factor R to calculate the seismic response coefficient, C_s .

Step 5 - Multiply the building's weight by C_s to get the design Base Shear.

Step 6 - Distribute the base shear vertically to each level using the Equivalent Lateral Force procedure (ELF).

Step 7 – Analyze how the forces distribute through the diaphragms, shear walls, braces and frames.

Step 8 – For allowable stress design (ASD) reduce the force by a factor of 0.7.

Step 9 – Verify that the ASD design forces do not exceed the allowable capacities for each element.

Step 10 – Check building deflections/drifts.

Design Example – Ensign Engineering's Office Building

- 45 West 10000 South, Sandy, UT
- 5 Story Steel Moment Frame Office Building
- Assume Site Class D
- Height = 68 ft
- Approx. Period = 0.82s



Step 1 - 3 -

Use the USGS website application to find risk-reduced ground motion parameters, S_s and S_1 (MCE_R).

Secure | <https://earthquake.usgs.gov/designmaps/us/application.php>

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U.S. Seismic Design Maps

For seismic design parameter values from the 2015 NEHRP Recommended Seismic Provisions, which are being adopted into the 2016 ASCE 7 Standard and the 2018 International Building Code, please see the [Beta version of the U.S. Seismic Design Maps application](#).

Within the 2013 ASCE 41 design code reference document option of this web tool, the "Custom" earthquake hazard level option is no longer available. However, outside of this tool, a USGS web service that includes the "Custom" option is now available [here](#).

Application **Batch Mode** **Help**

Design Code Reference Document
Consult your local design official if you need help selecting this.
2009 NEHRP

Report Title (Optional)
This will appear at the top of the generated report.
Ensign Office Building

Site Soil Classification
This is not automatically selected based on site location.
Site Class D – "Stiff Soil" (Default)

Risk Category
Used to compute the seismic design category.
I or II or III

Site Latitude
Decimal degrees for the site location.
40.5749102

Site Longitude
Decimal degrees for the site location.
-111.8866683

Compute Values

<https://earthquake.usgs.gov/designmaps/us/application.php>

- I selected 2009 NEHRP, so I can see a few more parameters.
- Enter Site Class, Risk Category and Location.

Step 1 Use the motion

USGS Design Maps Summary Report

User-Specified Input

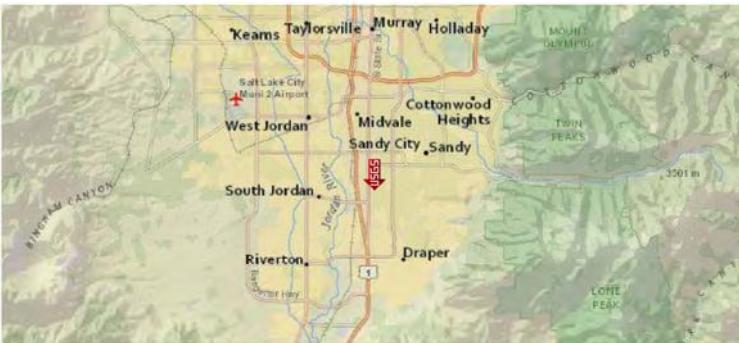
Report Title Ensign Office Building
Mon February 12, 2018 23:39:29 UTC

Building Code Reference Document 2009 NEHRP Recommended Seismic Provisions
(which utilizes USGS hazard data available in 2008)

Site Coordinates 40.57491°N, 111.88667°W

Site Soil Classification Site Class D – "Stiff Soil"

Risk Category I/II/III



USGS-Provided Output

$S_g = 1.435 \text{ g}$	$S_{gS} = 1.435 \text{ g}$	$S_{gD} = 0.957 \text{ g}$
$S_i = 0.481 \text{ g}$	$S_{iS} = 0.731 \text{ g}$	$S_{iD} = 0.487 \text{ g}$

For information on how the S_g and S_i values above have been calculated from probabilistic (risk-targeted) and deterministic ground motions in the direction of maximum horizontal response, please [view the detailed report](#).

MCE_H Spectrum

Design Response Spectrum

For PGA_{RP}, T_L, C_{RP}, and C_L values, please [view the detailed report](#).

Although this information is a product of the U.S. Geological Survey, we provide no warranty, expressed or implied, as to the accuracy of the data contained therein. This tool is not a substitute for technical subject-matter knowledge.

reduced ground

<https://earthquake.usgs.gov/designmaps/us/application.php>

- I selected 2009 NEHRP, so I can see a few more parameters.
- Enter Site Class, Risk Category and Location.

Step 1 Use the motion

USGS Design Maps Summary Report

User-Specified Input

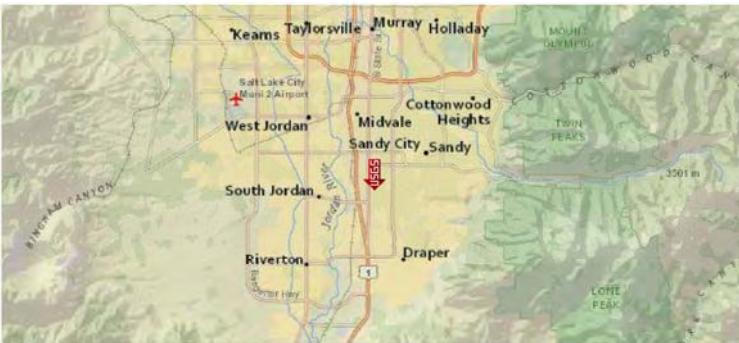
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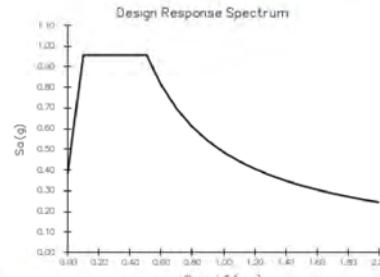
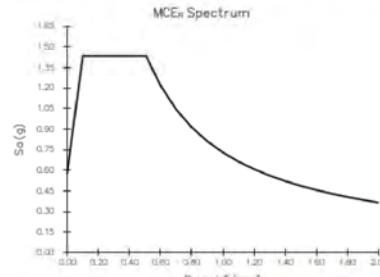
Risk Category I/II/III



USGS-Provided Output

$S_g = 1.435 \text{ g}$	$S_{gS} = 1.435 \text{ g}$	$S_{gD} = 0.957 \text{ g}$
$S_i = 0.481 \text{ g}$	$S_{iS} = 0.731 \text{ g}$	$S_{iD} = 0.487 \text{ g}$

For information on how the S_g and S_i values above have been calculated from probabilistic (risk-targeted) and deterministic ground motions in the direction of maximum horizontal response, please [view the detailed report](#).



For PGA_{MP} , T_{LI} , C_{RSI} and C_{RI} values, please [view the detailed report](#).

Although this information is a product of the U.S. Geological Survey, we provide no warranty, expressed or implied, as to the accuracy of the data contained therein. This tool is not a substitute for technical subject-matter knowledge.

reduced ground

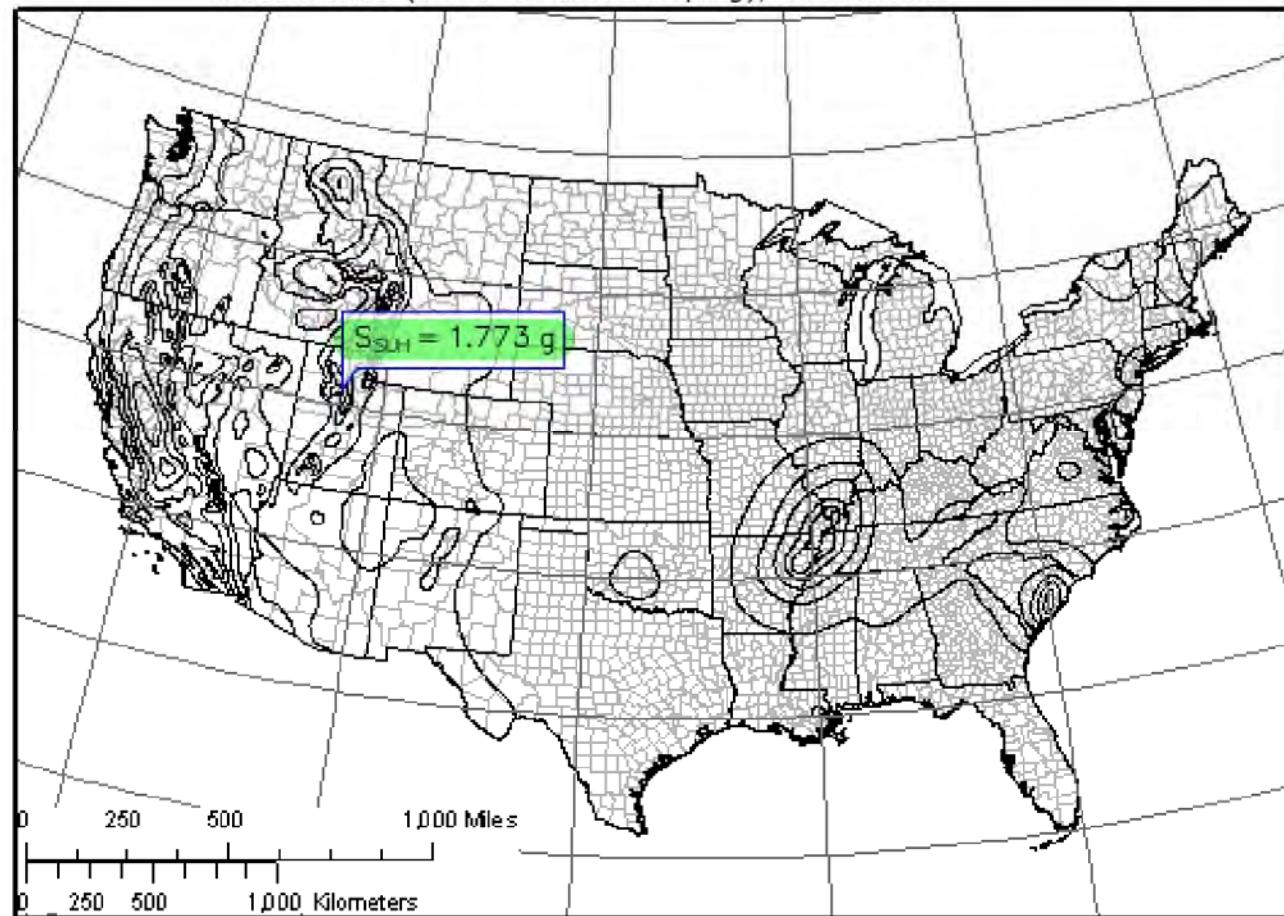
<https://earthquake.usgs.gov/designmaps/us/application.php>

- I selected 2009 NEHRP, so I can see a few more parameters.
- Enter Site Class, Risk Category and Location.

First, let's look at the USGS calculation
of S_s

$S_{SUH} = 1.773g$
PSHA 2% in 50yr "Uniform Hazard"
0.2s response acceleration.

Figure 22-1: Uniform-Hazard (2% in 50-Year) Ground Motions of 0.2-Second Spectral Response Acceleration (5% of Critical Damping), Site Class B

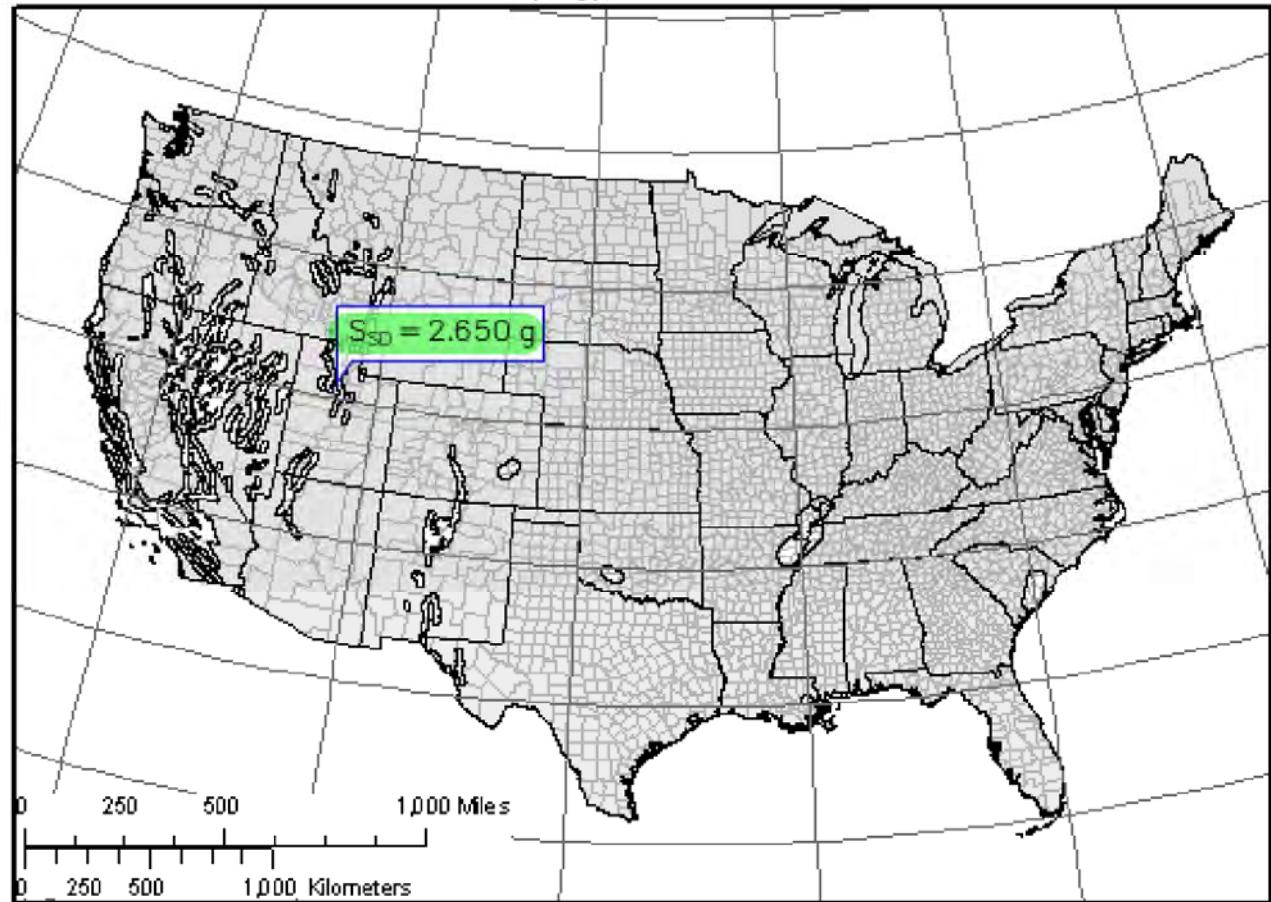


First, let's look at the USGS calculation
of S_s

$S_{SUH} = 1.773g$
PSHA 2% in 50yr "Uniform Hazard"
0.2s response acceleration.

$S_{SD} = 2.650g$
This is the DSHA 0.2s response
acceleration. (84th Percentile)

Figure 22-5: Deterministic Ground Motions of 0.2-Second Spectral Response Acceleration (5% of Critical Damping), Site Class B



First, let's look at the USGS calculation
of S_s

$$S_{SUH} = 1.773g$$

PSHA 2% in 50yr "Uniform Hazard"
0.2s response acceleration.

$$S_{SD} = 2.650g$$

This is the DSHA 0.2s response
acceleration. (84th Percentile)

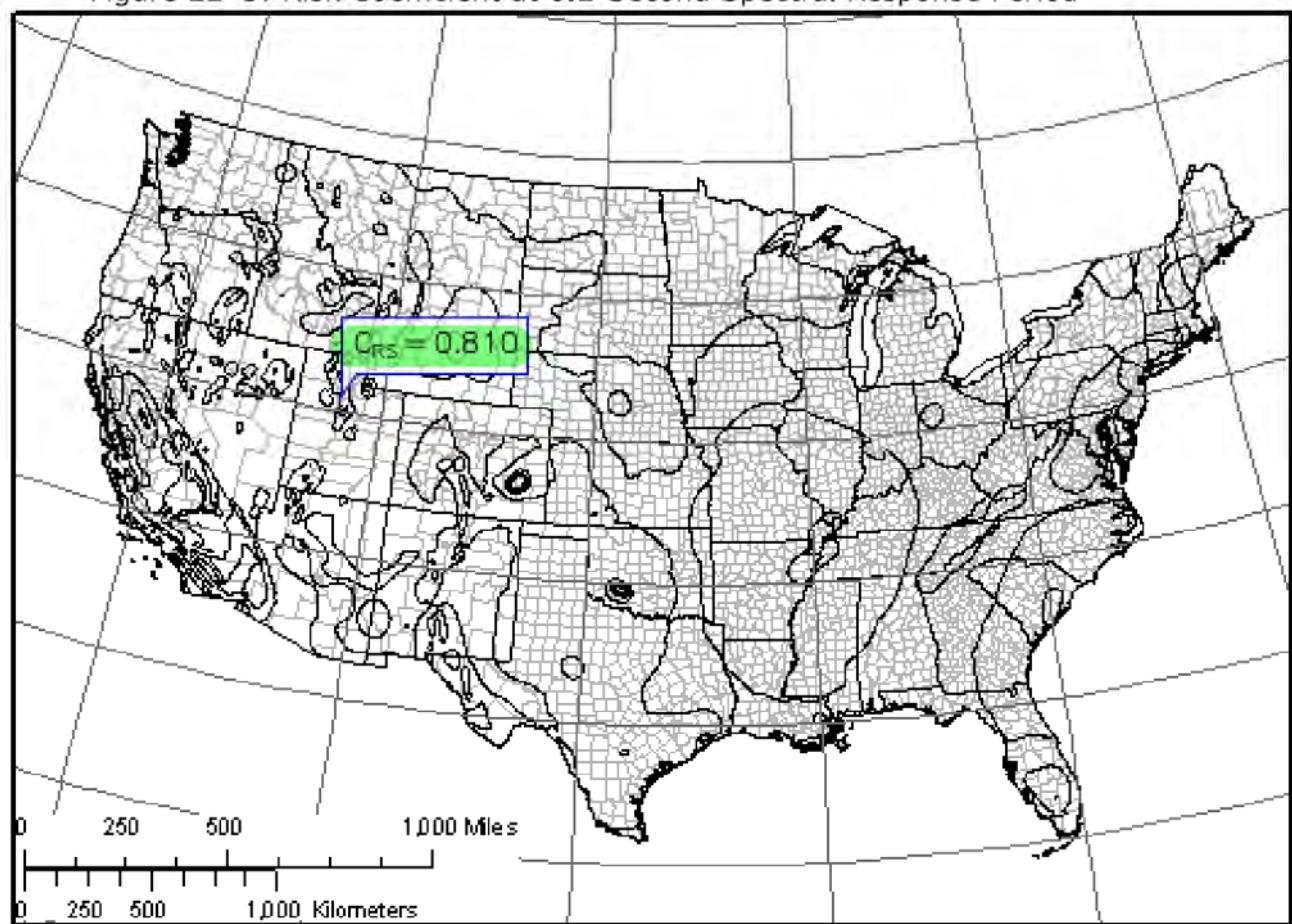
$$C_{RS} = 0.81$$

This is the Risk Coefficient. This factor
is intended to normalize the risk to a
fragility curve from California.

$$S_s = \min(C_{RS} * S_{SUH}, S_{SD}) = 1.436g$$
$$S_1 = \min(0.81 * 0.6, 0.88) = 0.481g$$

↑
 MCE_R

Figure 22-3: Risk Coefficient at 0.2-Second Spectral Response Period



Now let's look at Site Coefficients and Design Accelerations

$$S_s = 1.436g$$

$$F_a = 1.0$$

$$S_{MS} = F_a * S_s = 1.436g$$

$$S_{DS} = \frac{2}{3} * S_{MS} = 0.957g$$

$$S_1 = 0.481g$$

$$F_v = 1.519$$

$$S_{M1} = F_v * S_1 = 0.731g$$

$$S_{D1} = \frac{2}{3} * S_{M1} = 0.487g$$

Table 11.4-1: Site Coefficient F_a

Site Class	Spectral Response Acceleration Parameter at Short Period				
	$S_s \leq 0.25$	$S_s = 0.50$	$S_s = 0.75$	$S_s = 1.00$	$S_s \geq 1.25$
A	0.8	0.8	0.8	0.8	0.8
B	1.0	1.0	1.0	1.0	1.0
C	1.2	1.2	1.1	1.0	1.0
D	1.6	1.4	1.2	1.1	1.0
E	2.5	1.7	1.2	0.9	0.9
F	See Section 11.4.7 of ASCE 7				

Note: Use straight-line interpolation for intermediate values of S_s

For Site Class = D and $S_s = 1.435 g$, $F_a = 1.000$

Table 11.4-2: Site Coefficient F_v

Site Class	Spectral Response Acceleration Parameter at 1-Second Period				
	$S_1 \leq 0.10$	$S_1 = 0.20$	$S_1 = 0.30$	$S_1 = 0.40$	$S_1 \geq 0.50$
A	0.8	0.8	0.8	0.8	0.8
B	1.0	1.0	1.0	1.0	1.0
C	1.7	1.6	1.5	1.4	1.3
D	2.4	2.0	1.8	1.6	1.5
E	3.5	3.2	2.8	2.4	2.4
F	See Section 11.4.7 of ASCE 7				

Note: Use straight-line interpolation for intermediate values of S_1

For Site Class = D and $S_1 = 0.481 g$, $F_v = 1.519$

From these values we can plot a Design Response Spectrum

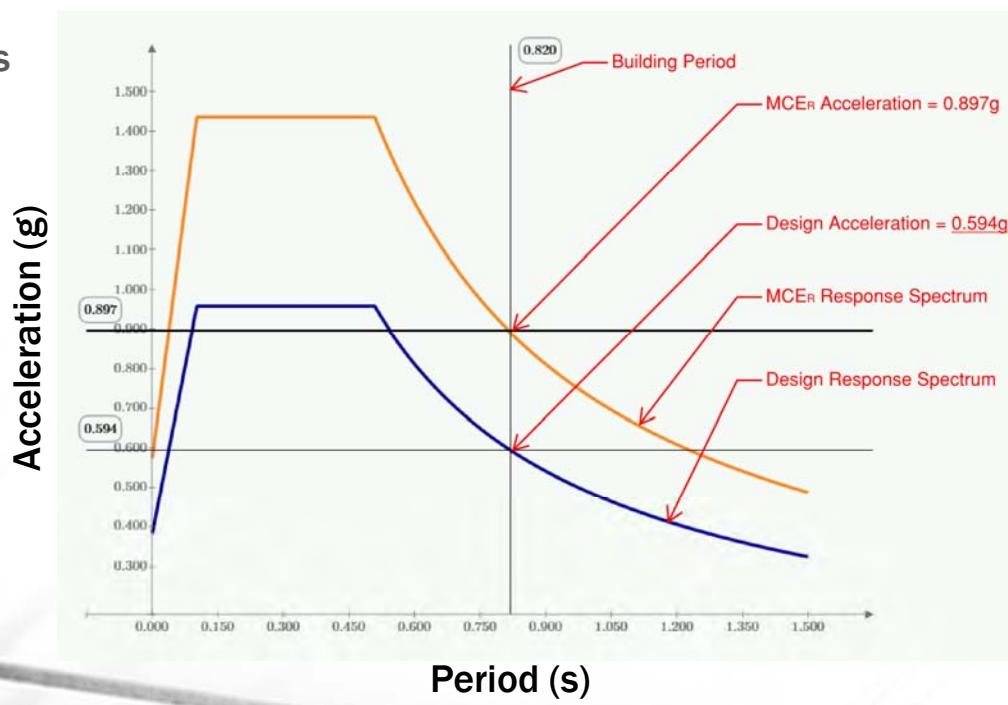
$$S_s = 1.436g$$

$$S_{ds} = \frac{2}{3} * S_{ms} = 0.957g$$

$$S_1 = 0.481g$$

$$S_{d1} = \frac{2}{3} * S_{m1} = 0.487g$$

$$T = 0.82s$$



Code Basis for Design-

At MCE_R the code targets a 10% probability of collapse. This is considered “Collapse Prevention”.

The code assumes that for traditional building design, there is a 1.5 safety factor against collapse, so we design for 2/3 MCE_R instead of MCE_R.

Step 4 –

Divide the design accelerations by the ductility factor R to calculate the seismic response coefficient, C_s .

- It is much easier to analyze a structure assuming it stays in the elastic range.
- So, we divide the Design Accelerations by a Response Modification Coefficient (R factor) which is a measure of how ductile a building system is. Typical R factors range from 1.5 to 8, with 8 being the most ductile. We can then analyze it assuming it remains elastic.
- Our example building is assumed to be a Special Steel Moment frame, R = 8.

Step 4 –

Divide the design accelerations by the ductility factor R to calculate the seismic response coefficient, C_s .

$$C_s = \min[S_{DS}/R, S_{D1}/(T^*R)]$$

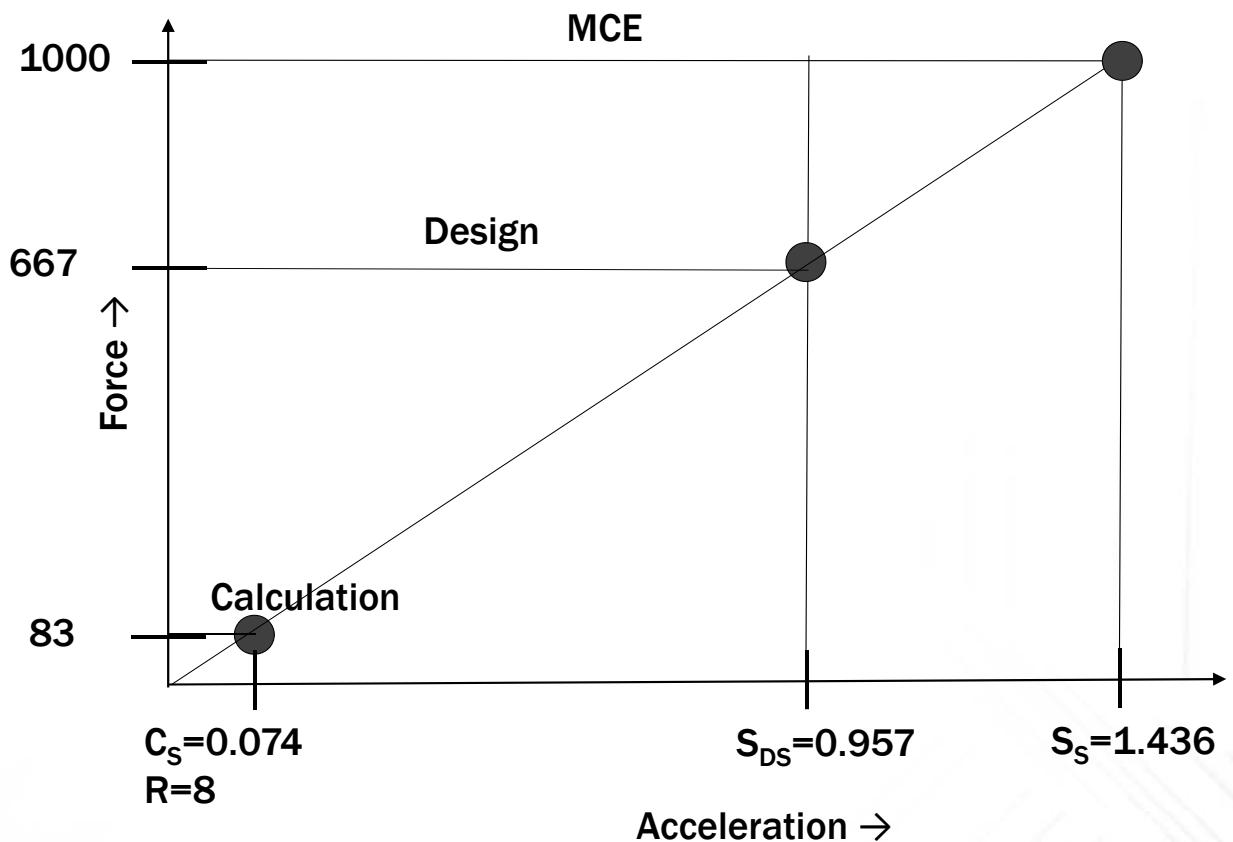
$$S_{DS}/R = 0.957g / 8 = 0.120g$$

$$S_{D1}/(T * R) = 0.487g / (0.82 * 8) = 0.074g$$

$$C_s = 0.074g$$



This is actual acceleration used in design. Theoretically, any response acceleration above this level would start to damage the building.



Step 5 –

Multiply the building's weight by C_s to get the design Base Shear.

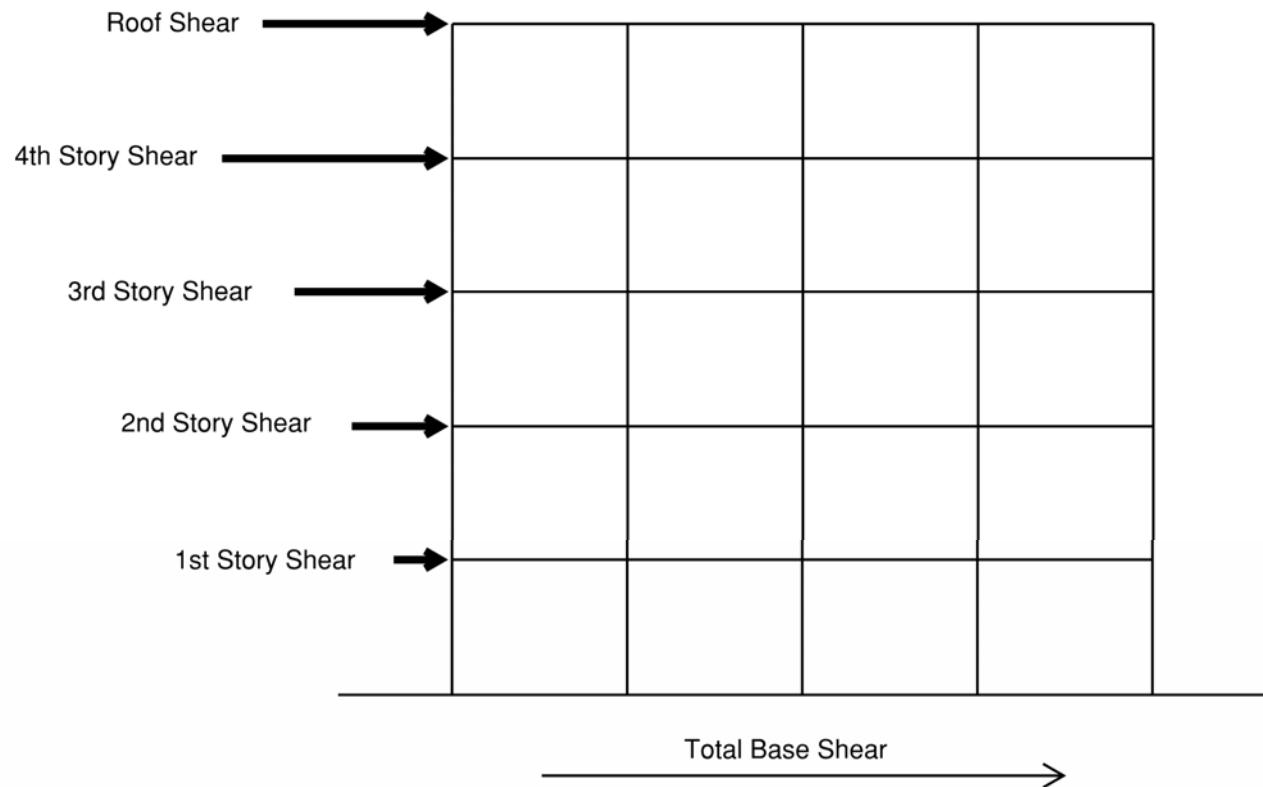
$$F = m * a$$

Base Shear (Lateral Force) = Building Mass * Design Acceleration

$$V = \text{Weight} * C_s = \text{Weight} * 0.074g = \text{Total Base Shear}$$

Step 6 – Distribute the base shear vertically to each level using the Equivalent Lateral Force procedure (ELF).

$$C_{vx} := \frac{w_x \cdot h_x^k}{\sum_{i=1}^n w_i \cdot h_i^k}$$



Step 7 – 11

Design the building for the calculated forces

Force in Column = 320 kip axial

ASD Force = $0.7 * 320 \text{ kip} = 224 \text{ kip}$

Column capacity is including a 1.67 safety factor is 235 kip

235 kip > 224 kip, so the column is okay.

Check drift

320 kip tension force
calculated in this column.

ASCE 7-10 Seismic Design Process

Step 1 - Use the USGS website application to get risk-modified ground motion parameters, S_s and S_1 (MCE_R).

Step 2 - Modify MCE_R parameters for soil effects (Site Class A-F).

Step 3 - Multiply site-modified MCE_R ground motions parameters by 2/3 to get design spectral acceleration parameters (S_{DS} and S_{D1}).

Step 4 - Divide S_{DS} and S_{D1} by the ductility factor R to calculate the seismic response coefficient, C_s .

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Step 6 - Distribute the base shear vertically to each level using the Equivalent Lateral Force procedure (ELF).

Step 7 – Analyze how the forces distribute through the diaphragms, shear walls, braces and frames.

Step 8 – For allowable stress design (ASD) reduce the force by a factor of 0.7.

Step 9 – Verify that the ASD design forces do not exceed the allowable capacities for each element.

Step 10 – Check building deflections/drifts.

In summary-

We looked at a taller building, but most buildings are short period. So-

1. Get mapped PSHA and DSHA 0.2s Response Accelerations. (1.773g and 2.650g)
2. Reduce PSHA by Risk Coefficient ($0.81 \times 1.773 = 1.436g$)
3. Take minimum between DSHA and reduced PSHA = $1.436g$ (MCE_R)
4. Modify for site response and multiply by 2/3 ($1.436 \times 1.0 \times 2 / 3 = 0.957g$)
5. Divide by Ductility Factor, R ($0.957g / 8 = 0.120g$)

Hence -

- A response acceleration of $0.120g$ theoretically could initiate damage in a short building.
- The building's ductility allows it to continue to take damage up to $0.957g$. There should be minimal loss of life up to this acceleration.
- Residual building capacity allows additional load beyond $0.957g$, but at $1.436g$ a code building will have a 10% likelihood of collapse.
- The ability of the building to withstand $1.773g$ or $2.650g$ accelerations is unknown. > 10% likelihood of collapse.

If instead of designing for the code minimums, a client wants me to design for a 7.0M Wasatch Fault Rupture, what design accelerations should I use?

Questions?

Eric Hoffman, PE

ehoffman@ensigneng.com

801.735.5197



2018 UGSWG

COMPARE 2018 IBC TO WASATCH FAULT RUPTURE

Public Expectations

Most lay people expect that the code protects them from a Wasatch fault rupture. Many structural engineers also have the same perception.

How close are the code MCE_R values compared to the 84th percentile deterministic values from a Wasatch fault rupture?

This Study

- Comparisons are based on dense soil/soft rock with a shear wave velocity of 760 m/s (2,500 f/t)
 - Boundary between Site Class B and Site Class C
- Does not compare other site classifications or site coefficients
- Uses ASCE 7-16
 - Derived from NGA West 2 GMPE's and 2014 USGS Seismic Hazard Maps
- Only looks at 2 periods – 0.2 S and 1.0 S
- First: Compare values from USGS Website: Probabilistic vs. 84th Percentile Deterministic
- Second: Look at NGA West 2 sensitivities using the PEER Spreadsheet

Apples to Apples: Comparing NGA West 2 to Code

- NGA West 2 calculates RotD50
- Code requires RotD100
- Adjustments to get from RotD50 to RotD100
 - $0.2 S = 1.1$
 - $1.0 S = 1.3$

USGS Website

Use Site Class B (Unmeasured) Rock
to get 760 m/s values.

The screenshot shows a web browser window for the USGS U.S. Seismic Design Maps beta site. The URL is https://earthquake.usgs.gov/designmaps/beta/us/. The page features the USGS and FEMA logos at the top, with a background image of a seismogram. The main title is "U.S. Seismic Design Maps". On the left, there's a sidebar with links for Earthquakes, Hazards, Data & Products, Learn, Monitoring, Research, and a search bar. The main content area has sections for "Title" (with a placeholder "Enter a title for this report..."), "Location" (with options to attempt automatic location, search by address, enter coordinates, or drop a pin), and "Reference Document" (set to 2015 NEHRP Provisions). Under "Site Class", it is set to "B (unmeasured): Rock". Under "Risk Category", it is set to "I or II or III". At the bottom, there are buttons for "Calculate", "New", "Print", "Download", and "Upload".

Information provided by USGS Webtool

Engineers no longer use the 2% in 50 year “Uniform Hazard” ground motion for building design.

They use a “Risk-targeted” ground motions which is the “Uniform Hazard” ground motion, multiplied by a risk factor C_{RS} , which converts the “Uniform Hazard” to a ground motion level that equates to a 1% risk of collapse in 50 years.

NGA2 calculates RotD50. Codes uses RotD100. To get code deterministic, multiply median by 1.1 or 1.3 to convert to RotD100. Then multiple by 1.8 to convert to approximate 84th percentile.

Site Coefficients and Risk-Targeted Maximum Considered Earthquake (MCE_R) Spectral Response Acceleration Parameters

Risk-targeted Ground Motion (0.2 s)

$$C_{RS} S_{SUH} = 0.864 \times 1.578 = 1.363 \text{ g}$$

Deterministic Ground Motion (0.2 s)

$$\text{Median} * 1.1 (\text{RotD100}) * 1.8$$

$$S_{SD} = 2.778 \text{ g}$$

$$S_S \equiv \text{Lesser of } C_{RS} S_{SUH} \text{ and } S_{SD} = 1.363 \text{ g}$$

Risk-targeted Ground Motion (1.0 s)

$$C_{R1} S_{1UH} = 0.878 \times 0.552 = 0.485 \text{ g}$$

Deterministic Ground Motion (1.0 s)

$$\text{Median} * 1.3 (\text{RotD100}) * 1.8$$

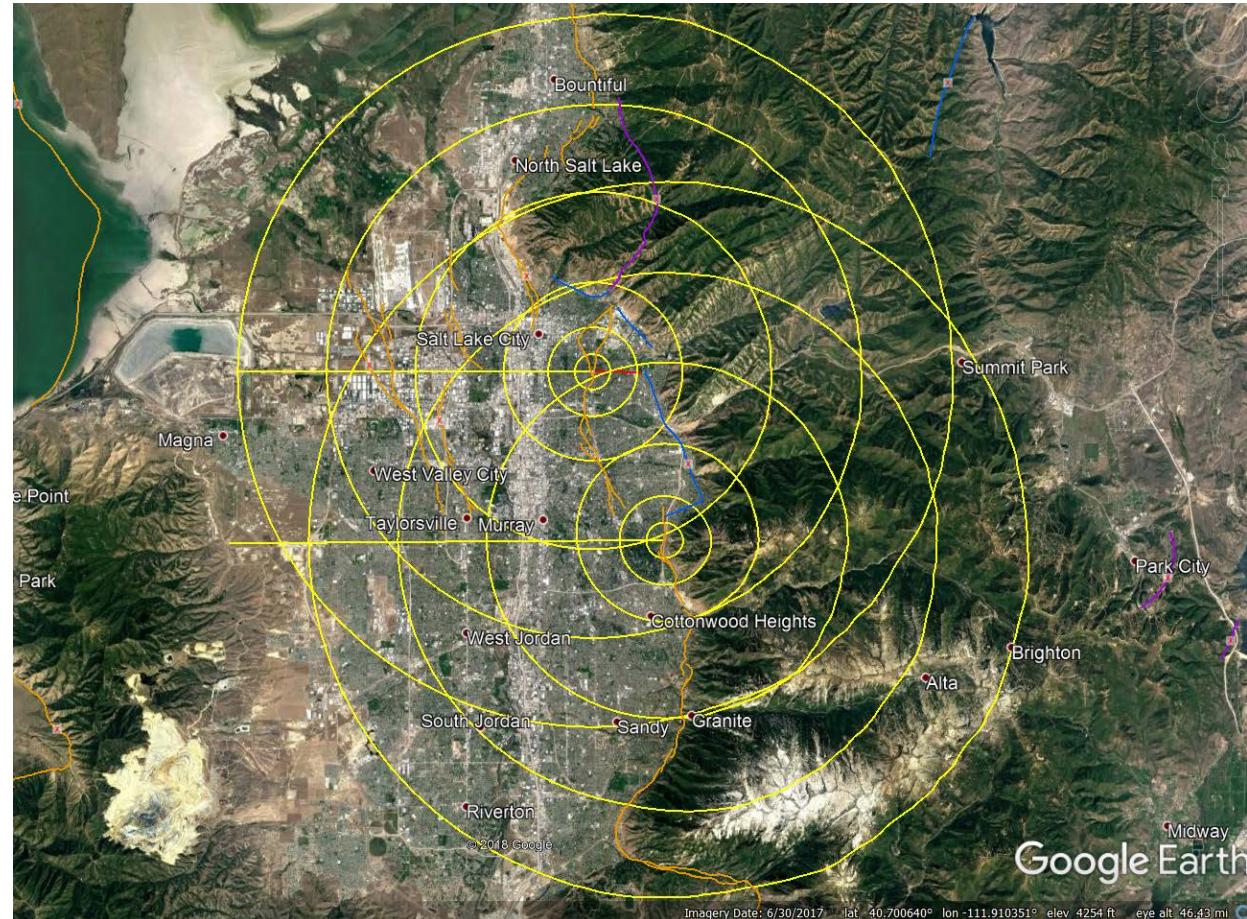
$$S_{1D} = 1.155 \text{ g}$$

$$S_1 \equiv \text{Lesser of } C_{R1} S_{1UH} \text{ and } S_{1D} = 0.485 \text{ g}$$

Calculate Values on Two Lines Across Salt Lake Valley

5300 South & 1300 South

- 1 km from fault
- 2.5 km from fault
- 5 km from fault
- 10 km from fault
- 15 km from fault
- 20 km from fault



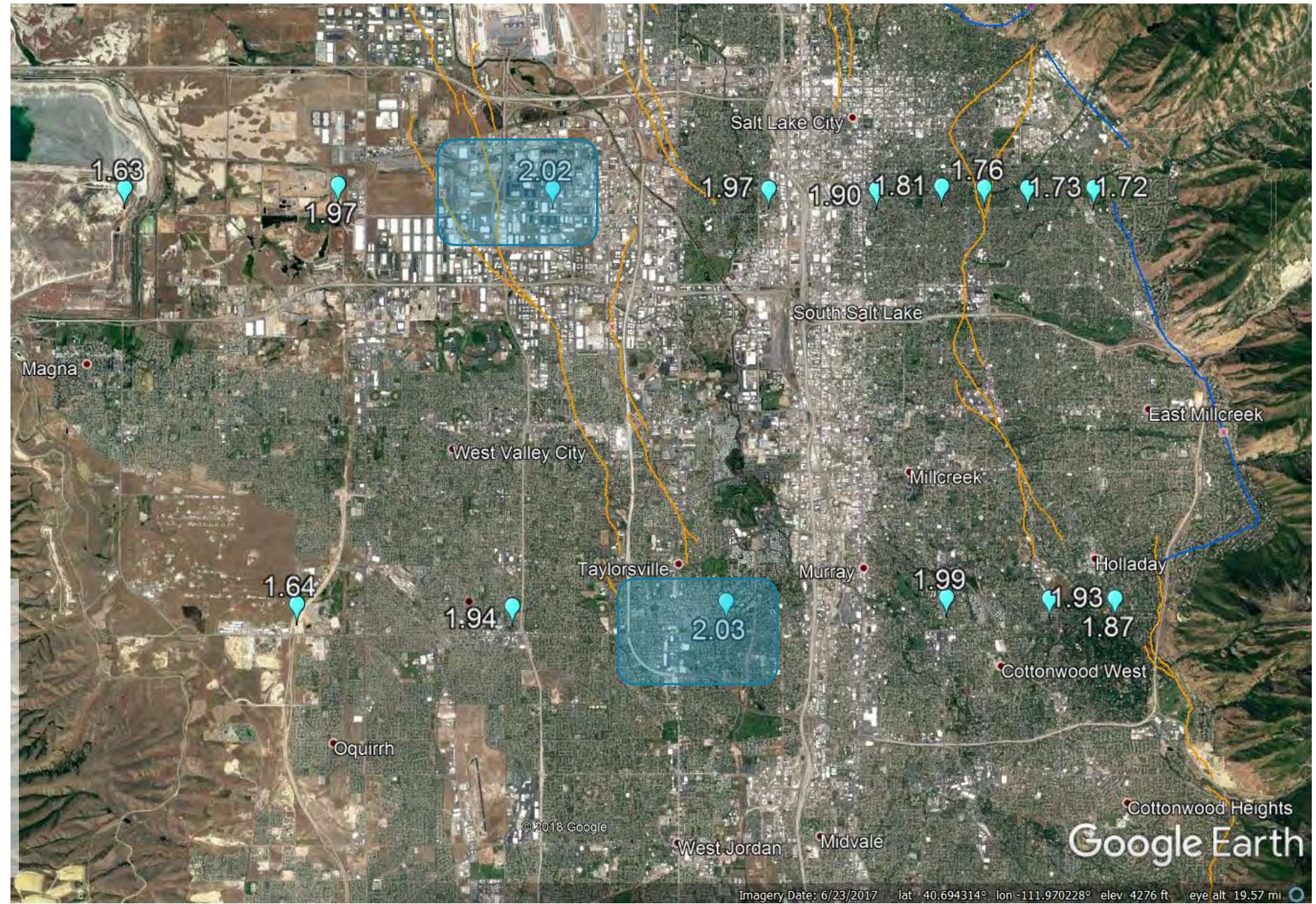
Input into Excel Spreadsheet

UGSWG 2018	0.2 S Response										1.0 S Response									
	84th Percentile		Uniform Hazard		Risk Coef.		MCE _R		2/3 MCE _R		84th Percentile		Uniform Hazard		Risk Coef.		MCE _R		2/3 MCE _R	
	Site Description	S _{SD}	S _{SUH}	C _{RS}	S _S	S _{DS}	S _{ID}	S _{IUH}	C _{R1}	S _I	S _{D1}									
5300 S 1 km W		2.547	1.579	0.862	1.360	0.907		1.121		0.575		0.870		0.500		0.333				
	Deterministic/Value			1.61		1.87	2.81					1.95				2.24		3.37		
5300 S 2.5 km W		2.742	1.650	0.860	1.419	0.946		1.163		0.594		0.867		0.515		0.344				
	Deterministic/Value			1.66		1.93	2.90					1.96				2.26		3.38		
5300 S 5 km W		2.932	1.712	0.859	1.471	0.981		1.186		0.607		0.865		0.526		0.350				
	Deterministic/Value			1.71		1.99	2.99					1.95				2.25		3.39		
5300 S 10 km W		2.942	1.687	0.858	1.447	0.965		1.101		0.583		0.868		0.506		0.338				
	Deterministic/Value			1.74		2.03	3.05					1.89				2.18		3.26		
5300 S 15 km W		2.415	1.437	0.869	1.248	0.832		0.871		0.500		0.875		0.437		0.292				
	Deterministic/Value			1.68		1.94	2.90					1.74				1.99		2.98		
5300 S 20 km W		1.681	1.166	0.879	1.026	0.684		0.609		0.412		0.879		0.363		0.242				
	Deterministic/Value			1.44		1.64	2.46					1.48				1.68		2.52		

0.2 Second

84th % Deterministic/MCE_R

In some cases 84th % is twice the MCE_R. (3 times the design (2/3 MCE_R).



Selected Wasatch Front Cities

0.2 S Response												1.0 S Response					
			84th Percentile Deterministic	Uniform Hazard	Risk Coef.	MCE _R	2/3 MCE _R				84th Percentile Deterministic	Uniform Hazard	Risk Coef.	MCE _R	2/3 MCE _R		
Site Description	Site Lat.	Site Long.	S _{SD}	S _{UH}	C _{RS}	S _s	S _{DS}	S _{ID}	S _{UH}	C _{R1}	S ₁	S _{D1}					
Tooele	40.531	-112.299	2.794	0.770	0.928	0.714	0.476	1.182	0.278	0.929	0.258	0.172					
Deterministic/Value				3.63		3.91	5.87		4.25		4.58	6.87					
Bountiful	40.882	-111.878	2.701	1.631	0.861	1.404	0.936	1.187	0.602	0.870	0.524	0.349					
Deterministic/Value				1.66		1.92	2.89		1.97		2.27	3.40					
Ogden	41.222	-111.97	2.983	1.580	0.863	1.363	0.909	1.254	0.565	0.880	0.497	0.331					
Deterministic/Value				1.89		2.19	3.28		2.22		2.52	3.79					
Brigham City	41.513	-112.016	2.778	1.578	0.864	1.363	0.909	1.155	0.552	0.878	0.485	0.323					
Deterministic/Value				1.76		2.04	3.06		2.09		2.38	3.58					
Provo	40.234	-111.669	3.056	1.628	0.857	1.396	0.931	1.294	0.589	0.875	0.515	0.343					
Deterministic/Value				1.88		2.19	3.28		2.20		2.51	3.77					

Results

- 84th percentile deterministic Wasatch fault ground motion values are significantly higher (1.6 to 2.5 time higher) than code MCE_R ground motion values.
- This is true even 20 km west of the fault.
- The code allows a 10% probability of collapse at MCE_R. What is the risk if the building experiences a ground motion twice as large?

NGA West 2 Sensitivities

Peer Excel Spreadsheet

PACIFIC EARTHQUAKE ENGINEERING RESEARCH CENTER 

WEIGHTED AVERAGE of 2014 NGA WEST-2 GMPEs

Last updated: 06 05 14

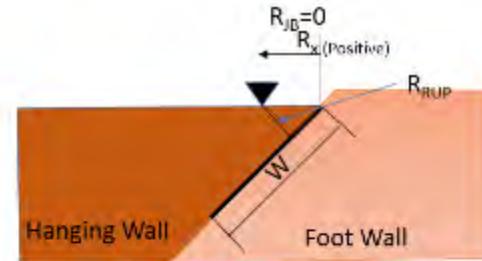
by Emel Seyhan, PhD, PEER & UCLA -- email: emel.seyhan@gmail.com, peer_center@berkeley.edu

Range of Values Used

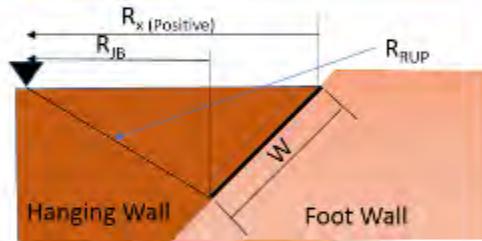
Coefficient		Min.	Max.	Best Guess (Default Used PEER Spreadsheet)
Magnitude	M_W	6.5	7.5	7.2
Shear Wave Velocity	V_{S30} (m/s)			760 m/s
Dip (Deg)		35	65	50
Coseismic Rupture	Z_{TOR} (km)	0	0	0 (at surface)
Hypocentral Depth	Z_{HYP} (km)	12	18	15 (Bottom of seismogenic crust)
Depth to $V_S=1$ km/S	$Z_{1.0}$ (km)	0.15	0.55	0.35
Depth to $V_S=2.5$ km/S	$Z_{2.5}$ (km)	1	3	
Fault Rupture Width	W (km)			Calculated (dip & seismogenic depth)
VS30 Flag				Measured
Region				California
FAS				No

Slice Through Salt Lake Valley at 5300 S.

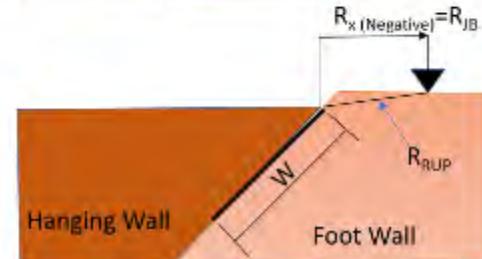
Used Mathcad to Calculate Distances Based on Dip Angle



$$R_{RUP} = R_x \cdot \sin(\text{dip})$$



$$\begin{aligned} R_{JB} &= R_x - W \cdot \cos(\text{dip}) \geq 0 \\ R_{RUP} &\text{ (for } R_x \leq W/\cos(\text{dip}) \text{)} = R_x \cdot \sin(\text{dip}) \\ R_{RUP} &\text{ (for } R_x > W/\cos(\text{dip}) \text{)} = [R_x^2 + W^2 - 2 \cdot R_x \cdot W \cdot \cos(\text{dip})]^{1/2} \end{aligned}$$



$$\begin{aligned} R_{RUP} &= (R_x^2 + \text{height}^2)^{1/2} \\ &= R_x \text{ if level ground} \end{aligned}$$

The following slides are based on ...

- 0.2 Second Response
- Weighted average using factor of 0.22 for ASK14, BSSA14 & CB14, and 0.12 for I14.

Variability in NGA 2 Models (Lowest to Highest)

	ASK14	BSSA14	CB14	CY14	I14	Max	Min	Difference	% Diff.
1.0 km	1.28	0.88	1.53	1.22	1.31	1.53	0.88	0.65	74%
2.5 km	1.33	0.88	1.68	1.22	1.15	1.68	0.88	0.80	92%
5.0 km	1.31	0.88	1.83	1.20	0.95	1.83	0.88	0.96	109%
10 km	1.12	0.88	1.76	1.04	0.68	1.76	0.68	1.08	158%
15 km	0.80	0.80	1.19	0.76	0.53	1.19	0.53	0.67	127%
20 km	0.54	0.55	0.76	0.53	0.42	0.76	0.42	0.34	81%

Dip Only – Compared to 50 deg. (Seismogenic Depth = 15 km)

		1 km	2.5 km	5 km	10 km	15 km	20 km
35 deg.		4%	6%	10%	21%	51%	98%
65 deg.		-4%	-6%	-11%	-30%	-36%	-30%

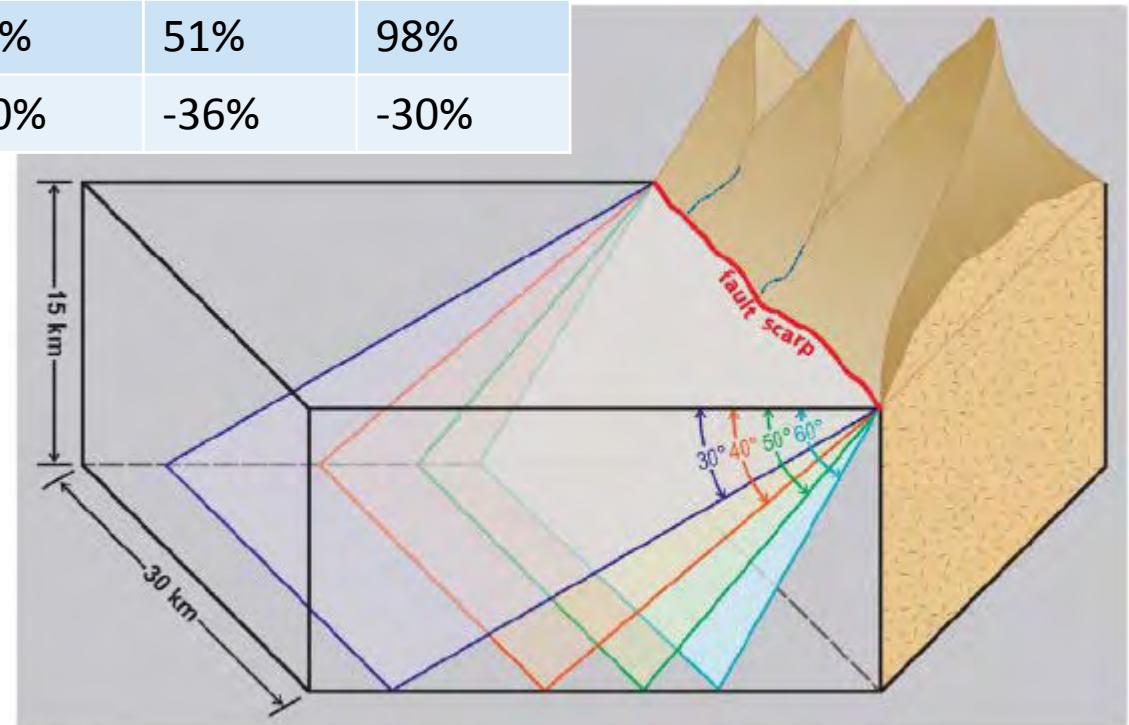


Figure 3.2-1. Schematic diagram showing the non-linear increase in fault area with decreasing dip angles.

Seismogenic Depth Only (Compared to 15km) (Dip = 50 deg.)

		1 km	2.5 km	5 km	10 km	15 km	20 km
12 km		-3%	-2%	-1%	-3%	-16%	-14%
18 km		3%	3%	2%	2%	17%	17%

Dip and Seismogenic Depth (Worst Case)

		1 km	2.5 km	5 km	10 km	15 km	20 km
Above Base		8%	9%	12%	22%	52%	103%
Below Base		-7%	-8%	-14%	-37%	-42%	-35%

Magnitude (Base 7.2)

Vary (6.5, 7.0, 7.1, 7.3, 7.5, 8.0)

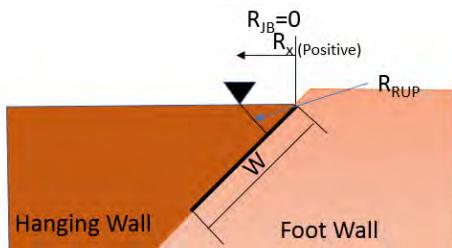
	1 km	2.5 km	5 km	10 km	15 km	20 km
6.5	-10%	-11%	-14%	-18%	-20%	-23%
7.0	-2%	-2%	-3%	-5%	-5%	-6%
7.1	-1%	-1%	-2%	-2%	-3%	-3%
7.3	1%	1%	2%	2%	3%	3%
7.5	3%	3%	5%	7%	8%	10%
8.0	7%	9%	13%	20%	23%	28%

Vary Z1 (Compare to 0.35 km)

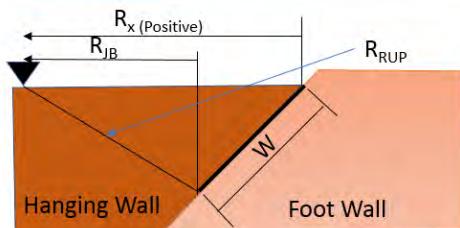
		1 km	2.5 km	5 km	10 km	15 km	20 km
0.55 km		0%	0%	0%	0%	0%	0%
0.15 km		-2%	-2%	-2%	-2%	-2%	-2%

Conclusions

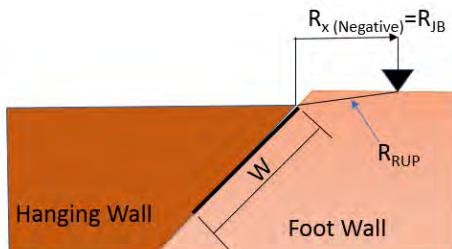
- There is huge variability in the ground motion prediction models (74% to 158% comparing lowest to highest)
- The single largest factor affecting ground motion is angle of dip.
- There is significantly more variability in ground motion 10 km and greater from the fault than there is in 5 km and less.
- Magnitudes from 6.5 to 7.5 have relatively small impact on ground motion, especially considering the variability in dip and the GMPE's



$$R_{RUP} = R_x * \sin(\text{dip})$$



$$\begin{aligned} R_{JB} &= R_x - W * \cos(\text{dip}) \geq 0 \\ R_{RUP} &(\text{for } R_x \leq W / \cos(\text{dip})) = R_x * \sin(\text{dip}) \\ R_{RUP} &(\text{for } R_x > W / \cos(\text{dip})) = [R_x^2 + W^2 - 2 * R_x * W * \cos(\text{dip})]^{1/2} \end{aligned}$$



$$\begin{aligned} R_{RUP} &= (R_x^2 + \text{height}^2)^{1/2} \\ &= R_x \text{ if level ground} \end{aligned}$$

Hanging Wall over Fault

Intermountain Medical Center
Lat: 40.6613 Long: -111.8912

$$R_{JB} := 0$$

$$R_{RUP} := R_{X1} * \sin(\text{Dip}) = 5.734 \text{ km}$$

$$W := 40 \text{ km}$$

$$\text{Dip} := 55 \text{ deg}$$

$$W * \cos(\text{Dip}) = 22.943 \text{ km}$$

Hanging Wall West of Fault

Tooele
Lat: 40.5306 Long: -112.2985

$$R_{X2} := 40 \text{ km}$$

$$R_{JB} := \max(R_{X2} - W * \cos(\text{Dip}), 0) = 17.057 \text{ km}$$

$$R_{RUP} := \begin{cases} \frac{W}{\cos(\text{Dip})} & \text{if } R_{X2} \leq \frac{W}{\cos(\text{Dip})} \\ R_{X2} * \sin(\text{Dip}) & \\ \text{else} & \left| \sqrt{R_{X2}^2 + W^2 - 2 * R_{X2} * W * \cos(\text{Dip})} \right| \end{cases} = 32.766 \text{ km}$$

Footwall East of Fault

Brent's House
Lat: 40.7386 Long: -111.8357

$$R_{X3} := -1.6 \text{ km}$$

$$R_B := 1.6 \text{ km}$$

$$R_{RUP} := 1.6 \text{ km}$$

Use values provided by Dr. James Pechmann from the University of Utah. **The value of W** is based on the seismogenic depth with could vary between 12 km to 18 km. Calculate the various values of W based on seismogenic depth. When this happens, the values of R X, R JB, and R RUP vary.

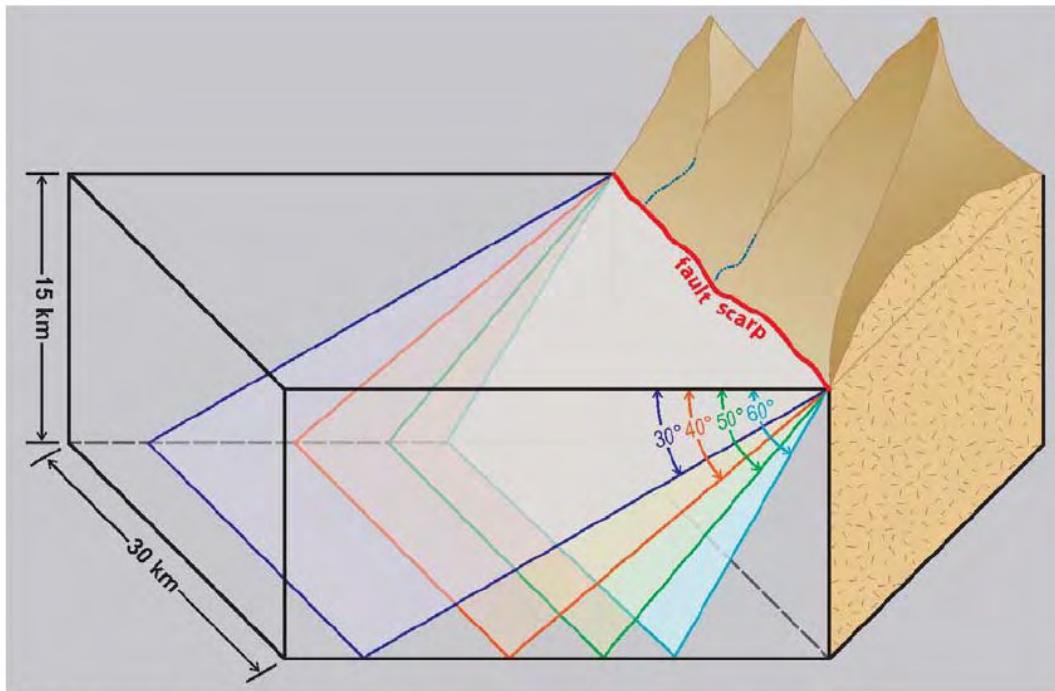


Figure 3.2-1. Schematic diagram showing the non-linear increase in fault area with decreasing dip angles.

$\text{Dip} := \begin{bmatrix} 35 \\ 40 \\ 45 \\ 50 \\ 55 \\ 60 \\ 65 \end{bmatrix}$ $W_{15} := \frac{\text{Seismogenic15}}{\sin(\text{Dip})} = \begin{bmatrix} 26.152 \\ 23.336 \\ 21.213 \\ 19.581 \\ 18.312 \\ 17.321 \\ 16.551 \end{bmatrix} \text{ km}$ $\text{Seismogenic12} := 12 \cdot \text{km}$ $W_{12} := \frac{\text{Seismogenic12}}{\sin(\text{Dip})} = \begin{bmatrix} 20.921 \\ 18.669 \\ 16.971 \\ 15.665 \\ 14.649 \\ 13.856 \\ 13.241 \end{bmatrix} \text{ km}$ $W_{18} := \frac{\text{Seismogenic18}}{\sin(\text{Dip})} = \begin{bmatrix} 31.382 \\ 28.003 \\ 25.456 \\ 23.497 \\ 21.974 \\ 20.785 \\ 19.861 \end{bmatrix} \text{ km}$	$\text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix}$ $\text{deg} \quad x15 := \frac{\text{Seismogenic15}}{\tan(\text{Dip})} = \begin{bmatrix} 21.422 \\ 17.876 \\ 15.000 \\ 12.586 \\ 10.503 \\ 8.660 \\ 6.995 \end{bmatrix} \text{ km}$ $\text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix}$ $\text{deg} \quad x12 := \frac{\text{Seismogenic12}}{\tan(\text{Dip})} = \begin{bmatrix} 17.138 \\ 14.301 \\ 12.000 \\ 10.069 \\ 8.402 \\ 6.928 \\ 5.596 \end{bmatrix} \text{ km}$ $\text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix}$ $\text{deg} \quad x18 := \frac{\text{Seismogenic18}}{\tan(\text{Dip})} = \begin{bmatrix} 25.707 \\ 21.452 \\ 18.000 \\ 15.104 \\ 12.604 \\ 10.392 \\ 8.394 \end{bmatrix} \text{ km}$
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Hanging Wall West of Fault

$$R_{X1} = 7.000 \text{ km}$$

$$j := 1 \dots 7$$

Intermountain Medical Center (IMC)

Lat: 40.6613 Long:-111.8912

$$R_X := R_{X1} = 7.000 \text{ km}$$

$$x := x15 \quad R_{JB15_j} := \max(R_X - x_j, 0) = \begin{bmatrix} 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$x := x12$$

$$R_{JB12_j} := \max(R_X - x_j, 0) = \begin{bmatrix} 0.000 \\ 0.000 \\ 0.072 \\ 1.404 \end{bmatrix} \text{ km}$$

$$x := x18 \quad R_{JB18_j} := \max(R_X - x_j, 0) = \begin{bmatrix} 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{bmatrix} \text{ km}$$

$$W := W_{15}$$

$$R_{RUP15_j} := \begin{cases} W_j & \text{if } R_X \leq \frac{W_j}{\cos(\text{Dip}_j)} \\ R_X \cdot \sin(\text{Dip}_j) & \\ \text{else} & \\ \sqrt{R_X^2 + W_j^2 - 2 \cdot R_X \cdot W_j \cdot \cos(\text{Dip}_j)} & \end{cases} = \begin{bmatrix} 4.015 \\ 4.500 \\ 4.950 \\ 5.362 \\ 5.734 \\ 6.062 \\ 6.344 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$W := W_{12}$$

$$R_{RUP12_j} := \begin{cases} W_j & \text{if } R_X \leq \frac{W_j}{\cos(\text{Dip}_j)} \\ R_X \cdot \sin(\text{Dip}_j) & \\ \text{else} & \\ \sqrt{R_X^2 + W_j^2 - 2 \cdot R_X \cdot W_j \cdot \cos(\text{Dip}_j)} & \end{cases} = \begin{bmatrix} 4.015 \\ 4.500 \\ 4.950 \\ 5.362 \\ 5.734 \\ 6.062 \\ 6.344 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$W := W_{18}$$

$$R_{RUP18_j} := \begin{cases} W_j & \text{if } R_X \leq \frac{W_j}{\cos(\text{Dip}_j)} \\ R_X \cdot \sin(\text{Dip}_j) & \\ \text{else} & \\ \sqrt{R_X^2 + W_j^2 - 2 \cdot R_X \cdot W_j \cdot \cos(\text{Dip}_j)} & \end{cases} = \begin{bmatrix} 4.015 \\ 4.500 \\ 4.950 \\ 5.362 \\ 5.734 \\ 6.062 \\ 6.344 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$W_{15} = \begin{bmatrix} 26.152 \\ 23.336 \\ 21.213 \\ 19.581 \\ 18.312 \\ 17.321 \\ 16.551 \end{bmatrix} \text{ km} \quad W_{12} = \begin{bmatrix} 20.921 \\ 18.669 \\ 16.971 \\ 15.665 \\ 14.649 \\ 13.856 \\ 13.241 \end{bmatrix} \text{ km} \quad W_{18} = \begin{bmatrix} 31.382 \\ 28.003 \\ 25.456 \\ 23.497 \\ 21.974 \\ 20.785 \\ 19.861 \end{bmatrix} \text{ km}$$

Dip = $\begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix}$ deg

$$R_{X1} = 7.000 \text{ km}$$

$$R_{JB15} = \begin{bmatrix} 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.005 \end{bmatrix} \text{ km} \quad R_{JB12} = \begin{bmatrix} 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.072 \\ 1.404 \end{bmatrix} \text{ km} \quad R_{JB18} = \begin{bmatrix} 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{bmatrix} \text{ km}$$

Dip = $\begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix}$ deg

$$R_{RUP15} = \begin{bmatrix} 4.015 \\ 4.500 \\ 4.950 \\ 5.362 \\ 5.734 \\ 6.062 \\ 6.344 \end{bmatrix} \text{ km} \quad R_{RUP12} = \begin{bmatrix} 4.015 \\ 4.500 \\ 4.950 \\ 5.362 \\ 5.734 \\ 6.062 \\ 6.344 \end{bmatrix} \text{ km} \quad R_{RUP18} = \begin{bmatrix} 4.015 \\ 4.500 \\ 4.950 \\ 5.362 \\ 5.734 \\ 6.062 \\ 6.344 \end{bmatrix} \text{ km}$$

Dip = $\begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix}$ deg

W varies by both Dip angle and seismogenic depth. The minimum value of W (13.24 km) is at a shallow seismogenic depth (12 km) and a steep dip angle (65 degrees). The maximum value of W (31.38) is at a deep seismogenic depth (18 km) and a shallow angle (35 degrees).

R X is the same for all seismogenic depths.

R JB is 0, except where seismogenic depth is shallow (12 km) and dip is steep (60 or 65 degrees). It gets as large as 1.40 km.

R RUP is the same for all seismogenic depths. It varies only by angle. The minimum value is 4.01 km, the maximum value is 6.34 km.

Run a sensitivity analysis for the IMC site. Use the 7 pairs of Dip and W. Set R X, R JB, and R RUP for the various values for the pairs of Dip and W.

The seismogenic depth does not affect the values of R except at the 12 km depth.

Run the 65 degree dip angle twice. Once with R JB at 0.0 km and once with R JB at 1.40 km to see how the values change.

Hanging Wall West of Fault	$R_{X2} = 40.000 \text{ km}$	$j := 1 \dots 7$
Tooele Lat: 40.5306 Long: -112.2985		
$R_X := R_{X2} = 40.000 \text{ km}$	$\begin{bmatrix} 18.578 \\ 22.124 \\ 25.000 \\ 27.414 \\ 29.497 \\ 22.862 \\ 25.699 \end{bmatrix} \text{ km}$	$\begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$
$x := x15$	$R_{JB15_j} := \max(R_X - x_j, 0) = \begin{bmatrix} 28.000 \\ 29.931 \\ 31.598 \\ 33.072 \\ 34.404 \end{bmatrix} \text{ km}$	
$x := x12$	$R_{JB12_j} := \max(R_X - x_j, 0) = \begin{bmatrix} 14.293 \\ 18.548 \\ 22.000 \end{bmatrix} \text{ km}$	
$x := x18$	$R_{JB18_j} := \max(R_X - x_j, 0) = \begin{bmatrix} 24.896 \\ 27.396 \\ 29.608 \\ 31.606 \end{bmatrix} \text{ km}$	
$W := W_{15}$	$R_{RUP15_j} := \begin{cases} W_j & \text{if } R_X \leq \frac{W_j}{\cos(\text{Dip}_j)} \\ R_X \cdot \sin(\text{Dip}_j) & \text{else} \end{cases}$	$= \begin{bmatrix} 23.877 \\ 26.729 \\ 29.155 \\ 31.249 \\ 33.092 \\ 34.744 \\ 36.254 \end{bmatrix} \text{ km}$
$W := W_{12}$	$R_{RUP12_j} := \begin{cases} W_j & \text{if } R_X \leq \frac{W_j}{\cos(\text{Dip}_j)} \\ R_X \cdot \sin(\text{Dip}_j) & \text{else} \end{cases}$	$= \begin{bmatrix} 25.820 \\ 28.363 \\ 30.463 \\ 32.247 \\ 33.799 \\ 35.182 \\ 36.437 \end{bmatrix} \text{ km}$
$W := W_{18}$	$R_{RUP18_j} := \begin{cases} W_j & \text{if } R_X \leq \frac{W_j}{\cos(\text{Dip}_j)} \\ R_X \cdot \sin(\text{Dip}_j) & \text{else} \end{cases}$	$= \begin{bmatrix} 22.985 \\ 25.847 \\ 28.425 \\ 30.722 \\ 32.780 \\ 34.641 \\ 36.252 \end{bmatrix} \text{ km}$

$$W_{15} = \begin{bmatrix} 26.152 \\ 23.336 \\ 21.213 \\ 19.581 \\ 18.312 \\ 17.321 \\ 16.551 \end{bmatrix} \text{ km} \quad W_{12} = \begin{bmatrix} 20.921 \\ 18.669 \\ 16.971 \\ 15.665 \\ 14.649 \\ 13.856 \\ 13.241 \end{bmatrix} \text{ km} \quad W_{18} = \begin{bmatrix} 31.382 \\ 28.003 \\ 25.456 \\ 23.497 \\ 21.974 \\ 20.785 \\ 19.861 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$R_{X2} = 40.000 \text{ km}$$

$$R_{JB15} = \begin{bmatrix} 18.578 \\ 22.124 \\ 25.000 \\ 27.414 \\ 29.497 \\ 31.340 \\ 33.005 \end{bmatrix} \text{ km} \quad R_{JB12} = \begin{bmatrix} 22.862 \\ 25.699 \\ 28.000 \\ 29.931 \\ 31.598 \\ 33.072 \\ 34.404 \end{bmatrix} \text{ km} \quad R_{JB18} = \begin{bmatrix} 14.293 \\ 18.548 \\ 22.000 \\ 24.896 \\ 27.396 \\ 29.608 \\ 31.606 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$R_{RUP15} = \begin{bmatrix} 23.877 \\ 26.729 \\ 29.155 \\ 31.249 \\ 33.092 \\ 34.744 \\ 36.254 \end{bmatrix} \text{ km} \quad R_{RUP12} = \begin{bmatrix} 25.820 \\ 28.363 \\ 30.463 \\ 32.247 \\ 33.799 \\ 35.182 \\ 36.437 \end{bmatrix} \text{ km} \quad R_{RUP18} = \begin{bmatrix} 22.985 \\ 25.847 \\ 28.425 \\ 30.722 \\ 32.780 \\ 34.641 \\ 36.252 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

R X is the same for all seismogenic depths.

R JB varies by both seismogenic depth and dip. The smallest value of R JB (14.29 km) is at deep seismogenic depth and shallow angle (i.e. bottom of fault extends way west). The largest value of R JB (34.40 km) is as a shallow seismogenic depth and steep angle (i.e. the bottom of fault is furthest to the east).

R RUP varies by both seismogenic depth and dip. It is similar to R JB. The smallest value of R RUP (22.96 km) is at deep seismogenic depth and shallow angle (i.e. bottom of fault extends way west). The largest value of R RUP (36.44 km) is as a shallow seismogenic depth and steep angle (i.e. the bottom of fault is furthest to the east).

Run a sensitivity analysis for the IMC site. Use the 7 pairs of Dip and W using. Set R X, R JB, and R RUP for the various values for the pairs of Dip and W.

The seismogenic depth does not affect the values of R except at the 12 km depth.

Run the 65 degree dip angle twice. Once with R JB at 0.0 km and once with R JB at 1.40 km to see how the values change.

Footwall East of Fault

$$R_{X3} = -1.600 \text{ km}$$

Brent's House

Lat:40.7386 Long:-111.8357

$$R_B := 1.6 \text{ km}$$

$$R_{RUP} := 1.6 \text{ km}$$

The three values of R do not vary with seismogenic depth or with angle of dip.

Hanging Wall West of Fault

$$R_{X4} := 1 \text{ km}$$

$$j := 1 \dots 7$$

1 KM West of Scarp

Lat: 40.656 Long:-111.819

$$R_X := R_{X4} = 1.000 \text{ km}$$

$$x := x15 \quad R_{JB15_j} := \max(R_X - x_j, 0) = \begin{bmatrix} 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$x := x12$$

$$R_{JB12_j} := \max(R_X - x_j, 0) = \begin{bmatrix} 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{bmatrix} \text{ km}$$

$$x := x18 \quad R_{JB18_j} := \max(R_X - x_j, 0) = \begin{bmatrix} 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{bmatrix} \text{ km}$$

$$W := W_{15}$$

$$R_{RUP15_j} := \begin{cases} \frac{W_j}{\cos(\text{Dip}_j)} & \text{if } R_X \leq \frac{W_j}{\cos(\text{Dip}_j)} \\ R_X \cdot \sin(\text{Dip}_j) & \text{else} \\ \sqrt{R_X^2 + W_j^2 - 2 \cdot R_X \cdot W_j \cdot \cos(\text{Dip}_j)} & \end{cases} = \begin{bmatrix} 0.574 \\ 0.643 \\ 0.707 \\ 0.766 \\ 0.819 \\ 0.866 \\ 0.906 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$W := W_{12}$$

$$R_{RUP12_j} := \begin{cases} \frac{W_j}{\cos(\text{Dip}_j)} & \text{if } R_X \leq \frac{W_j}{\cos(\text{Dip}_j)} \\ R_X \cdot \sin(\text{Dip}_j) & \text{else} \\ \sqrt{R_X^2 + W_j^2 - 2 \cdot R_X \cdot W_j \cdot \cos(\text{Dip}_j)} & \end{cases} = \begin{bmatrix} 0.574 \\ 0.643 \\ 0.707 \\ 0.766 \\ 0.819 \\ 0.866 \\ 0.906 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$W := W_{18}$$

$$R_{RUP18_j} := \begin{cases} \frac{W_j}{\cos(\text{Dip}_j)} & \text{if } R_X \leq \frac{W_j}{\cos(\text{Dip}_j)} \\ R_X \cdot \sin(\text{Dip}_j) & \text{else} \\ \sqrt{R_X^2 + W_j^2 - 2 \cdot R_X \cdot W_j \cdot \cos(\text{Dip}_j)} & \end{cases} = \begin{bmatrix} 0.574 \\ 0.643 \\ 0.707 \\ 0.766 \\ 0.819 \\ 0.866 \\ 0.906 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$W_{15} = \begin{bmatrix} 26.152 \\ 23.336 \\ 21.213 \\ 19.581 \\ 18.312 \\ 17.321 \\ 16.551 \end{bmatrix} \text{ km} \quad W_{12} = \begin{bmatrix} 20.921 \\ 18.669 \\ 16.971 \\ 15.665 \\ 14.649 \\ 13.856 \\ 13.241 \end{bmatrix} \text{ km} \quad W_{18} = \begin{bmatrix} 31.382 \\ 28.003 \\ 25.456 \\ 23.497 \\ 21.974 \\ 20.785 \\ 19.861 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$R_X = 1.000 \text{ km}$$

$$R_{JB15} = \begin{bmatrix} 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{bmatrix} \text{ km} \quad R_{JB12} = \begin{bmatrix} 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{bmatrix} \text{ km} \quad R_{JB18} = \begin{bmatrix} 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$R_{RUP15} = \begin{bmatrix} 0.574 \\ 0.643 \\ 0.707 \\ 0.766 \\ 0.819 \\ 0.866 \\ 0.906 \end{bmatrix} \text{ km} \quad R_{RUP12} = \begin{bmatrix} 0.574 \\ 0.643 \\ 0.707 \\ 0.766 \\ 0.819 \\ 0.866 \\ 0.906 \end{bmatrix} \text{ km} \quad R_{RUP18} = \begin{bmatrix} 0.574 \\ 0.643 \\ 0.707 \\ 0.766 \\ 0.819 \\ 0.866 \\ 0.906 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

Hanging Wall West of Fault

$$R_{X5} := 2.5 \text{ km}$$

$$j := 1 \dots 7$$

2.5 KM West of Scarp

Lat: 40.656 Long:-111.837

$$R_X := R_{X5} = 2.500 \text{ km}$$

$$x := x15 \quad R_{JB15_j} := \max(R_X - x_j, 0) = \begin{bmatrix} 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$x := x12$$

$$R_{JB12_j} := \max(R_X - x_j, 0) = \begin{bmatrix} 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{bmatrix} \text{ km}$$

$$x := x18$$

$$R_{JB18_j} := \max(R_X - x_j, 0) = \begin{bmatrix} 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{bmatrix} \text{ km}$$

$$W := W_{15}$$

$$R_{RUP15_j} := \begin{cases} \frac{W_j}{\cos(\text{Dip}_j)} & \text{if } R_X \leq \frac{W_j}{\cos(\text{Dip}_j)} \\ R_X \cdot \sin(\text{Dip}_j) & \text{else} \\ \sqrt{R_X^2 + W_j^2 - 2 \cdot R_X \cdot W_j \cdot \cos(\text{Dip}_j)} & \end{cases} = \begin{bmatrix} 1.434 \\ 1.607 \\ 1.768 \\ 1.915 \\ 2.048 \\ 2.165 \\ 2.266 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$W := W_{12}$$

$$R_{RUP12_j} := \begin{cases} \frac{W_j}{\cos(\text{Dip}_j)} & \text{if } R_X \leq \frac{W_j}{\cos(\text{Dip}_j)} \\ R_X \cdot \sin(\text{Dip}_j) & \text{else} \\ \sqrt{R_X^2 + W_j^2 - 2 \cdot R_X \cdot W_j \cdot \cos(\text{Dip}_j)} & \end{cases} = \begin{bmatrix} 1.434 \\ 1.607 \\ 1.768 \\ 1.915 \\ 2.048 \\ 2.165 \\ 2.266 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$W := W_{18}$$

$$R_{RUP18_j} := \begin{cases} \frac{W_j}{\cos(\text{Dip}_j)} & \text{if } R_X \leq \frac{W_j}{\cos(\text{Dip}_j)} \\ R_X \cdot \sin(\text{Dip}_j) & \text{else} \\ \sqrt{R_X^2 + W_j^2 - 2 \cdot R_X \cdot W_j \cdot \cos(\text{Dip}_j)} & \end{cases} = \begin{bmatrix} 1.434 \\ 1.607 \\ 1.768 \\ 1.915 \\ 2.048 \\ 2.165 \\ 2.266 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$W_{15} = \begin{bmatrix} 26.152 \\ 23.336 \\ 21.213 \\ 19.581 \\ 18.312 \\ 17.321 \\ 16.551 \end{bmatrix} \text{ km} \quad W_{12} = \begin{bmatrix} 20.921 \\ 18.669 \\ 16.971 \\ 15.665 \\ 14.649 \\ 13.856 \\ 13.241 \end{bmatrix} \text{ km} \quad W_{18} = \begin{bmatrix} 31.382 \\ 28.003 \\ 25.456 \\ 23.497 \\ 21.974 \\ 20.785 \\ 19.861 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$R_X = 2.500 \text{ km}$$

$$R_{JB15} = \begin{bmatrix} 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{bmatrix} \text{ km} \quad R_{JB12} = \begin{bmatrix} 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{bmatrix} \text{ km} \quad R_{JB18} = \begin{bmatrix} 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$R_{RUP15} = \begin{bmatrix} 1.434 \\ 1.607 \\ 1.768 \\ 1.915 \\ 2.048 \\ 2.165 \\ 2.266 \end{bmatrix} \text{ km} \quad R_{RUP12} = \begin{bmatrix} 1.434 \\ 1.607 \\ 1.768 \\ 1.915 \\ 2.048 \\ 2.165 \\ 2.266 \end{bmatrix} \text{ km} \quad R_{RUP18} = \begin{bmatrix} 1.434 \\ 1.607 \\ 1.768 \\ 1.915 \\ 2.048 \\ 2.165 \\ 2.266 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

Hanging Wall West of Fault

$$R_{X5} := 2.5 \text{ km}$$

$j := 1 \dots 7$

2.5 KM West of Scarp

Lat: 40.656 Long:-111.837

$$R_X := R_{X5} = 2.500 \text{ km}$$

$$x := x15$$

$$R_{JB15_j} := \max(R_X - x_j, 0) = \begin{bmatrix} 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$x := x12$$

$$R_{JB12_j} := \max(R_X - x_j, 0) = \begin{bmatrix} 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{bmatrix} \text{ km}$$

$$x := x18$$

$$R_{JB18_j} := \max(R_X - x_j, 0) = \begin{bmatrix} 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{bmatrix} \text{ km}$$

$$W := W_{15}$$

$$R_{RUP15_j} := \begin{cases} \frac{W_j}{\cos(\text{Dip}_j)} & \text{if } R_X \leq \frac{W_j}{\cos(\text{Dip}_j)} \\ R_X \cdot \sin(\text{Dip}_j) & \text{else} \end{cases} = \begin{bmatrix} 1.434 \\ 1.607 \\ 1.768 \\ 1.915 \\ 2.048 \\ 2.165 \\ 2.266 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$W := W_{12}$$

$$R_{RUP12_j} := \begin{cases} \frac{W_j}{\cos(\text{Dip}_j)} & \text{if } R_X \leq \frac{W_j}{\cos(\text{Dip}_j)} \\ R_X \cdot \sin(\text{Dip}_j) & \text{else} \end{cases} = \begin{bmatrix} 1.434 \\ 1.607 \\ 1.768 \\ 1.915 \\ 2.048 \\ 2.165 \\ 2.266 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$W := W_{18}$$

$$R_{RUP18_j} := \begin{cases} \frac{W_j}{\cos(\text{Dip}_j)} & \text{if } R_X \leq \frac{W_j}{\cos(\text{Dip}_j)} \\ R_X \cdot \sin(\text{Dip}_j) & \text{else} \end{cases} = \begin{bmatrix} 1.434 \\ 1.607 \\ 1.768 \\ 1.915 \\ 2.048 \\ 2.165 \\ 2.266 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$W_{15} = \begin{bmatrix} 26.152 \\ 23.336 \\ 21.213 \\ 19.581 \\ 18.312 \\ 17.321 \\ 16.551 \end{bmatrix} \text{ km} \quad W_{12} = \begin{bmatrix} 20.921 \\ 18.669 \\ 16.971 \\ 15.665 \\ 14.649 \\ 13.856 \\ 13.241 \end{bmatrix} \text{ km} \quad W_{18} = \begin{bmatrix} 31.382 \\ 28.003 \\ 25.456 \\ 23.497 \\ 21.974 \\ 20.785 \\ 19.861 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$R_X = 2.500 \text{ km}$$

$$R_{JB15} = \begin{bmatrix} 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{bmatrix} \text{ km} \quad R_{JB12} = \begin{bmatrix} 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{bmatrix} \text{ km} \quad R_{JB18} = \begin{bmatrix} 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$R_{RUP15} = \begin{bmatrix} 1.434 \\ 1.607 \\ 1.768 \\ 1.915 \\ 2.048 \\ 2.165 \\ 2.266 \end{bmatrix} \text{ km} \quad R_{RUP12} = \begin{bmatrix} 1.434 \\ 1.607 \\ 1.768 \\ 1.915 \\ 2.048 \\ 2.165 \\ 2.266 \end{bmatrix} \text{ km} \quad R_{RUP18} = \begin{bmatrix} 1.434 \\ 1.607 \\ 1.768 \\ 1.915 \\ 2.048 \\ 2.165 \\ 2.266 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

Hanging Wall West of Fault

$$R_{X6} := 5 \text{ km}$$

$$j := 1 \dots 7$$

5 KM West of Scarp

Lat: 40.656 Long:-111.8656

$$R_X := R_{X6} = 5.000 \text{ km}$$

$$x := x15 \quad R_{JB15_j} := \max(R_X - x_j, 0) = \begin{bmatrix} 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$x := x12$$

$$R_{JB12_j} := \max(R_X - x_j, 0) = \begin{bmatrix} 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{bmatrix} \text{ km}$$

$$x := x18$$

$$R_{JB18_j} := \max(R_X - x_j, 0) = \begin{bmatrix} 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{bmatrix} \text{ km}$$

$$W := W_{15}$$

$$R_{RUP15_j} := \begin{cases} \frac{W_j}{\cos(\text{Dip}_j)} & \text{if } R_X \leq \frac{W_j}{\cos(\text{Dip}_j)} \\ R_X \cdot \sin(\text{Dip}_j) & \text{else} \\ \sqrt{R_X^2 + W_j^2 - 2 \cdot R_X \cdot W_j \cdot \cos(\text{Dip}_j)} & \end{cases} = \begin{bmatrix} 2.868 \\ 3.214 \\ 3.536 \\ 3.830 \\ 4.096 \\ 4.330 \\ 4.532 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$W := W_{12}$$

$$R_{RUP12_j} := \begin{cases} \frac{W_j}{\cos(\text{Dip}_j)} & \text{if } R_X \leq \frac{W_j}{\cos(\text{Dip}_j)} \\ R_X \cdot \sin(\text{Dip}_j) & \text{else} \\ \sqrt{R_X^2 + W_j^2 - 2 \cdot R_X \cdot W_j \cdot \cos(\text{Dip}_j)} & \end{cases} = \begin{bmatrix} 2.868 \\ 3.214 \\ 3.536 \\ 3.830 \\ 4.096 \\ 4.330 \\ 4.532 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$W := W_{18}$$

$$R_{RUP18_j} := \begin{cases} \frac{W_j}{\cos(\text{Dip}_j)} & \text{if } R_X \leq \frac{W_j}{\cos(\text{Dip}_j)} \\ R_X \cdot \sin(\text{Dip}_j) & \text{else} \\ \sqrt{R_X^2 + W_j^2 - 2 \cdot R_X \cdot W_j \cdot \cos(\text{Dip}_j)} & \end{cases} = \begin{bmatrix} 2.868 \\ 3.214 \\ 3.536 \\ 3.830 \\ 4.096 \\ 4.330 \\ 4.532 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$W_{15} = \begin{bmatrix} 26.152 \\ 23.336 \\ 21.213 \\ 19.581 \\ 18.312 \\ 17.321 \\ 16.551 \end{bmatrix} \text{ km} \quad W_{12} = \begin{bmatrix} 20.921 \\ 18.669 \\ 16.971 \\ 15.665 \\ 14.649 \\ 13.856 \\ 13.241 \end{bmatrix} \text{ km} \quad W_{18} = \begin{bmatrix} 31.382 \\ 28.003 \\ 25.456 \\ 23.497 \\ 21.974 \\ 20.785 \\ 19.861 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$R_X = 5.000 \text{ km}$$

$$R_{JB15} = \begin{bmatrix} 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{bmatrix} \text{ km} \quad R_{JB12} = \begin{bmatrix} 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{bmatrix} \text{ km} \quad R_{JB18} = \begin{bmatrix} 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$R_{RUP15} = \begin{bmatrix} 2.868 \\ 3.214 \\ 3.536 \\ 3.830 \\ 4.096 \\ 4.330 \\ 4.532 \end{bmatrix} \text{ km} \quad R_{RUP12} = \begin{bmatrix} 2.868 \\ 3.214 \\ 3.536 \\ 3.830 \\ 4.096 \\ 4.330 \\ 4.532 \end{bmatrix} \text{ km} \quad R_{RUP18} = \begin{bmatrix} 2.868 \\ 3.214 \\ 3.536 \\ 3.830 \\ 4.096 \\ 4.330 \\ 4.532 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

Hanging Wall West of Fault

$$R_{X7} := 10 \text{ km}$$

$$j := 1 \dots 7$$

10 KM West of Scarp

Lat: 40.656 Long:-111.9256

$$R_X := R_{X7} = 10.000 \text{ km}$$

$$x := x15 \quad R_{JB15_j} := \max(R_X - x_j, 0) = \begin{bmatrix} 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 1.340 \\ 3.005 \\ 0.000 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$x := x12$$

$$R_{JB12_j} := \max(R_X - x_j, 0) = \begin{bmatrix} 0.000 \\ 1.598 \\ 3.072 \\ 4.404 \end{bmatrix} \text{ km}$$

$$x := x18$$

$$R_{JB18_j} := \max(R_X - x_j, 0) = \begin{bmatrix} 0.000 \\ 0.000 \\ 0.000 \\ 1.606 \end{bmatrix} \text{ km}$$

$$W := W_{15}$$

$$R_{RUP15_j} := \begin{cases} \frac{W_j}{\cos(\text{Dip}_j)} & \text{if } R_X \leq \frac{W_j}{\cos(\text{Dip}_j)} \\ R_X \cdot \sin(\text{Dip}_j) & \text{else} \\ \sqrt{R_X^2 + W_j^2 - 2 \cdot R_X \cdot W_j \cdot \cos(\text{Dip}_j)} & \end{cases} = \begin{bmatrix} 5.736 \\ 6.428 \\ 7.071 \\ 7.660 \\ 8.192 \\ 8.660 \\ 9.063 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$W := W_{12}$$

$$R_{RUP12_j} := \begin{cases} \frac{W_j}{\cos(\text{Dip}_j)} & \text{if } R_X \leq \frac{W_j}{\cos(\text{Dip}_j)} \\ R_X \cdot \sin(\text{Dip}_j) & \text{else} \\ \sqrt{R_X^2 + W_j^2 - 2 \cdot R_X \cdot W_j \cdot \cos(\text{Dip}_j)} & \end{cases} = \begin{bmatrix} 5.736 \\ 6.428 \\ 7.071 \\ 7.660 \\ 8.192 \\ 8.660 \\ 9.063 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$W := W_{18}$$

$$R_{RUP18_j} := \begin{cases} \frac{W_j}{\cos(\text{Dip}_j)} & \text{if } R_X \leq \frac{W_j}{\cos(\text{Dip}_j)} \\ R_X \cdot \sin(\text{Dip}_j) & \text{else} \\ \sqrt{R_X^2 + W_j^2 - 2 \cdot R_X \cdot W_j \cdot \cos(\text{Dip}_j)} & \end{cases} = \begin{bmatrix} 5.736 \\ 6.428 \\ 7.071 \\ 7.660 \\ 8.192 \\ 8.660 \\ 9.063 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$W_{15} = \begin{bmatrix} 26.152 \\ 23.336 \\ 21.213 \\ 19.581 \\ 18.312 \\ 17.321 \\ 16.551 \end{bmatrix} \text{ km} \quad W_{12} = \begin{bmatrix} 20.921 \\ 18.669 \\ 16.971 \\ 15.665 \\ 14.649 \\ 13.856 \\ 13.241 \end{bmatrix} \text{ km} \quad W_{18} = \begin{bmatrix} 31.382 \\ 28.003 \\ 25.456 \\ 23.497 \\ 21.974 \\ 20.785 \\ 19.861 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$R_X = 10.000 \text{ km}$$

$$R_{JB15} = \begin{bmatrix} 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 1.340 \\ 3.005 \end{bmatrix} \text{ km} \quad R_{JB12} = \begin{bmatrix} 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 1.598 \\ 3.072 \\ 4.404 \end{bmatrix} \text{ km} \quad R_{JB18} = \begin{bmatrix} 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 1.606 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$R_{RUP15} = \begin{bmatrix} 5.736 \\ 6.428 \\ 7.071 \\ 7.660 \\ 8.192 \\ 8.660 \\ 9.063 \end{bmatrix} \text{ km} \quad R_{RUP12} = \begin{bmatrix} 5.736 \\ 6.428 \\ 7.071 \\ 7.660 \\ 8.192 \\ 8.660 \\ 9.063 \end{bmatrix} \text{ km} \quad R_{RUP18} = \begin{bmatrix} 5.736 \\ 6.428 \\ 7.071 \\ 7.660 \\ 8.192 \\ 8.660 \\ 9.063 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

Hanging Wall West of Fault

$$R_{X8} := 15 \text{ km}$$

$$j := 1 .. 7$$

15 KM West of Scarp

Lat: 40.656 Long:-111.9848

$$R_X := R_{X8} = 15.000 \text{ km}$$

$$x := x_{15} \quad R_{JB15_j} := \max(R_X - x_j, 0) = \begin{bmatrix} 0.000 \\ 0.000 \\ 0.000 \\ 2.414 \\ 4.497 \\ 0.000 \\ 6.340 \\ 0.699 \\ 8.005 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$x := x_{12}$$

$$R_{JB12_j} := \max(R_X - x_j, 0) = \begin{bmatrix} 3.000 \\ 4.931 \\ 6.598 \\ 8.072 \\ 9.404 \end{bmatrix} \text{ km}$$

$$x := x_{18}$$

$$R_{JB18_j} := \max(R_X - x_j, 0) = \begin{bmatrix} 0.000 \\ 2.396 \\ 4.608 \\ 6.606 \end{bmatrix} \text{ km}$$

$$W := W_{15}$$

$$R_{RUP15_j} := \begin{cases} \frac{W_j}{\cos(\text{Dip}_j)} & \text{if } R_X \leq \frac{W_j}{\cos(\text{Dip}_j)} \\ R_X \cdot \sin(\text{Dip}_j) & \text{else} \\ \sqrt{R_X^2 + W_j^2 - 2 \cdot R_X \cdot W_j \cdot \cos(\text{Dip}_j)} \end{cases} = \begin{bmatrix} 8.604 \\ 9.642 \\ 10.607 \\ 11.491 \\ 12.287 \\ 12.990 \\ 13.595 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$W := W_{12}$$

$$R_{RUP12_j} := \begin{cases} \frac{W_j}{\cos(\text{Dip}_j)} & \text{if } R_X \leq \frac{W_j}{\cos(\text{Dip}_j)} \\ R_X \cdot \sin(\text{Dip}_j) & \text{else} \\ \sqrt{R_X^2 + W_j^2 - 2 \cdot R_X \cdot W_j \cdot \cos(\text{Dip}_j)} \end{cases} = \begin{bmatrix} 8.604 \\ 9.642 \\ 10.607 \\ 11.491 \\ 12.287 \\ 12.990 \\ 13.595 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$W := W_{18}$$

$$R_{RUP18_j} := \begin{cases} \frac{W_j}{\cos(\text{Dip}_j)} & \text{if } R_X \leq \frac{W_j}{\cos(\text{Dip}_j)} \\ R_X \cdot \sin(\text{Dip}_j) & \text{else} \\ \sqrt{R_X^2 + W_j^2 - 2 \cdot R_X \cdot W_j \cdot \cos(\text{Dip}_j)} \end{cases} = \begin{bmatrix} 8.604 \\ 9.642 \\ 10.607 \\ 11.491 \\ 12.287 \\ 12.990 \\ 13.595 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$W_{15} = \begin{bmatrix} 26.152 \\ 23.336 \\ 21.213 \\ 19.581 \\ 18.312 \\ 17.321 \\ 16.551 \end{bmatrix} \text{ km} \quad W_{12} = \begin{bmatrix} 20.921 \\ 18.669 \\ 16.971 \\ 15.665 \\ 14.649 \\ 13.856 \\ 13.241 \end{bmatrix} \text{ km} \quad W_{18} = \begin{bmatrix} 31.382 \\ 28.003 \\ 25.456 \\ 23.497 \\ 21.974 \\ 20.785 \\ 19.861 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$R_X = 15.000 \text{ km}$$

$$R_{JB15} = \begin{bmatrix} 0.000 \\ 0.000 \\ 0.000 \\ 2.414 \\ 4.497 \\ 6.340 \\ 8.005 \end{bmatrix} \text{ km} \quad R_{JB12} = \begin{bmatrix} 0.000 \\ 0.699 \\ 3.000 \\ 4.931 \\ 6.598 \\ 8.072 \\ 9.404 \end{bmatrix} \text{ km} \quad R_{JB18} = \begin{bmatrix} 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 2.396 \\ 4.608 \\ 6.606 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$R_{RUP15} = \begin{bmatrix} 8.604 \\ 9.642 \\ 10.607 \\ 11.491 \\ 12.287 \\ 12.990 \\ 13.595 \end{bmatrix} \text{ km} \quad R_{RUP12} = \begin{bmatrix} 8.604 \\ 9.642 \\ 10.607 \\ 11.491 \\ 12.287 \\ 12.990 \\ 13.595 \end{bmatrix} \text{ km} \quad R_{RUP18} = \begin{bmatrix} 8.604 \\ 9.642 \\ 10.607 \\ 11.491 \\ 12.287 \\ 12.990 \\ 13.595 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

Hanging Wall West of Fault

$$R_{X8} := 20 \text{ km}$$

$j := 1 \dots 7$

20 KM West of Scarp

Lat: 40.656 Long:-112.0440

$$R_X := R_{X8} = 20.000 \text{ km}$$

$x := x_{15}$

$$R_{JB15_j} := \max(R_X - x_j, 0) = \begin{bmatrix} 0.000 \\ 2.124 \\ 5.000 \\ 7.414 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \end{bmatrix} \text{ deg}$$

$$\begin{bmatrix} 9.497 \\ 2.862 \\ 11.340 \\ 5.699 \end{bmatrix} \quad \begin{bmatrix} 55.000 \\ 60.000 \\ 65.000 \end{bmatrix}$$

$$\begin{bmatrix} 13.005 \\ 8.000 \end{bmatrix}$$

$x := x_{12}$

$$R_{JB12_j} := \max(R_X - x_j, 0) = \begin{bmatrix} 9.931 \\ 11.598 \\ 13.072 \\ 14.404 \end{bmatrix} \text{ km}$$

$$\begin{bmatrix} 0.000 \\ 0.000 \\ 2.000 \end{bmatrix}$$

$$x := x_{18}$$

$$R_{JB18_j} := \max(R_X - x_j, 0) = \begin{bmatrix} 4.896 \\ 7.396 \\ 9.608 \\ 11.606 \end{bmatrix} \text{ km}$$

$W := W_{15}$

$$R_{RUP15_j} := \begin{cases} \frac{W_j}{\cos(\text{Dip}_j)} & \text{if } R_X \leq \frac{W_j}{\cos(\text{Dip}_j)} \\ R_X \cdot \sin(\text{Dip}_j) & \text{else} \\ \sqrt{R_X^2 + W_j^2 - 2 \cdot R_X \cdot W_j \cdot \cos(\text{Dip}_j)} & \end{cases} = \begin{bmatrix} 11.472 \\ 12.856 \\ 14.142 \\ 15.321 \\ 16.383 \\ 17.321 \\ 18.126 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$W := W_{12}$

$$R_{RUP12_j} := \begin{cases} \frac{W_j}{\cos(\text{Dip}_j)} & \text{if } R_X \leq \frac{W_j}{\cos(\text{Dip}_j)} \\ R_X \cdot \sin(\text{Dip}_j) & \text{else} \\ \sqrt{R_X^2 + W_j^2 - 2 \cdot R_X \cdot W_j \cdot \cos(\text{Dip}_j)} & \end{cases} = \begin{bmatrix} 11.472 \\ 12.856 \\ 14.142 \\ 15.321 \\ 16.383 \\ 17.321 \\ 18.126 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$W := W_{18}$

$$R_{RUP18_j} := \begin{cases} \frac{W_j}{\cos(\text{Dip}_j)} & \text{if } R_X \leq \frac{W_j}{\cos(\text{Dip}_j)} \\ R_X \cdot \sin(\text{Dip}_j) & \text{else} \\ \sqrt{R_X^2 + W_j^2 - 2 \cdot R_X \cdot W_j \cdot \cos(\text{Dip}_j)} & \end{cases} = \begin{bmatrix} 11.472 \\ 12.856 \\ 14.142 \\ 15.321 \\ 16.383 \\ 17.321 \\ 18.126 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$W_{15} = \begin{bmatrix} 26.152 \\ 23.336 \\ 21.213 \\ 19.581 \\ 18.312 \\ 17.321 \\ 16.551 \end{bmatrix} \text{ km} \quad W_{12} = \begin{bmatrix} 20.921 \\ 18.669 \\ 16.971 \\ 15.665 \\ 14.649 \\ 13.856 \\ 13.241 \end{bmatrix} \text{ km} \quad W_{18} = \begin{bmatrix} 31.382 \\ 28.003 \\ 25.456 \\ 23.497 \\ 21.974 \\ 20.785 \\ 19.861 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$R_X = 20.000 \text{ km}$$

$$R_{JB15} = \begin{bmatrix} 0.000 \\ 2.124 \\ 5.000 \\ 7.414 \\ 9.497 \\ 11.340 \\ 13.005 \end{bmatrix} \text{ km} \quad R_{JB12} = \begin{bmatrix} 2.862 \\ 5.699 \\ 8.000 \\ 9.931 \\ 11.598 \\ 13.072 \\ 14.404 \end{bmatrix} \text{ km} \quad R_{JB18} = \begin{bmatrix} 0.000 \\ 0.000 \\ 2.000 \\ 4.896 \\ 7.396 \\ 9.608 \\ 11.606 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$

$$R_{RUP15} = \begin{bmatrix} 11.472 \\ 12.856 \\ 14.142 \\ 15.321 \\ 16.383 \\ 17.321 \\ 18.126 \end{bmatrix} \text{ km} \quad R_{RUP12} = \begin{bmatrix} 11.472 \\ 12.856 \\ 14.142 \\ 15.321 \\ 16.383 \\ 17.321 \\ 18.126 \end{bmatrix} \text{ km} \quad R_{RUP18} = \begin{bmatrix} 11.472 \\ 12.856 \\ 14.142 \\ 15.321 \\ 16.383 \\ 17.321 \\ 18.126 \end{bmatrix} \text{ km} \quad \text{Dip} = \begin{bmatrix} 35.000 \\ 40.000 \\ 45.000 \\ 50.000 \\ 55.000 \\ 60.000 \\ 65.000 \end{bmatrix} \text{ deg}$$



Site-Specific Performance-Based Seismic Design Ground Motions: Case Study

Ivan Wong and Patricia Thomas

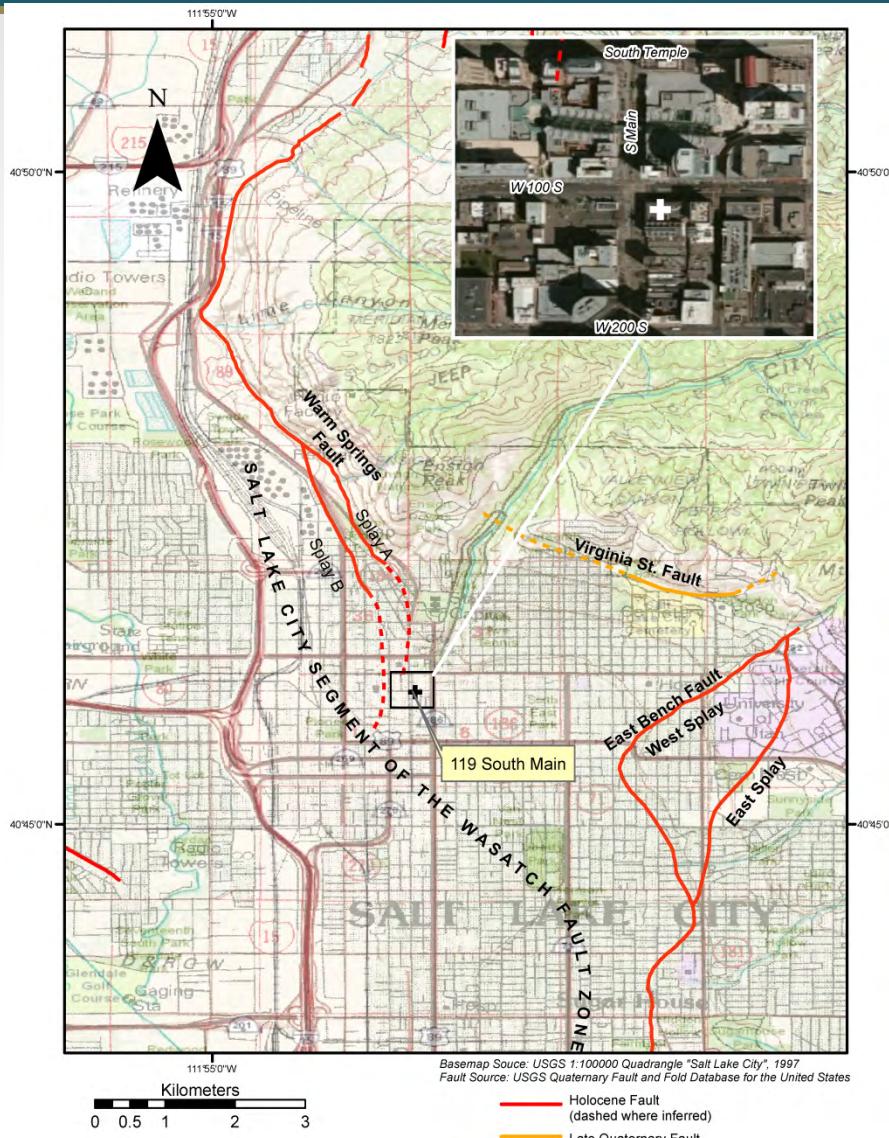
Meeting of the Utah Ground Shaking Working Group

Salt Lake City, UT
13 February 2018

Introduction

- Site-specific probabilistic and deterministic seismic hazard analyses were performed for the 111 Main building in downtown Salt Lake City
- Design criteria were developed in accordance with ASCE 7-10, the IBC, and the Tall Building Initiative Guidelines for Performance-Based Seismic Design of Tall Buildings
- Horizontal and vertical MCEr spectra were computed (geometric mean – no maximum component).
- Seven sets of three-component time histories were developed.

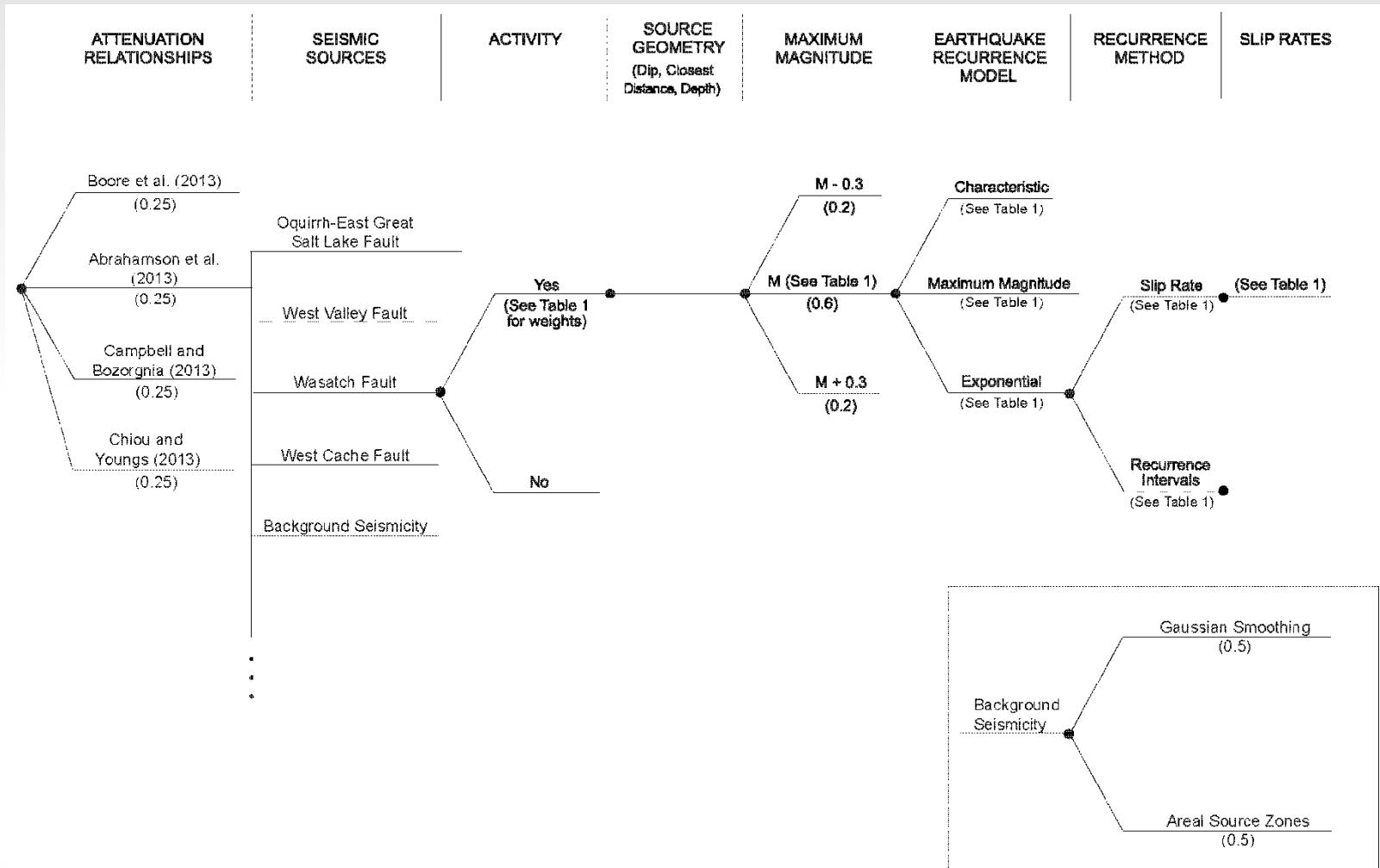
Site Vicinity Map



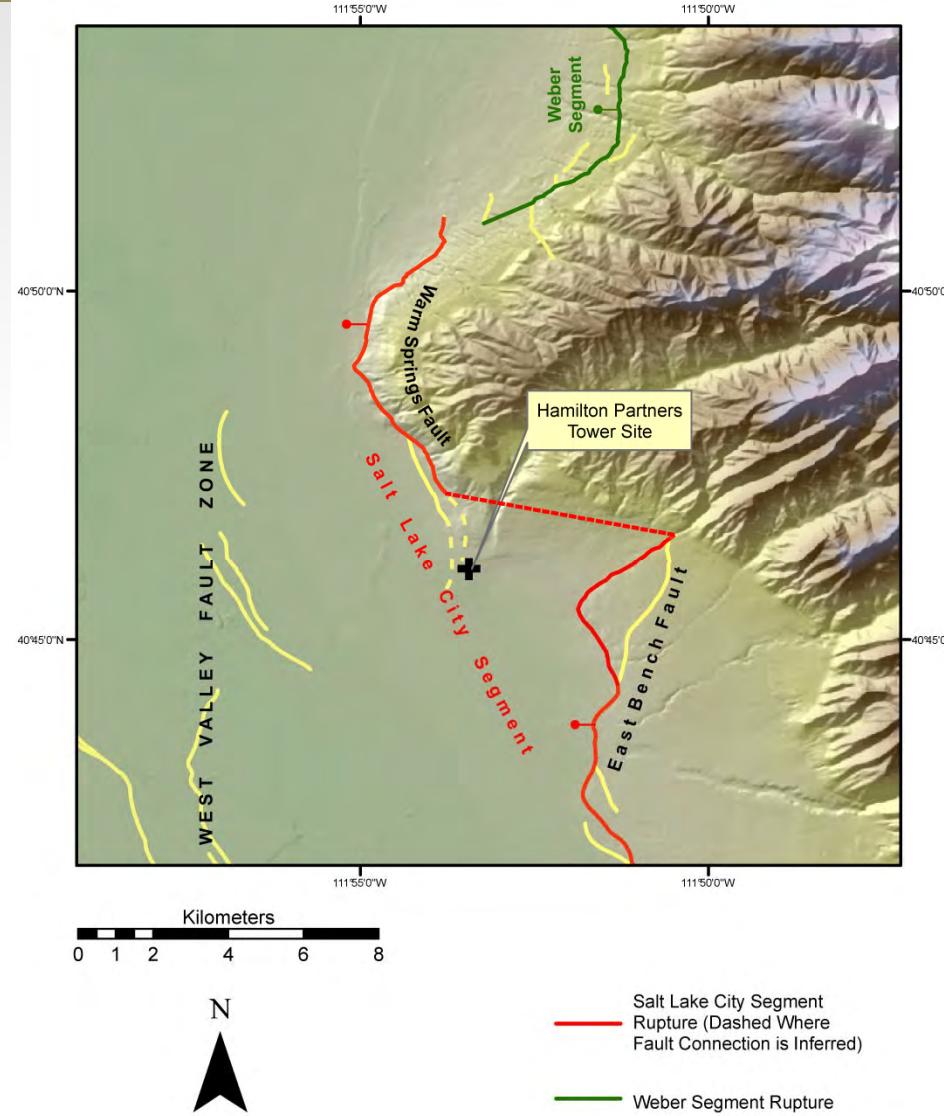
Issues

- Rupture scenarios for the Salt Lake City segment in downtown Salt Lake City including the West Valley fault zone
- Effects of the near-surface geology
- Effects of the Salt Lake Basin
- Effects of forward rupture directivity on normal faults
- Surface faulting hazard in downtown Salt Lake City
- Accounting for the elapsed time since the last large earthquake on the Salt Lake City segment (Patricia's talk)

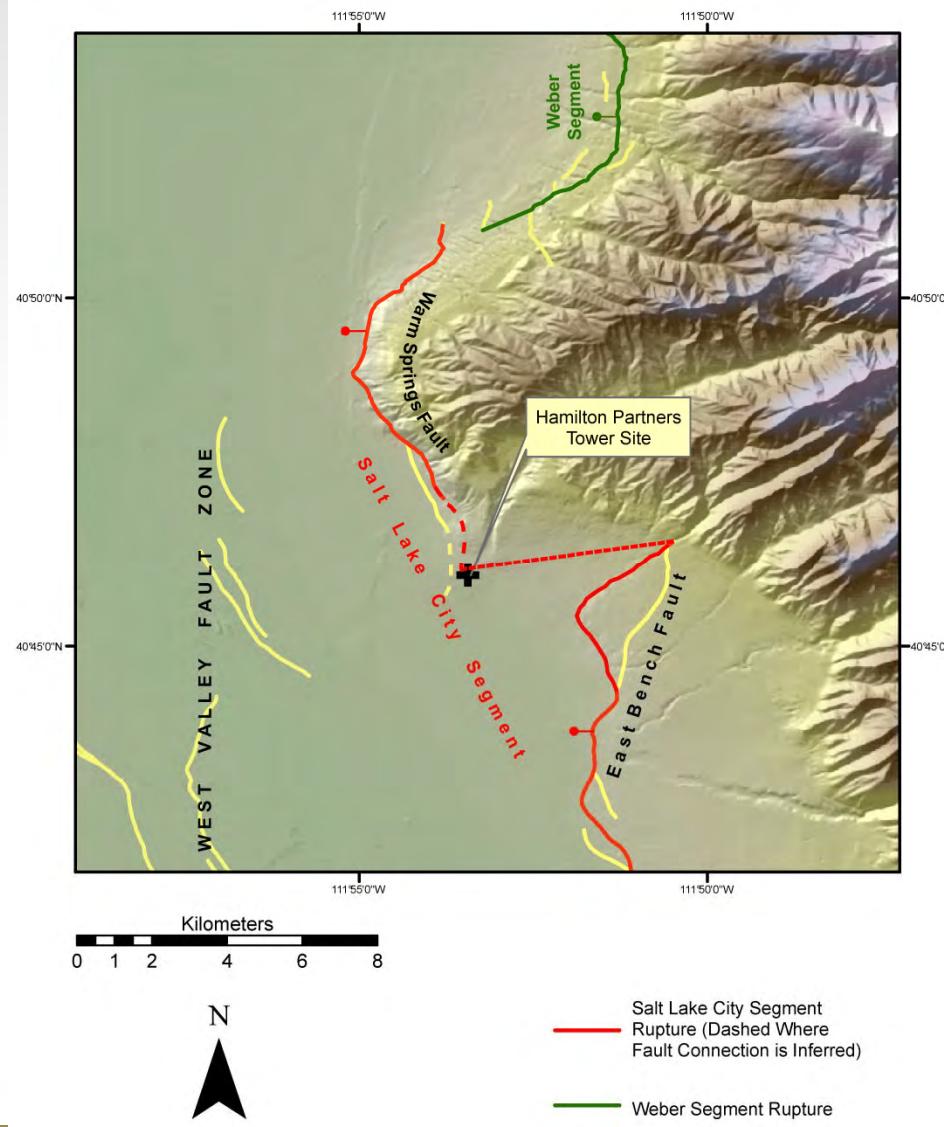
Seismic Hazard Model Logic Tree



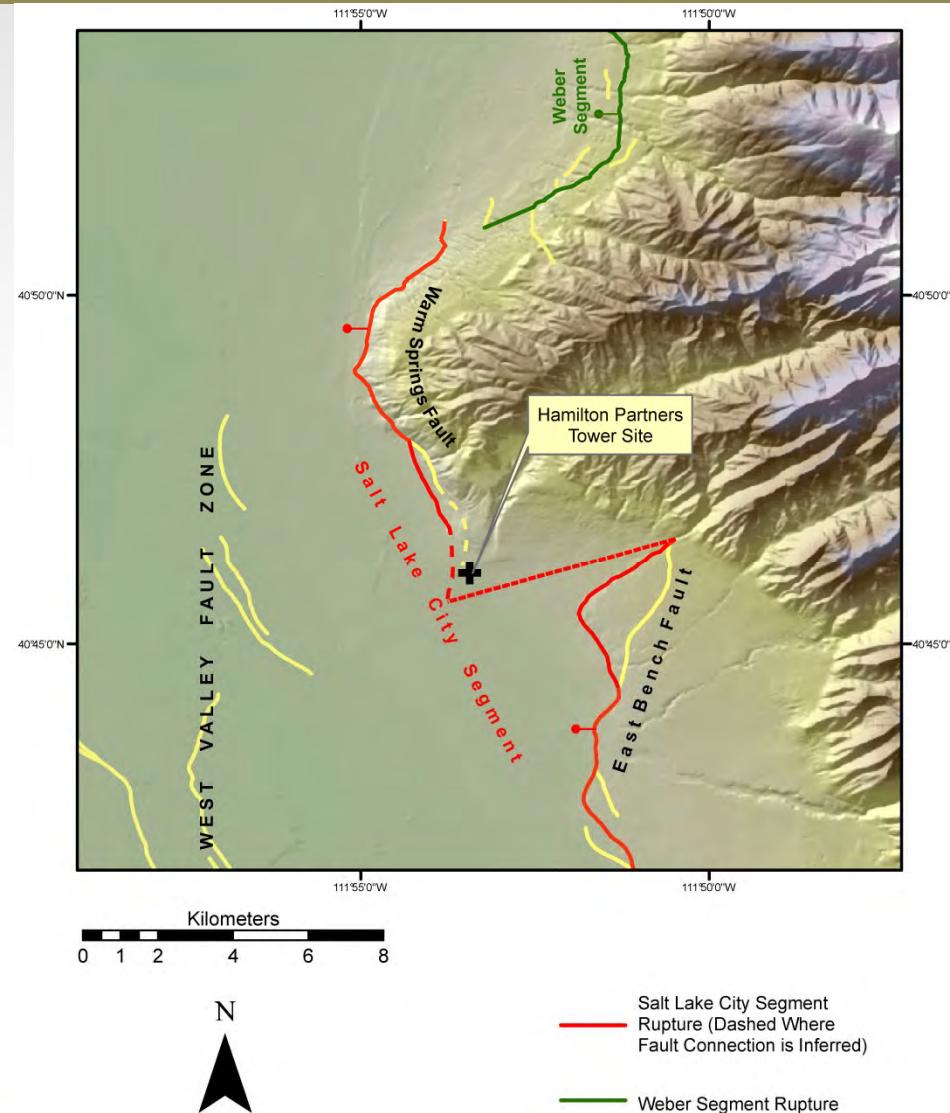
Rupture Scenario A for the East Bench - Warm Springs Faults Stepover Zone



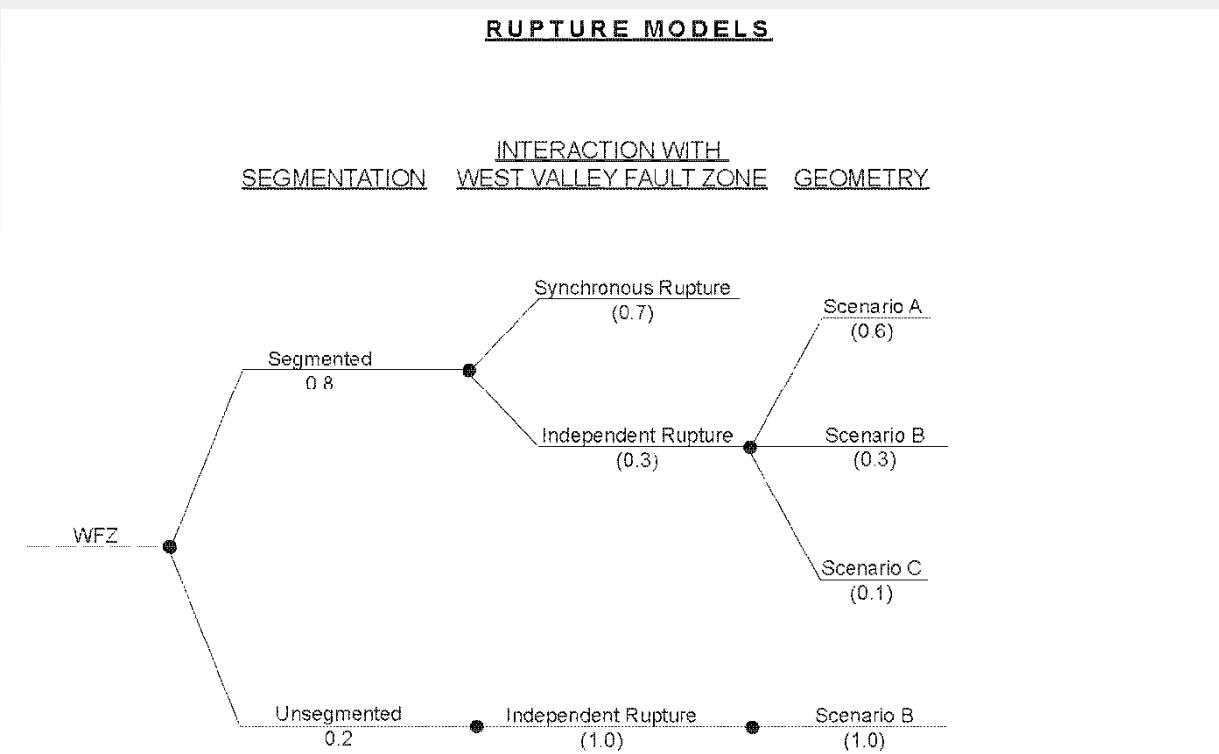
Rupture Scenario B for the East Bench - Warm Springs Faults Stepover Zone



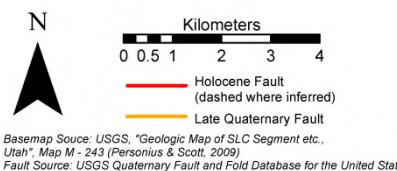
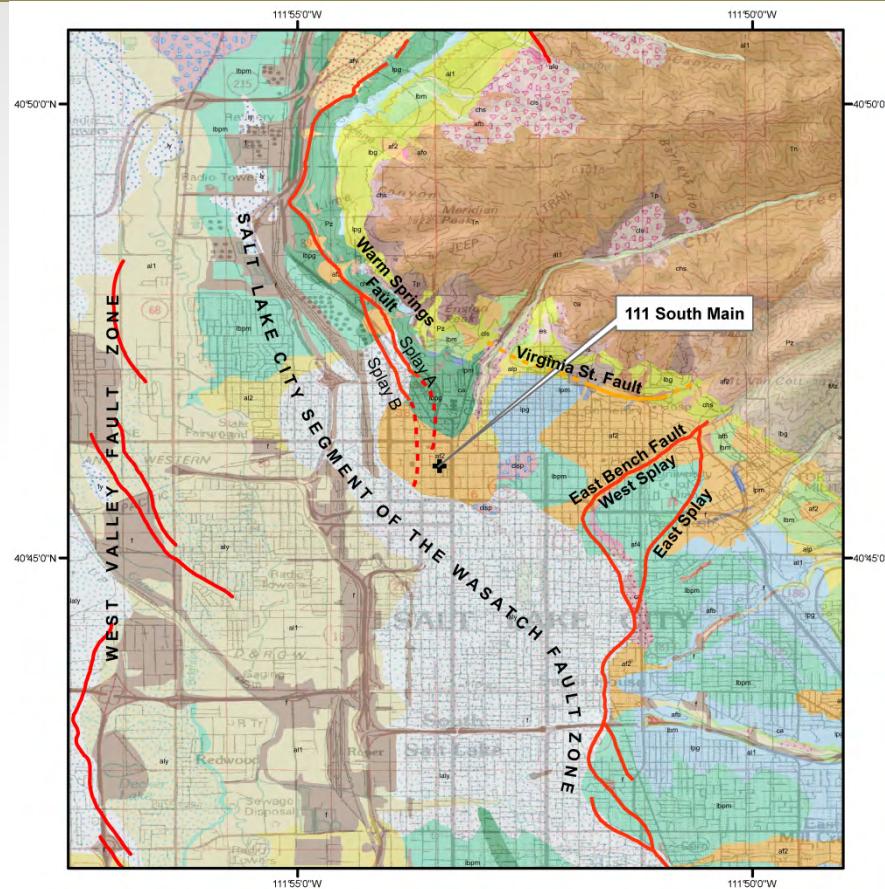
Rupture Scenario C for the East Bench - Warm Springs Faults Stepover Zone



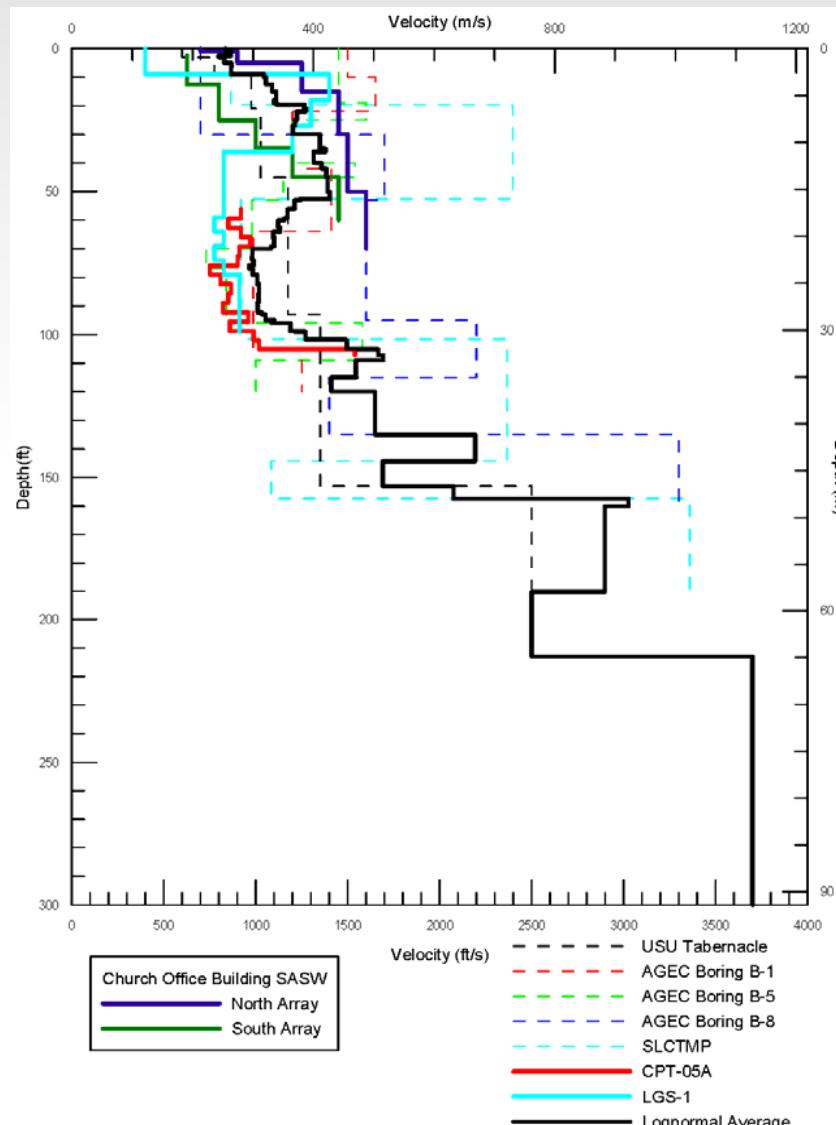
Logic Tree for Wasatch Fault Zone Rupture Models



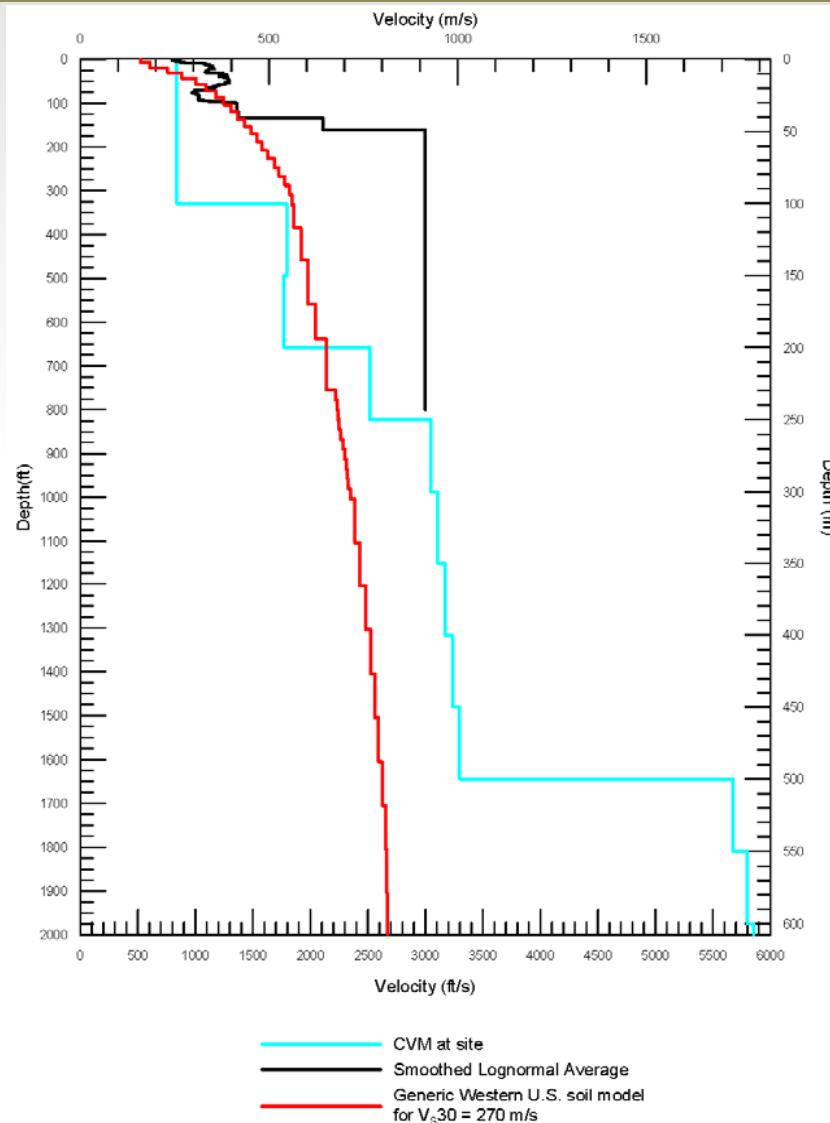
Surficial Geology in Salt Lake City



V_s Profiles for Downtown Salt Lake City

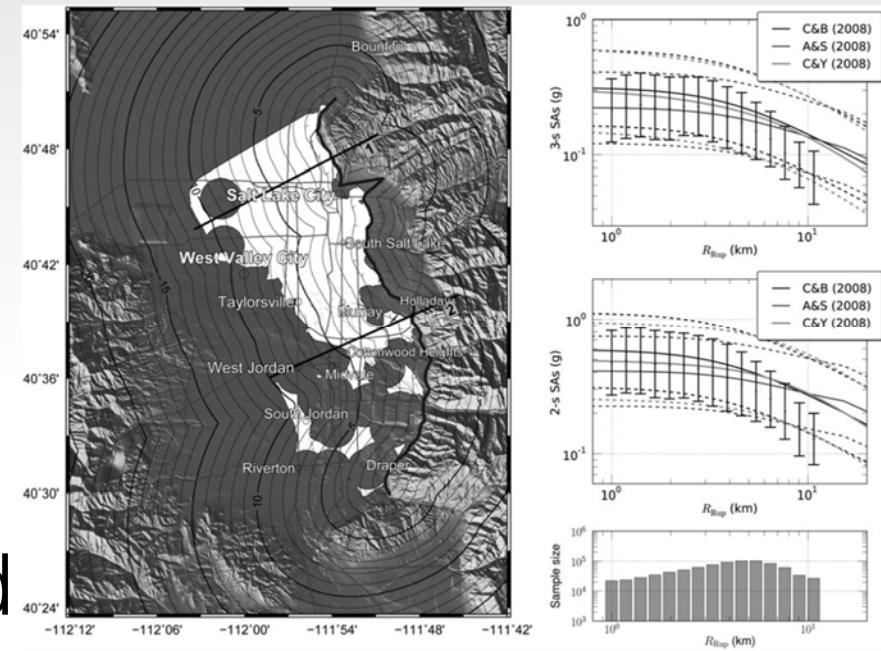


Basecase Vs Profile and Generic Soil Model Used in Site Response Analysis

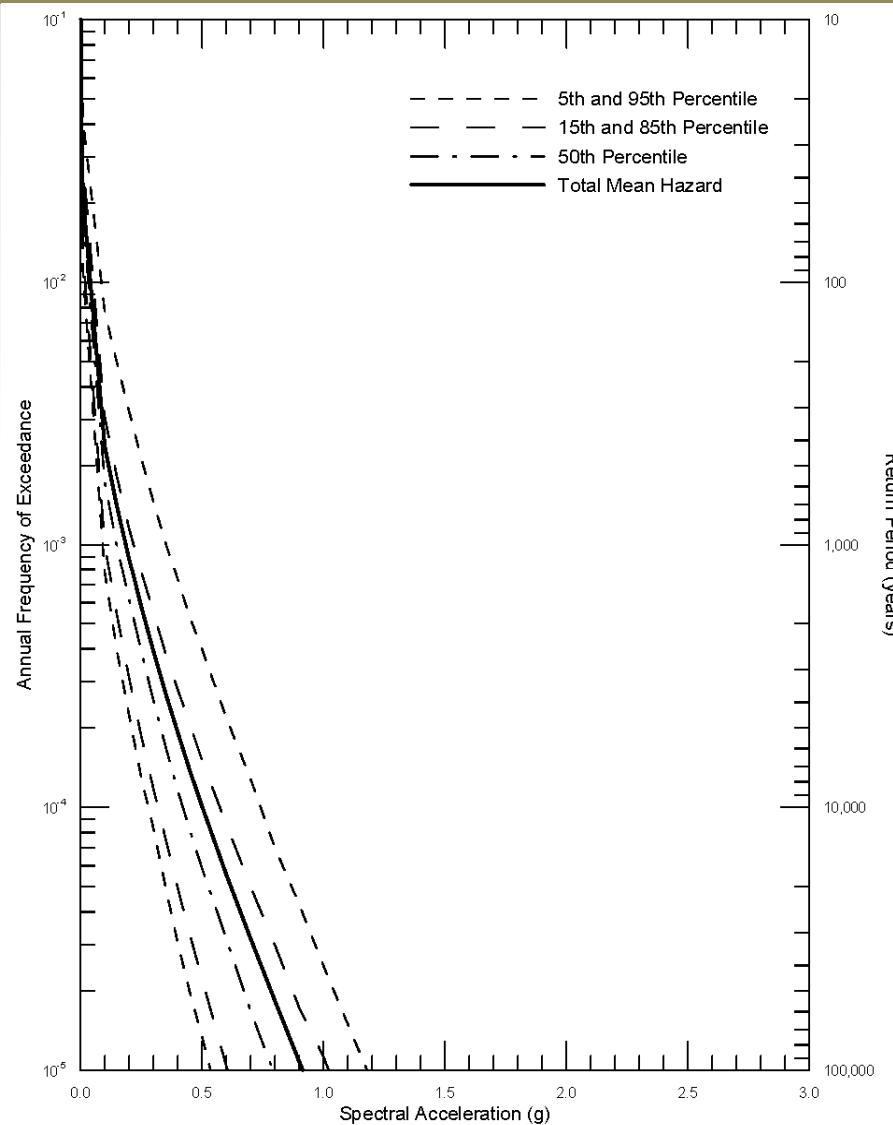


Basin Effects

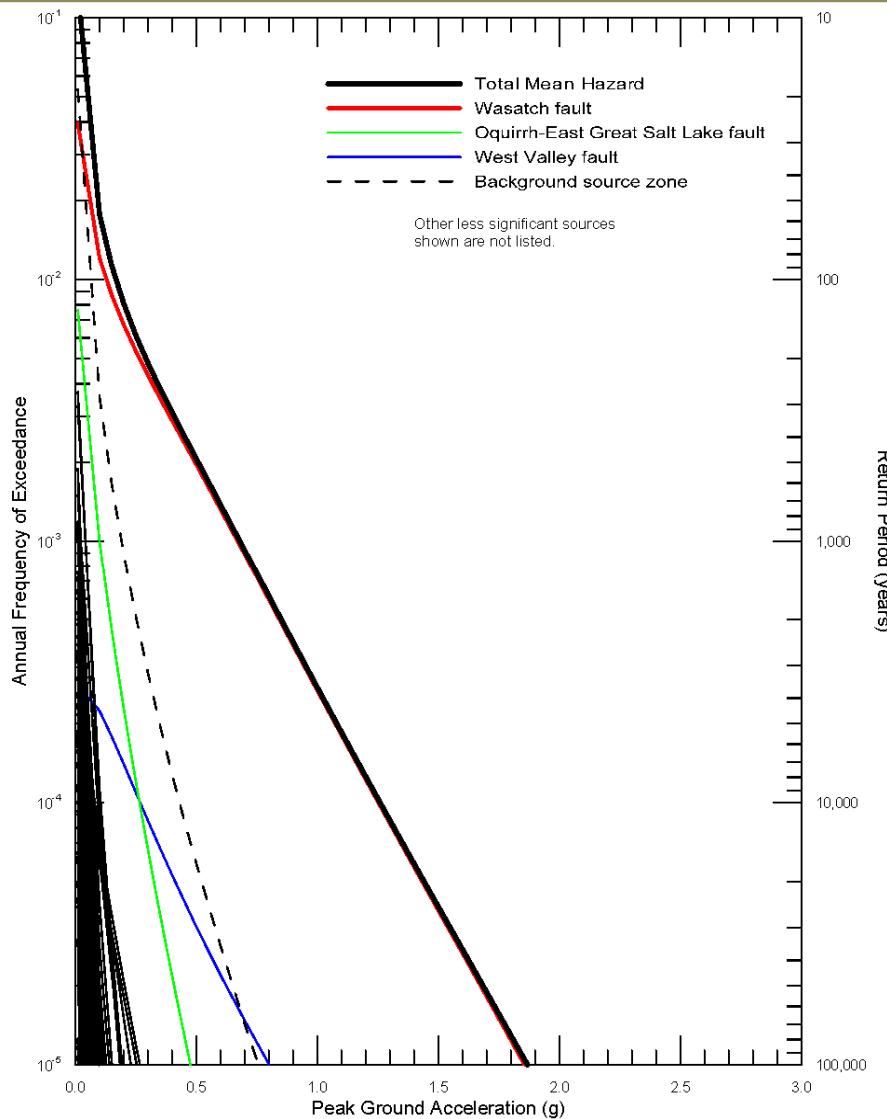
- Basin modeling by Roten et al. (2011) indicate that the NGA-West1 models capture on average the amplification effects of the Salt Lake Basin on long-period ground motions.
- X



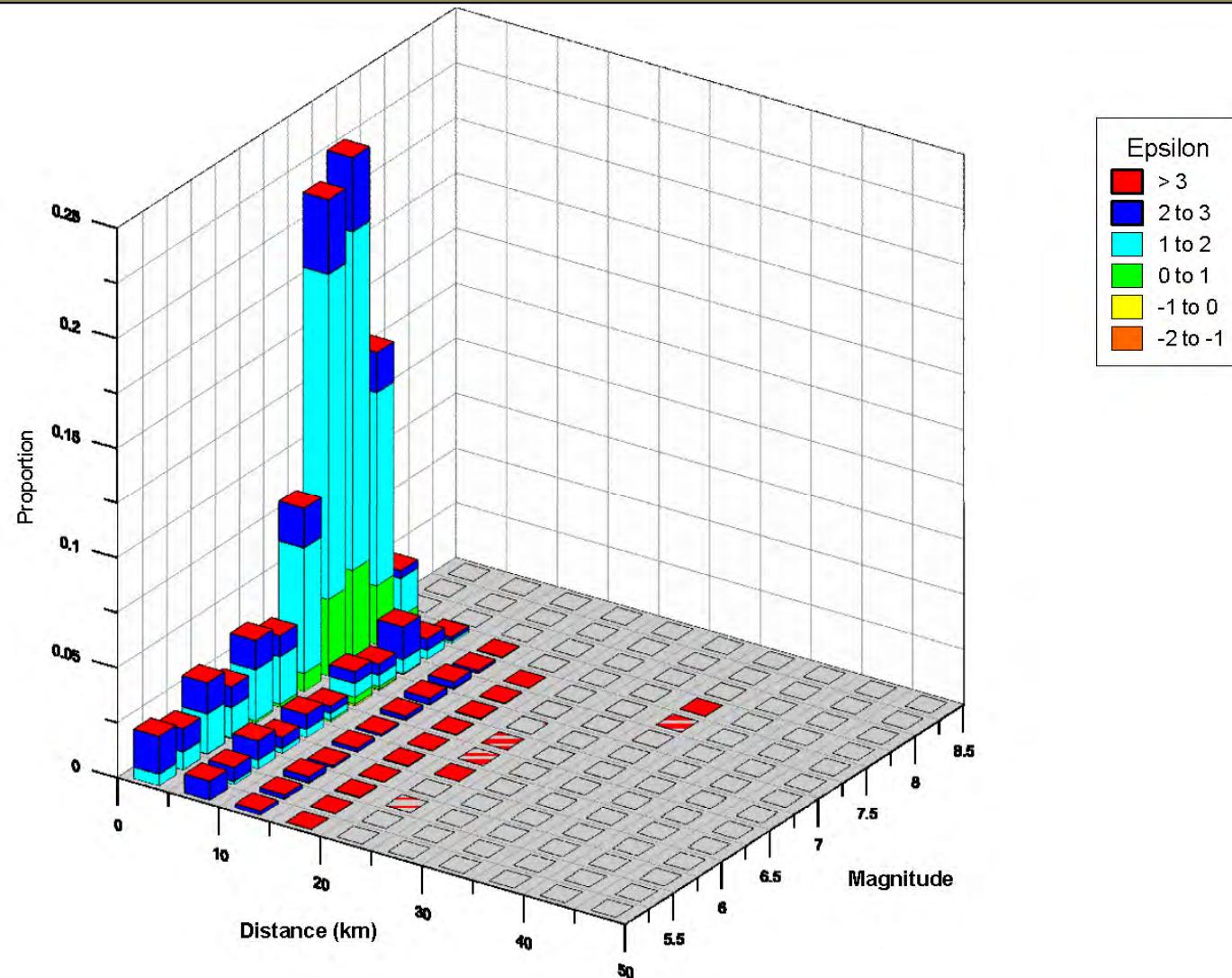
Seismic Hazard Curves for 4.0 Sec Horizontal Spectral Acceleration



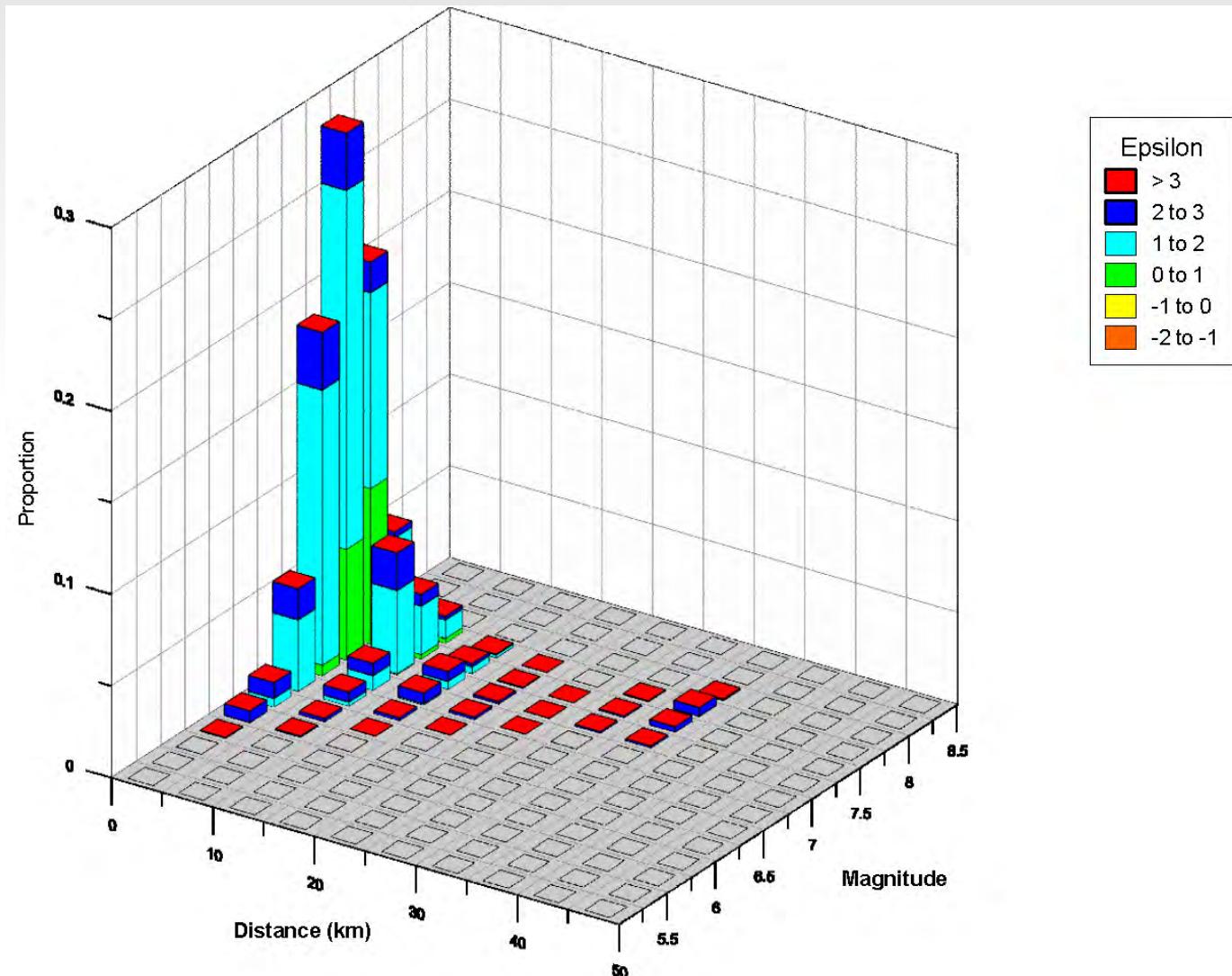
Seismic Source Contributions to Mean Peak Horizontal Acceleration Hazard



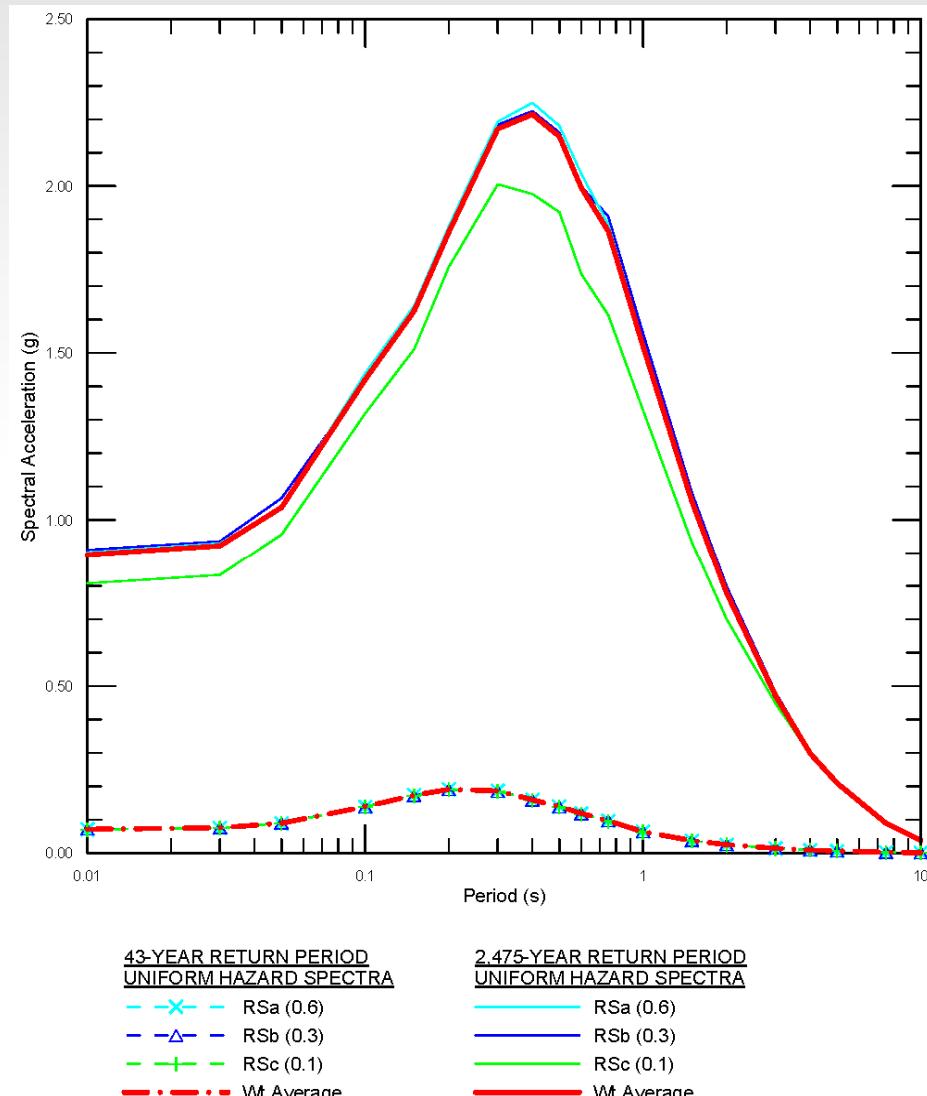
Magnitude and Distance Contributions to the Mean Peak Horizontal Acceleration Hazard at 2,475-Year Return Period



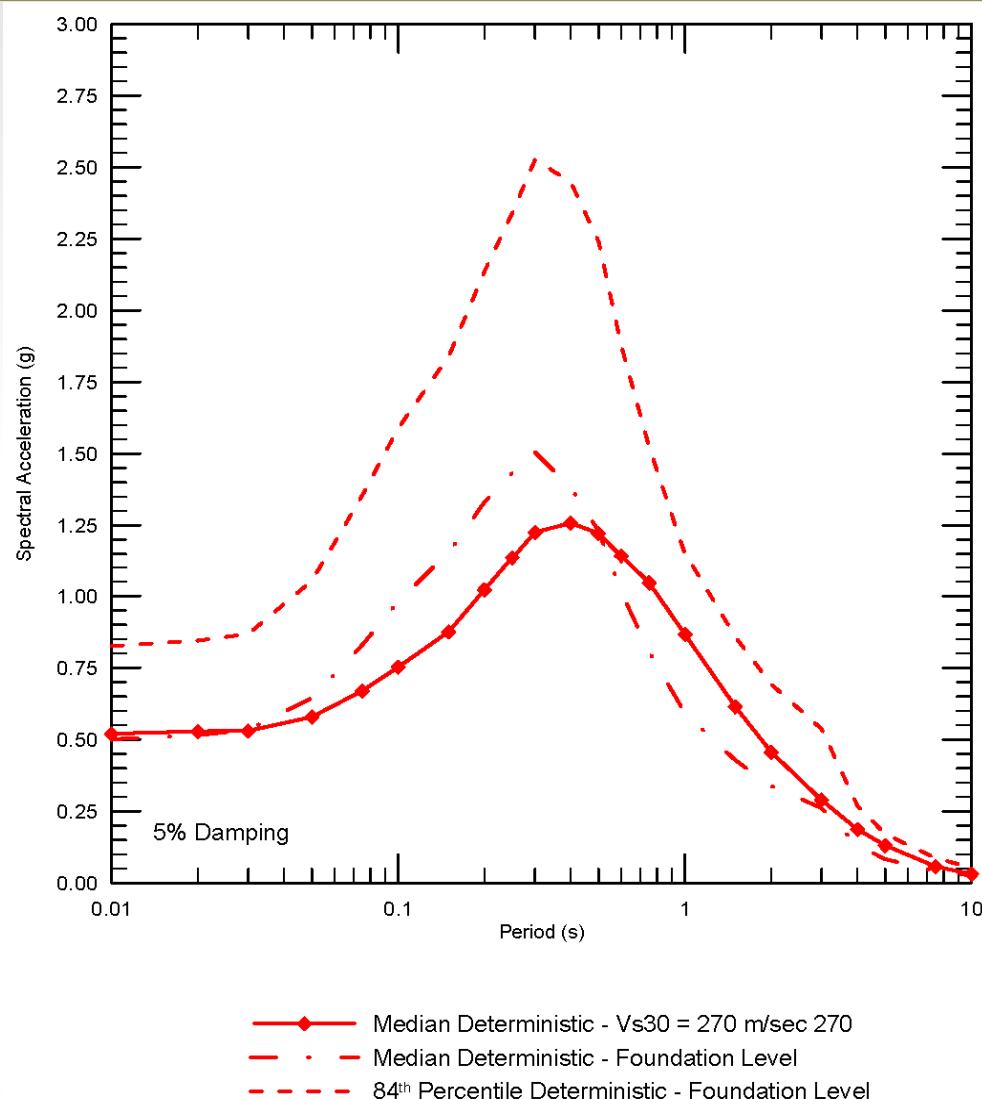
Magnitude and Distance Contributions to the Mean 4.0 Sec Horizontal Spectral Acceleration Hazard at 2,475-Year Return Period



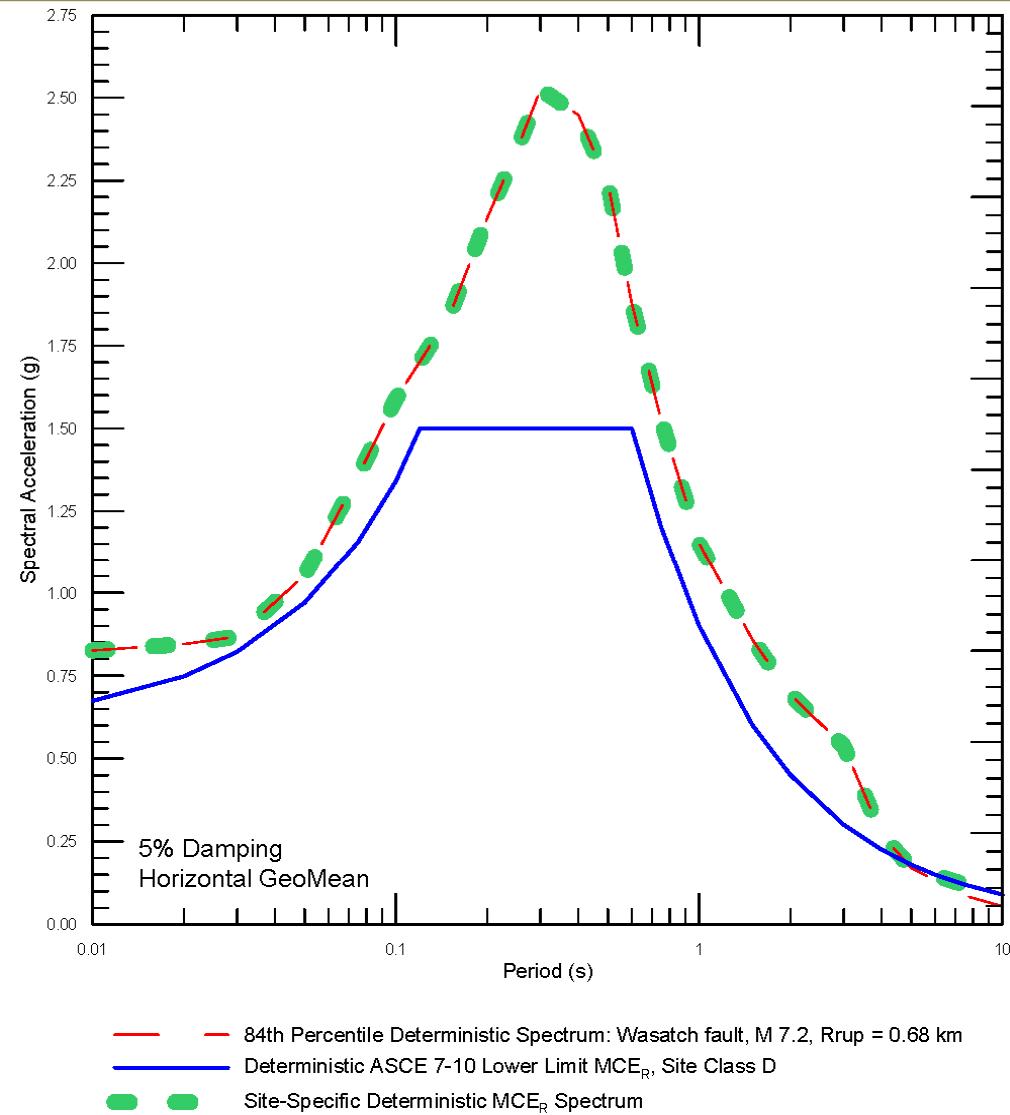
Sensitivity to East Bench-Warm Springs Faults Stepover – 5%-Damped Uniform Hazard Spectra at 43- and 2,475-Year Return Periods



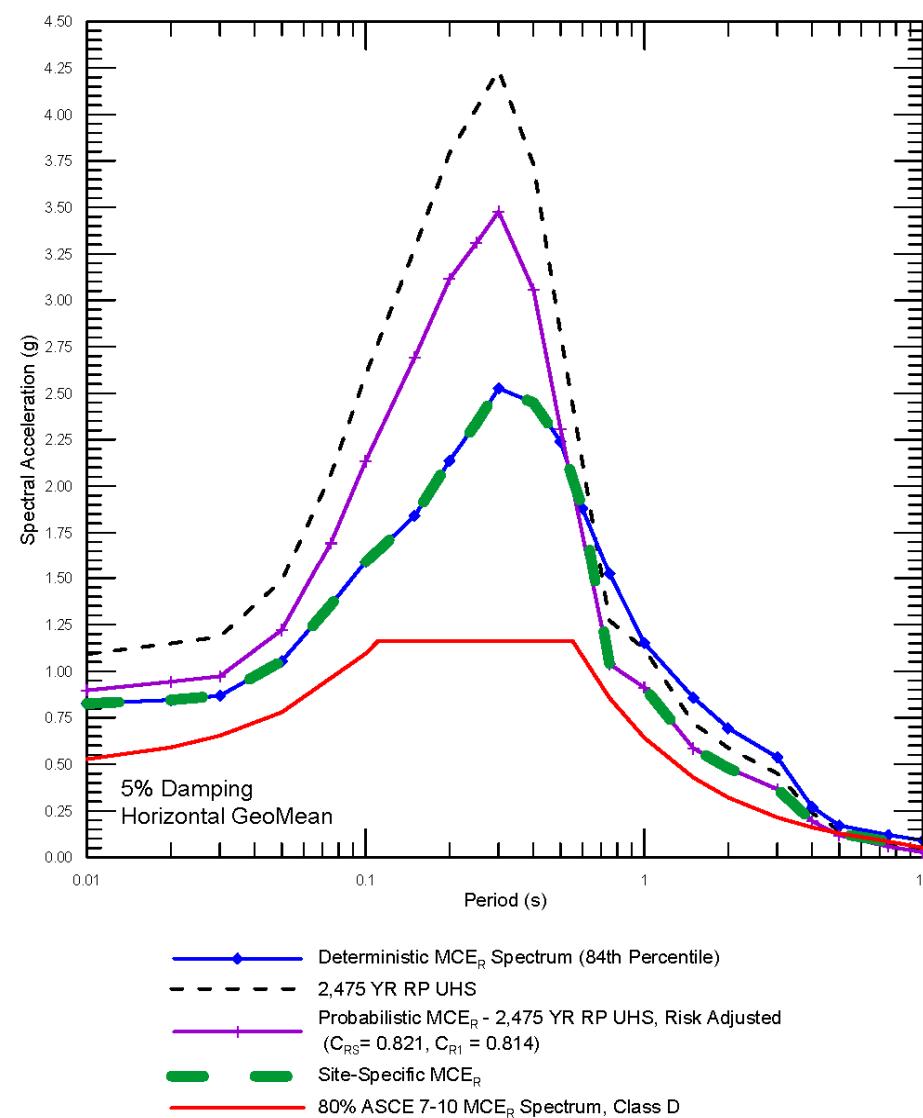
5%-Damped Deterministic Spectra Before and After Site Response Analysis



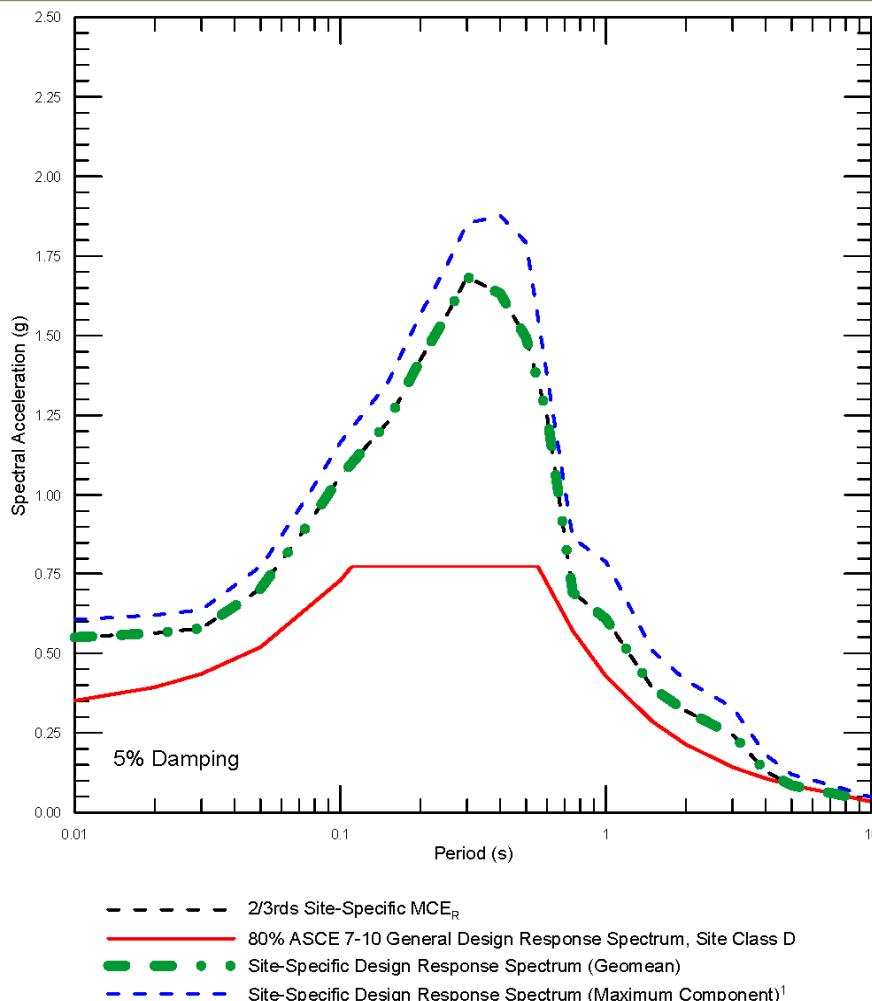
Deterministic MCE_R Spectrum Compared With ASCE 7-05 Lower Limit Deterministic MCE Spectrum



Site-Specific Horizontal MCE_R Spectrum

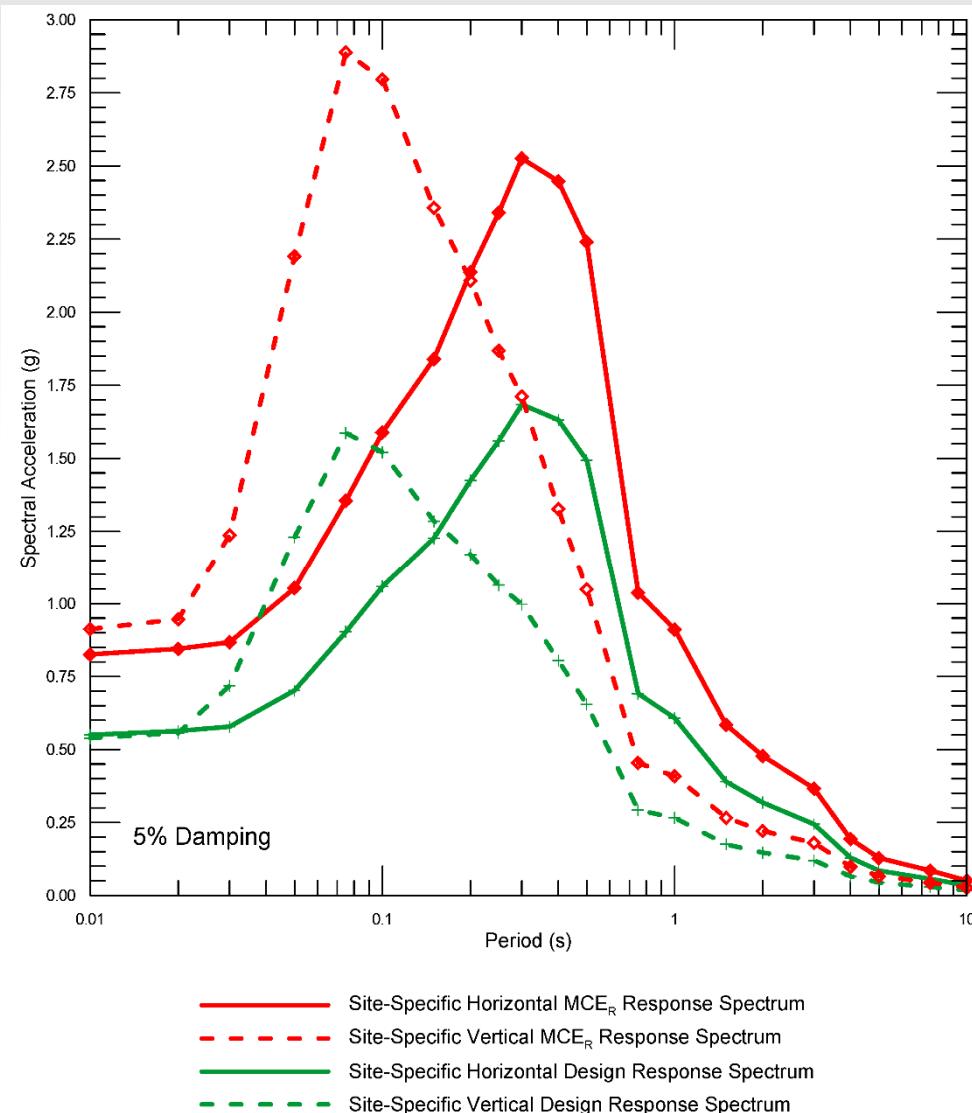


Site-Specific Horizontal Design Response Spectrum

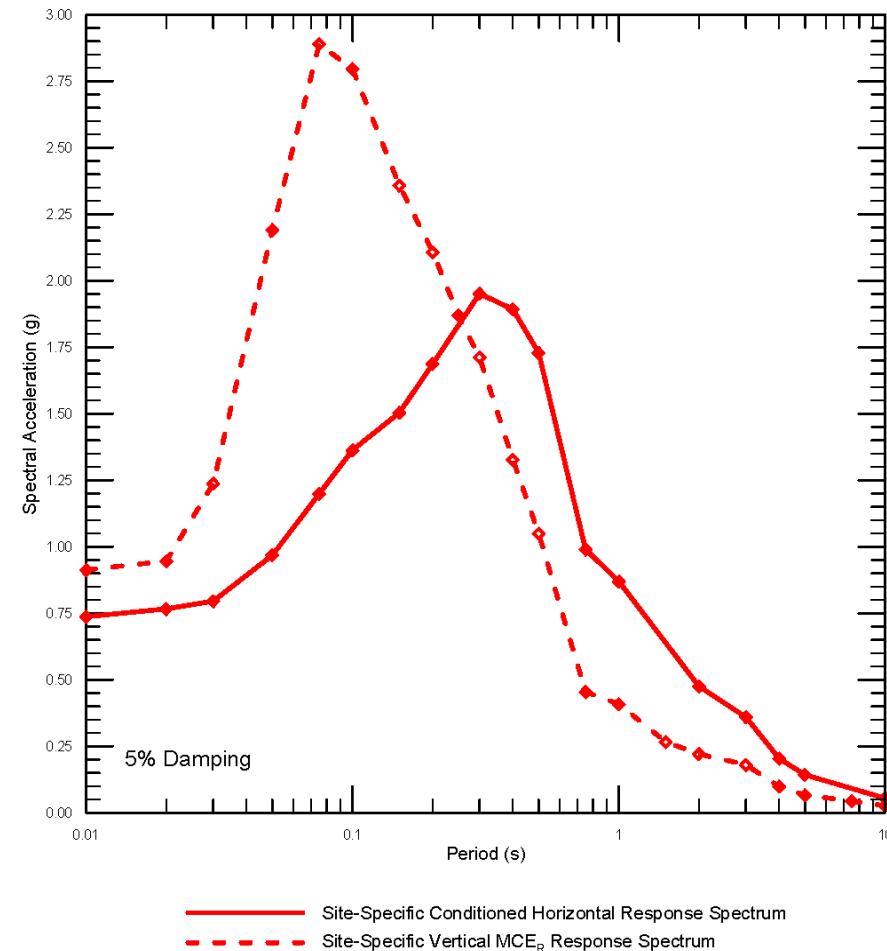


¹ For this project, the Design Response Spectrum is not being used for final design. Geometric mean horizontal Design Response Spectrum is provided for preliminary analyses. If the Design Response Spectrum is to be used for final design, the maximum direction horizontal Design Response Spectrum should be used.

Site-Specific Horizontal and Vertical MCE_R and Design Response Spectra



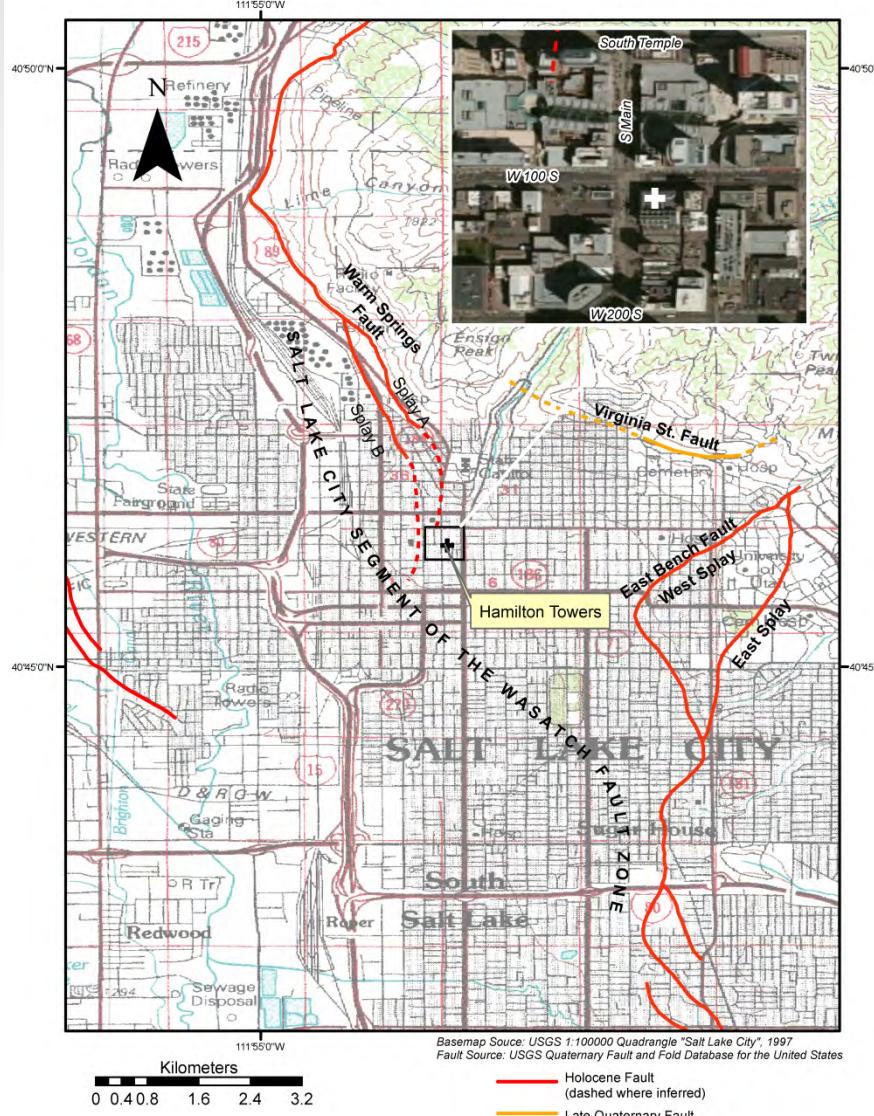
Site-Specific Conditional Horizontal and Vertical MCE_R Response Spectra



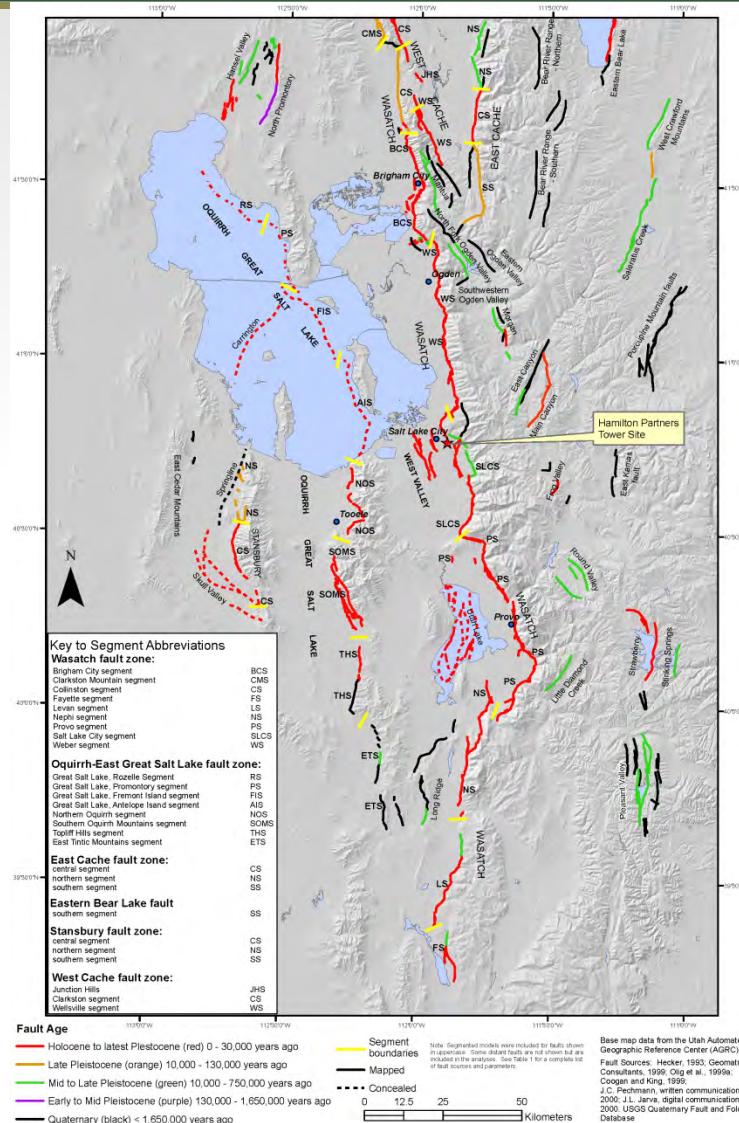
Summary

- There are still several issues that require additional data to improve site-specific seismic design in Salt Lake City and the Wasatch Front
- As previously described, those issues include the rupture behavior of the Salt Lake City segment, forward rupture directivity, and basin effects.
-

Active Faults Near the Site



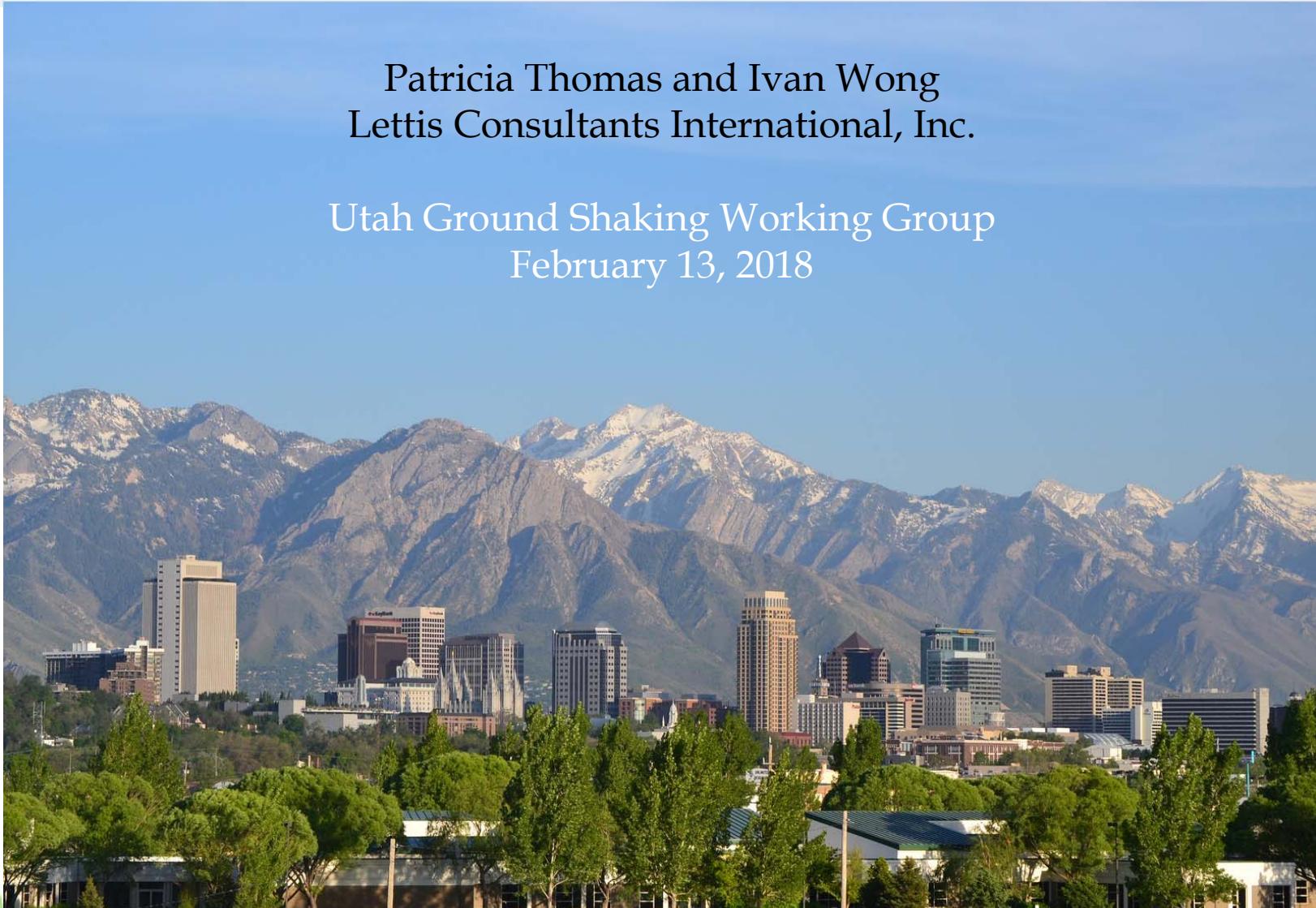
Selected Quaternary Fault Sources Included in the Hazard Analysis



The Impact on Seismic Hazard from Modeling the Time-Dependent Behavior of the Wasatch Fault

Patricia Thomas and Ivan Wong
Lettis Consultants International, Inc.

Utah Ground Shaking Working Group
February 13, 2018



WGUEP Members

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Bill Lund, UGS (Co-Chair)

Walter Arabasz, UUSS

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Mark Petersen, USGS

David Schwartz, USGS

Bob Smith, UU

Patricia Thomas, URS (now LCI)

Assistance from Steve Bowman, UGS and Rich Briggs, USGS

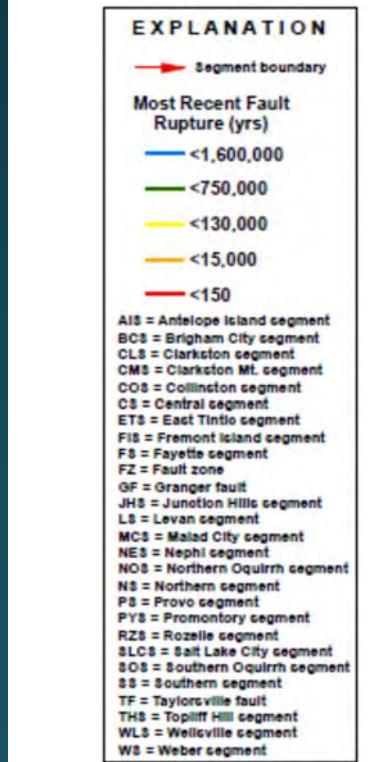


Implementation of the WGUEP Model for Time-Dependent Hazard Calculations

- WGUEP developed a seismic source model that includes the Wasatch and the Oquirrh-Great Salt Lake fault zones and 45 other faults/fault segments along with background seismicity in the Wasatch Front Region (39°N to 42.5°N , 110.75°W to 113.25°W).
- Time-independent rupture probabilities were calculated for individual faults, background earthquakes and the region for $M \geq 5$, 6.0 and 6.75 for a suite of time periods up to 100 years.
- Time-dependent probabilities were calculated for Wasatch and the Great Salt Lake fault zones where the data is available on the expected mean frequency of earthquakes and the elapsed time since the most recent large earthquake.
- Even for these faults, significant weight was given to the time-independent model.

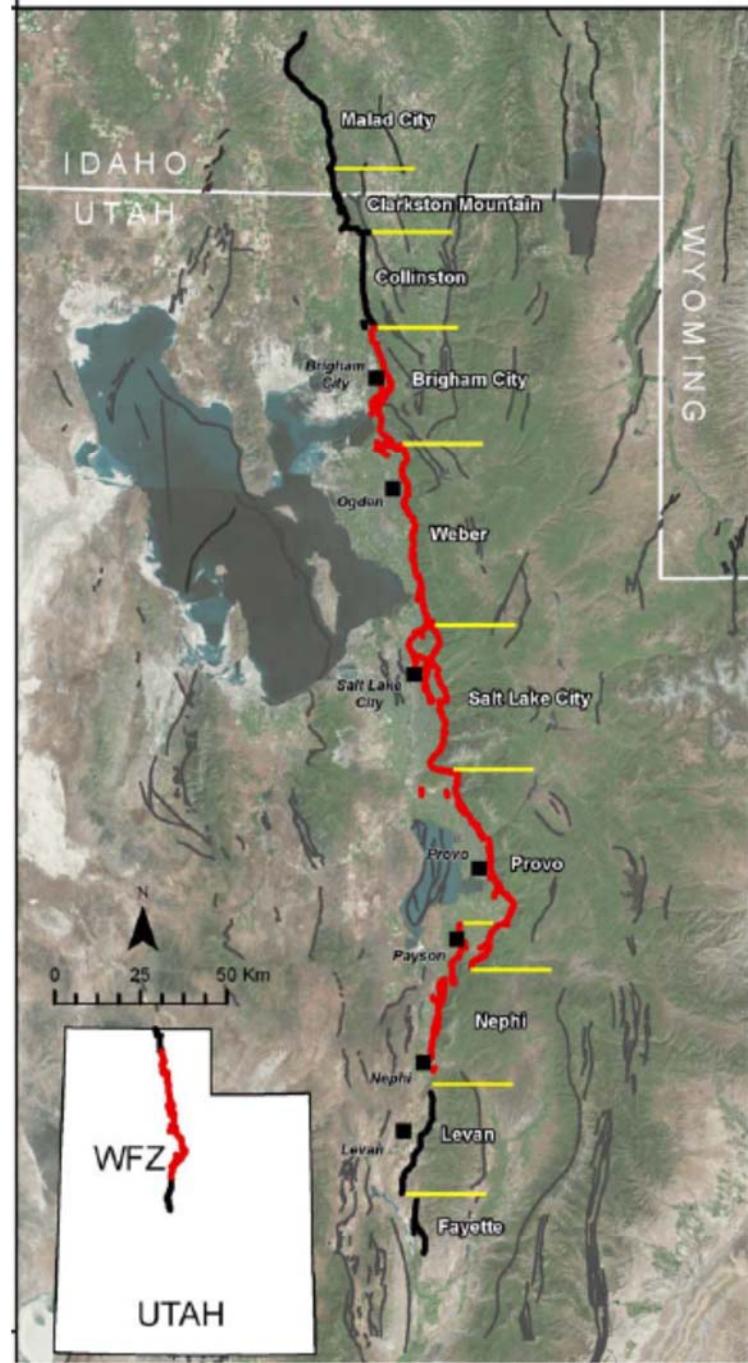
Quaternary Faults

- 47 faults included in the WGUEP model
- 6 segments with multiple rupture models
- 4 pairs of antithetic faults which can rupture simultaneously



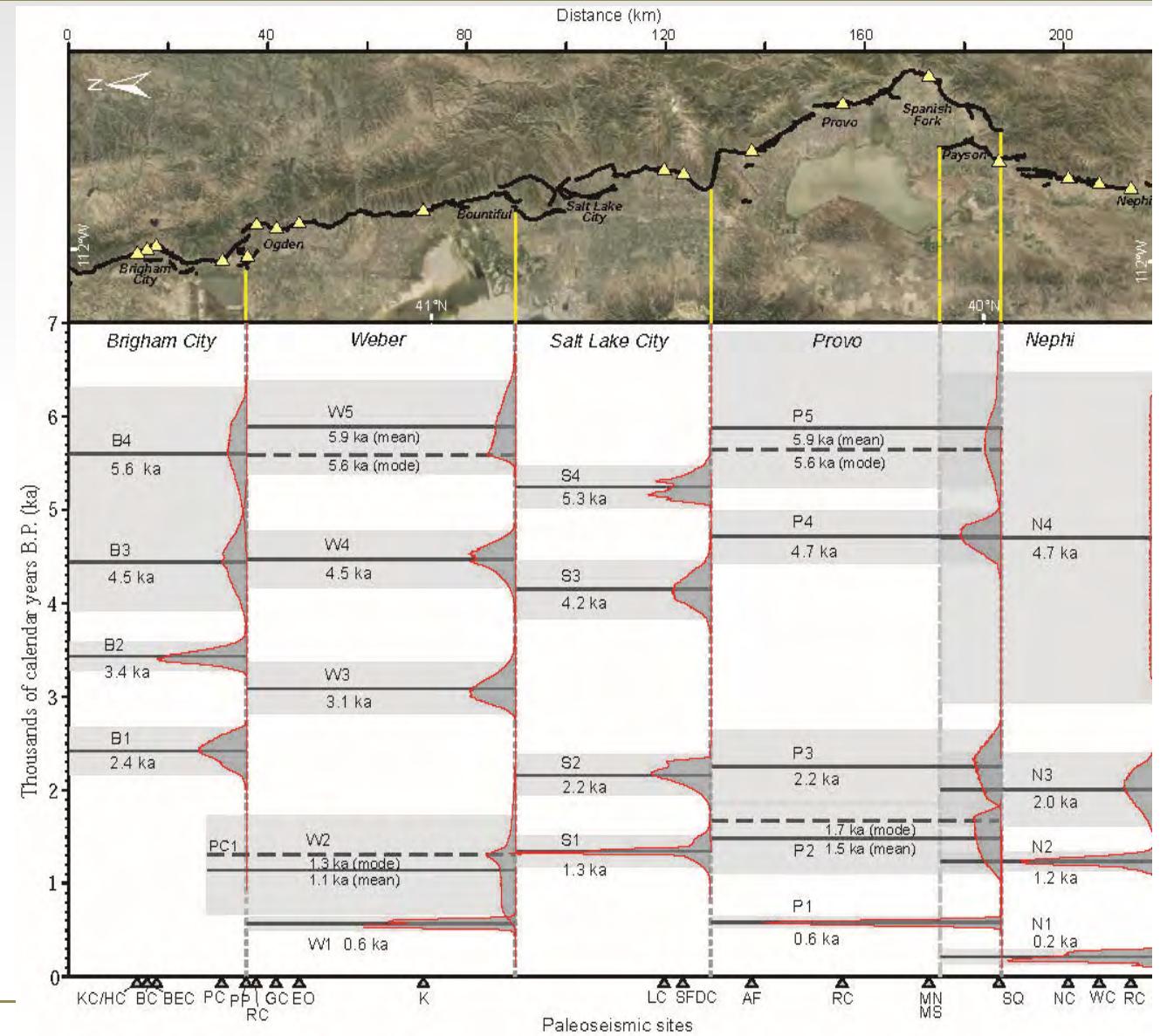
10 Segments of WFZ

- 5 Central Segments
 - Brigham City
 - Weber
 - Salt Lake City
 - Provo
 - Nehpi
- Higher slip rates
- Paleoseismic data from numerous trenching studies



Paleoseismic Data for Central WFZ

- 22 paleoseismic research sites along the central WFZ
- 4 – 5 events identified for each of the segments
- Rupture models developed based on earthquake chronologies and displacement estimates per segment

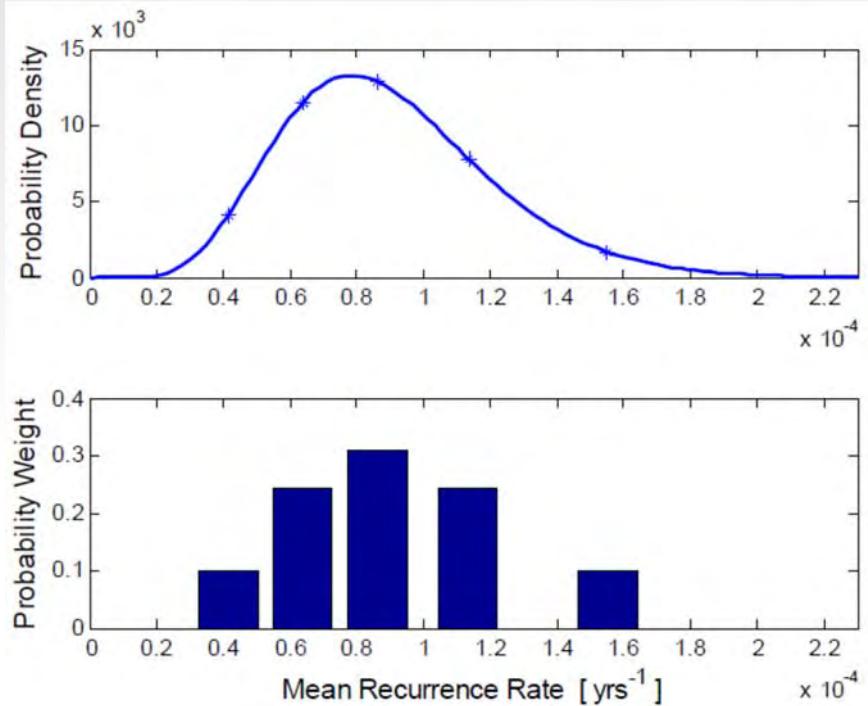


Central Wasatch Fault Zone Rupture Models

Rupture Model	Rupture Sources	Rupture Model Wt.	Earthquakes
SSR	B, W, S, P, N	0.7	22 SSR
Int. C	B, W, S, P, N, B+W	0.075	18 SSR, 2 MSR
Int. A	B, W, S, P, N, B+W, S+P	0.05	16 SSR, 3 MSR
Int. B	B, W, S, P, N, B+W, P+N	0.05	16, SSR, 3 MSR
MSR	B, W, S, P, N, B+W, W+S, S+P, P+N, S+P+N	0.025	7 SSR, 7 MSR
Unsegmented floating		0.1	

Recurrence Intervals

- Implemented the earthquake RI approach from CEUS-SSC report.
- The gamma distribution discretized into a five-point approximation.
- The method includes sample size uncertainty.
- Uncertainty in event timing found to be insignificant relative to sample size uncertainty.



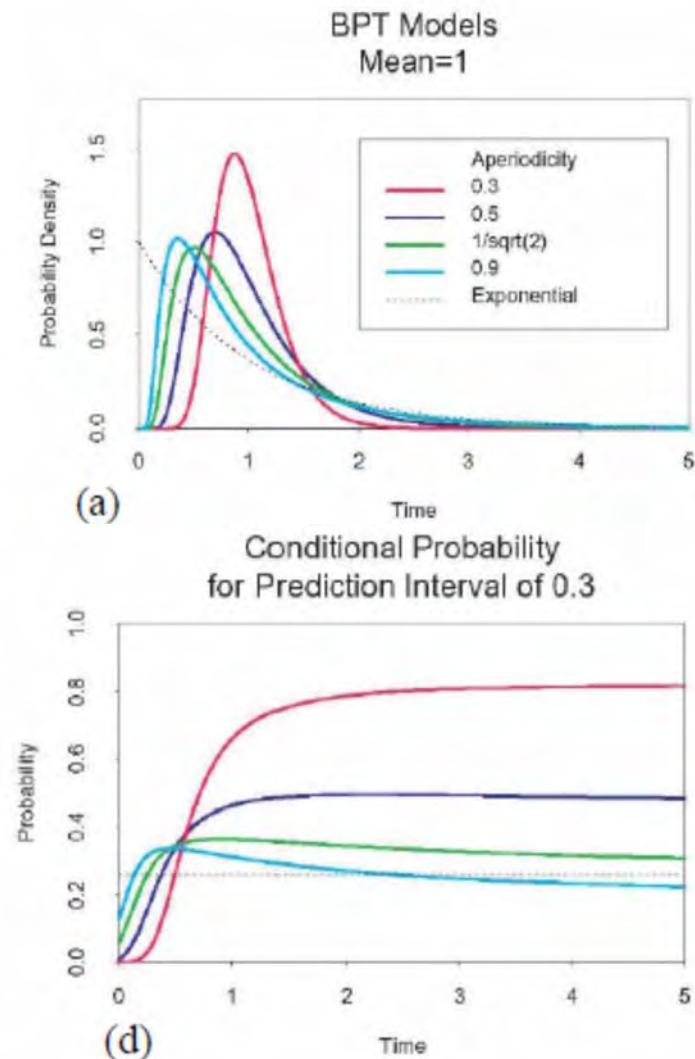
Segment	Wt. Mean Poisson RI
BCS	1500
WS	1427
SLCS	1331
PS	1235
NS	1080

Time Dependent Probability Model

- A time-dependent renewal process model embodies the expectation that after one earthquake on a fault, another earthquake is unlikely until sufficient time has elapsed for stress to gradually re-accumulate.
- The BPT model (Mathews et al., 2002) is one such model where stress increases from a ground state to a stress threshold.
- The BPT probability density function is given by:

$$f_{BPT}(t) = \sqrt{\frac{\mu}{2\pi a^2 t^3}} \exp\left\{-\frac{(t-\mu)^2}{2\mu a^2}\right\}$$

- The BPT model requires the mean recurrence interval, μ , and the aperiodicity or COV, a , as input parameters.
- The BPT process reaches a finite quasi-stationary state in which the failure rate is independent of elapsed time. After that point, conditional probabilities do not continue to increase.



Coefficient of Variation on Recurrence

- The standard deviation of inter-event RI divided by their mean is a measure of the periodicity of earthquakes on a fault.
- Smaller values of COV indicate more periodic recurrence and larger values indicate more random timing
- Based on the analysis of global dataset of repeating earthquakes (Ellsworth et al., 1999), WGCEP (2003, 2008) used a COV of 0.5 +/-0.2.
- While the data set for WFZ is small, the suitability of the global COV to the WFZ was tested by computing a composite COV for the central WFZ using grouped inter-event recurrence data.
- The composite COV is 0.5 +/-0.1 (2σ) with a minimum and maximum of about 0.3 to 0.7, supported the use of the range used by WGCEP based on the global data set.

Time-Dependent Rupture Probabilities, single-segment rupture model, $M \geq 6.75$

Segment	Wt. Mean Poisson RI (years)	Mean Elapsed Time Since Last Event (years)
BCS	1500	2491
WS	1427	626
SLCS	1331	1408
PS	1235	643
NS	1080	271

Fault Segment	50 Years	
	Poisson	BPT
Brigham City	3.2%	7.5%
Weber	3.5%	2.0%
Salt Lake City	3.6%	6.1%
Provo	4.0%	2.8%
Nephi	4.4%	0.5%

Sensitivity of Time-Dependent Rupture Probabilities to COV, single-segment rupture model, $M \geq 6.75$

Fault Segment	Poisson Probability	BPT, $\alpha = 0.3$			BPT, $\alpha = 0.5$			BPT, $\alpha = 0.7$		
		Probability	Lapse Time / Mean RI	Ratio of BPT to Poisson Probability	Probability	Lapse Time / Mean RI	Ratio of BPT to Poisson Probability	Probability	Lapse Time / Mean RI	Ratio of BPT to Poisson Probability
Brigham City	3.2%	14.9%	1.7	4.6	6.3%	1.5	2.0	3.7%	1.3	1.2
Weber	3.4%	1.1%	0.5	0.3	2.0%	0.4	0.6	2.6%	0.38	0.8
Salt Lake City	3.6%	10.3%	1.0	2.9	5.5%	0.9	1.5	3.7%	0.74	1.0
Provo	4.0%	1.7%	0.5	0.4	3.1%	0.5	0.8	3.2%	0.39	0.8
Nephi	4.4%	<0.1%	0.3	0.007	0.48%	0.3	0.1	1.0%	0.21	0.2

Equivalent-Poisson Rupture Rates

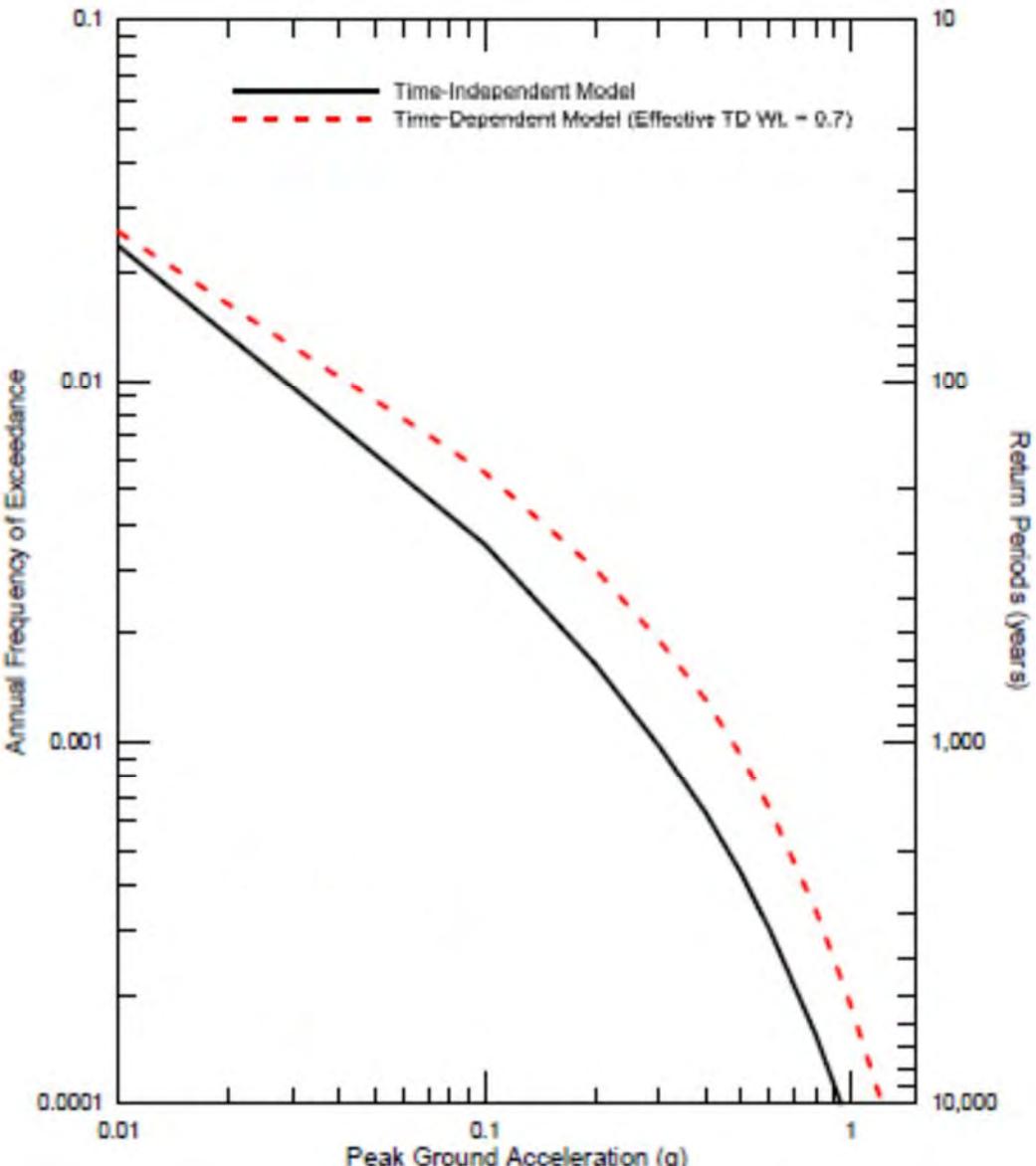
- Equivalent-Poisson rupture rates can be back calculated from the BPT rupture probabilities for a specified time interval and used in a PSHA to compute time-dependent hazard.

Segment	Wt. Mean Time-Independent Poisson RI (years)	Wt. Mean Time-Dependent Equivalent Poisson RI (years)
BCS	1500	535
WS	1427	2408
SLCS	1331	707
PS	1235	1510
NS	1080	6065

- Equivalent-Poisson RI for BCS and SLCS significantly lower than time-independent Poisson rates

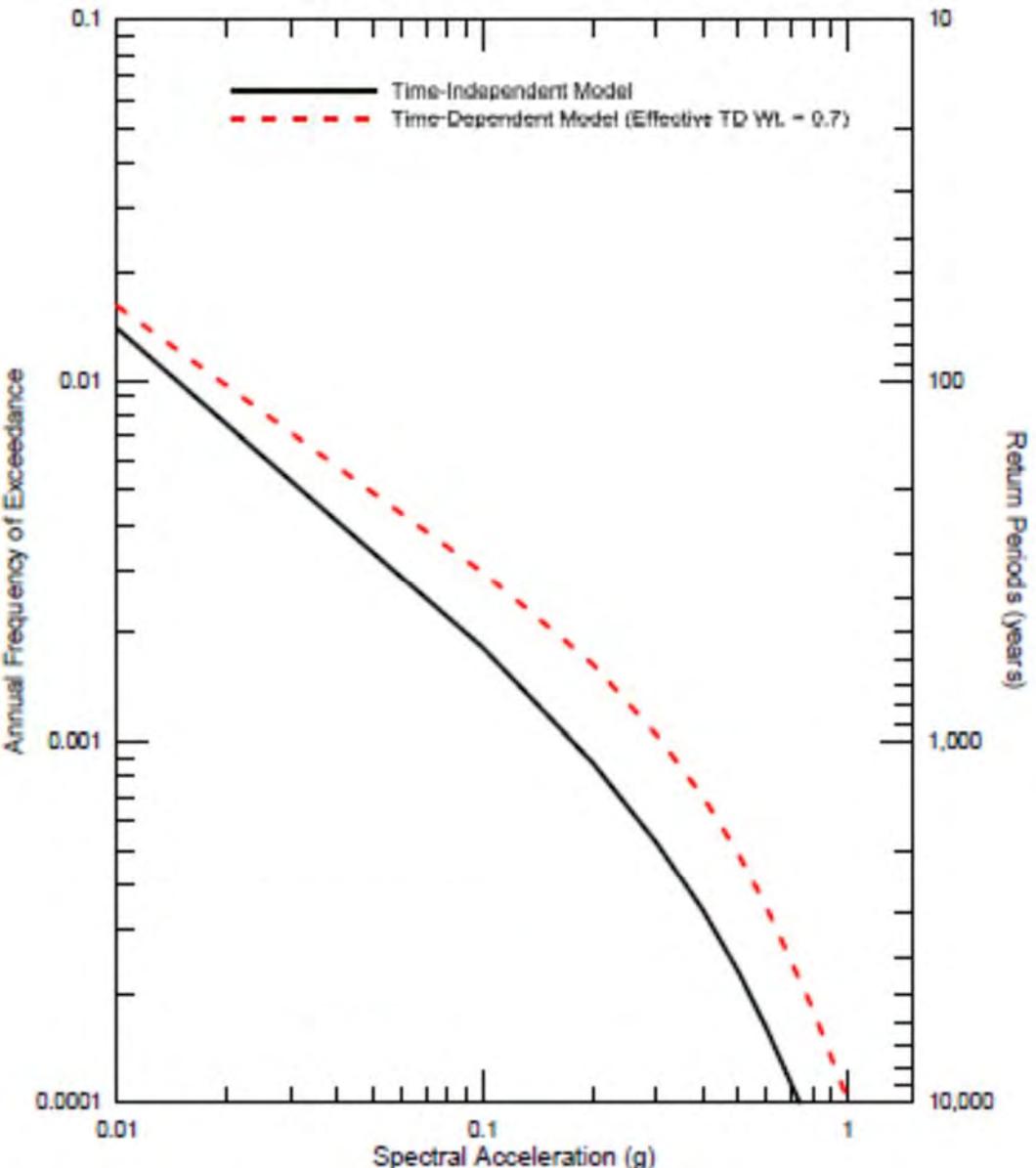
Brigham City, Utah

- 2,475-yr Return Period PGA
 TI: 0.52 g
 TD: 0.74 g
- $V_s30 = 760$ m/sec
- NGA-West2 GMM



Brigham City, Utah

- 2,475-yr Return Period 1.0 sec SA
 TI: 0.36 g
 TD: 0.55 g
- $V_s 30 = 760$ m/sec
- NGA-West2 GMM

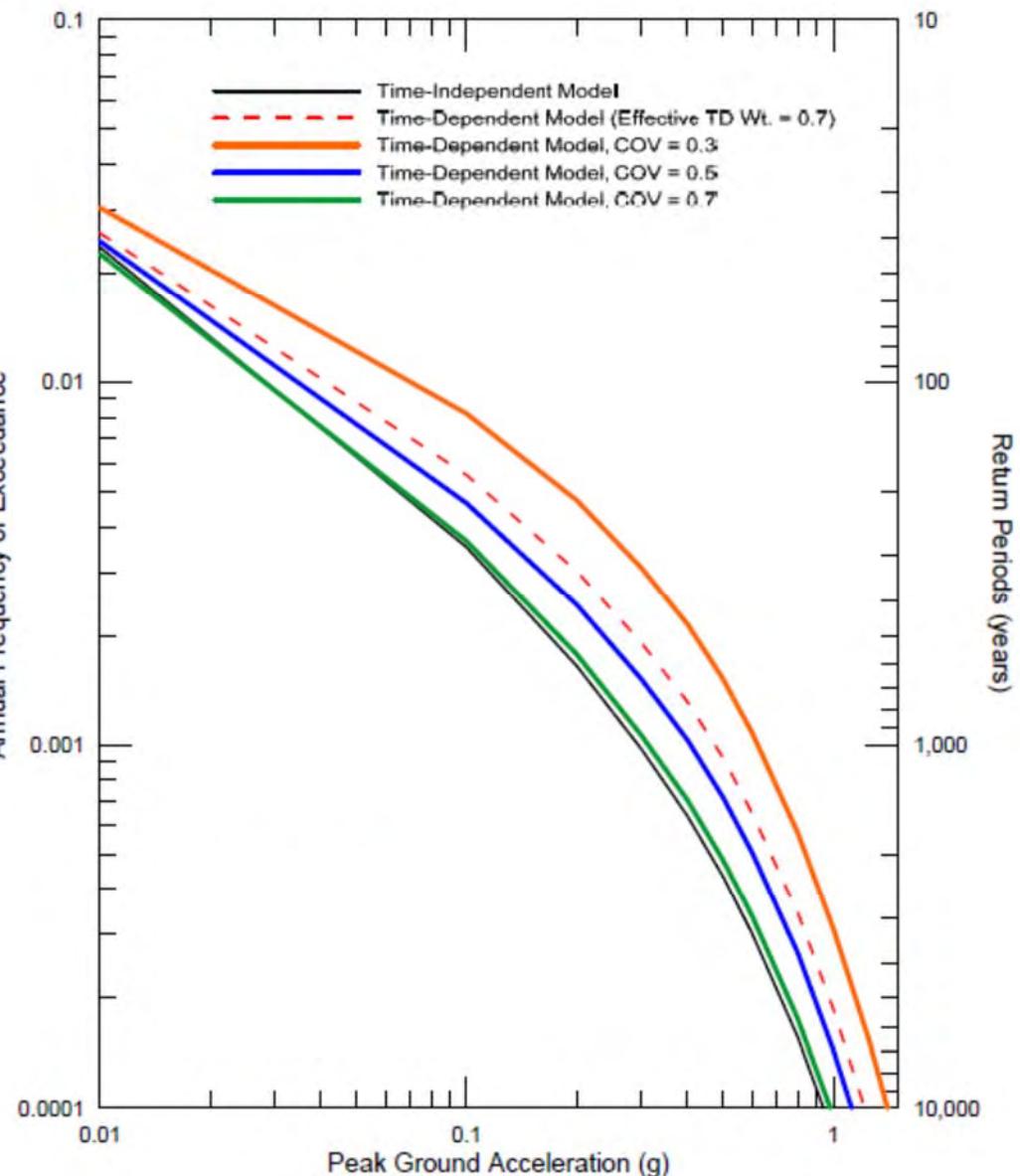


Brigham City, Utah

- 2,475-yr Return Period 1.0 sec SA

TI: 0.52 g

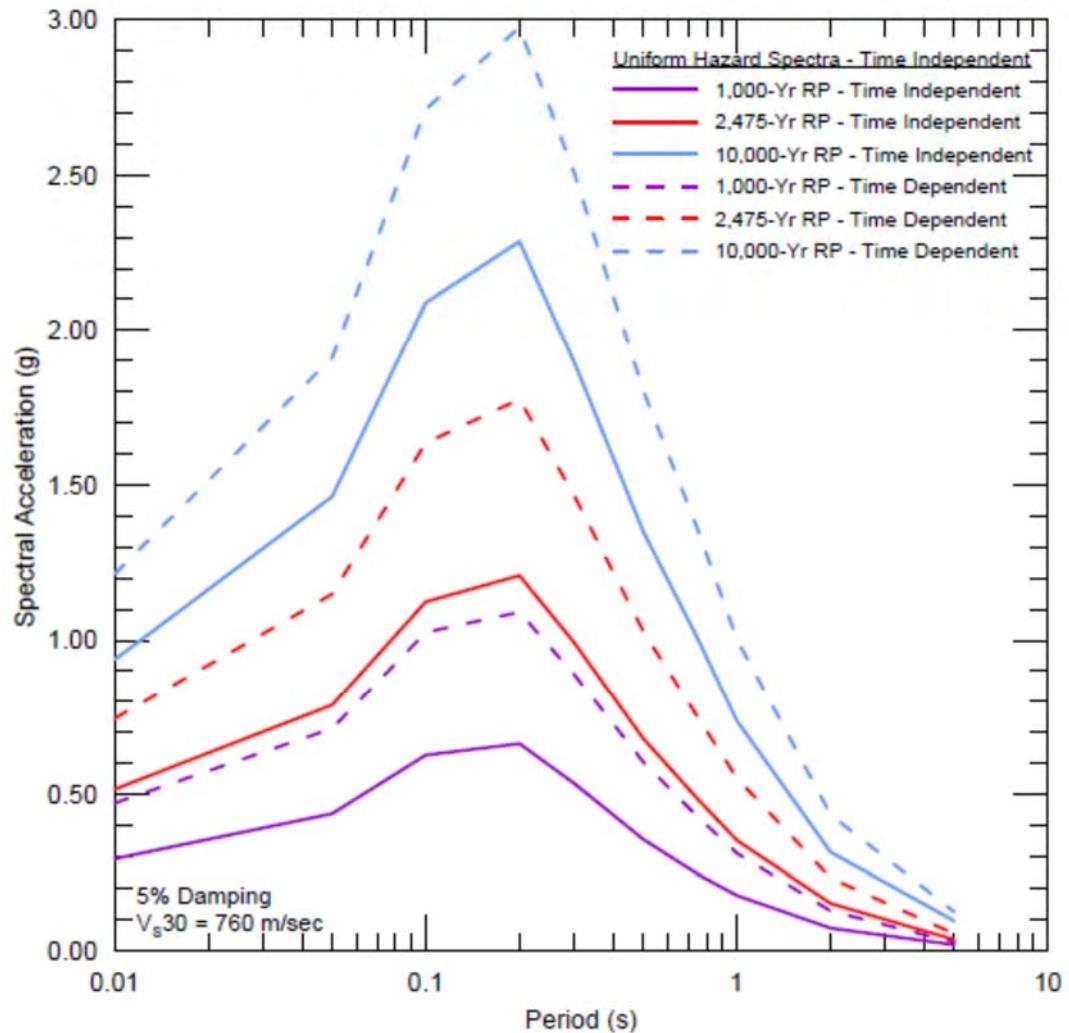
TD, COV=0.3: 0.91 g
TD, COV=0.5: 0.66 g
TD, COV=0.7: 0.55 g



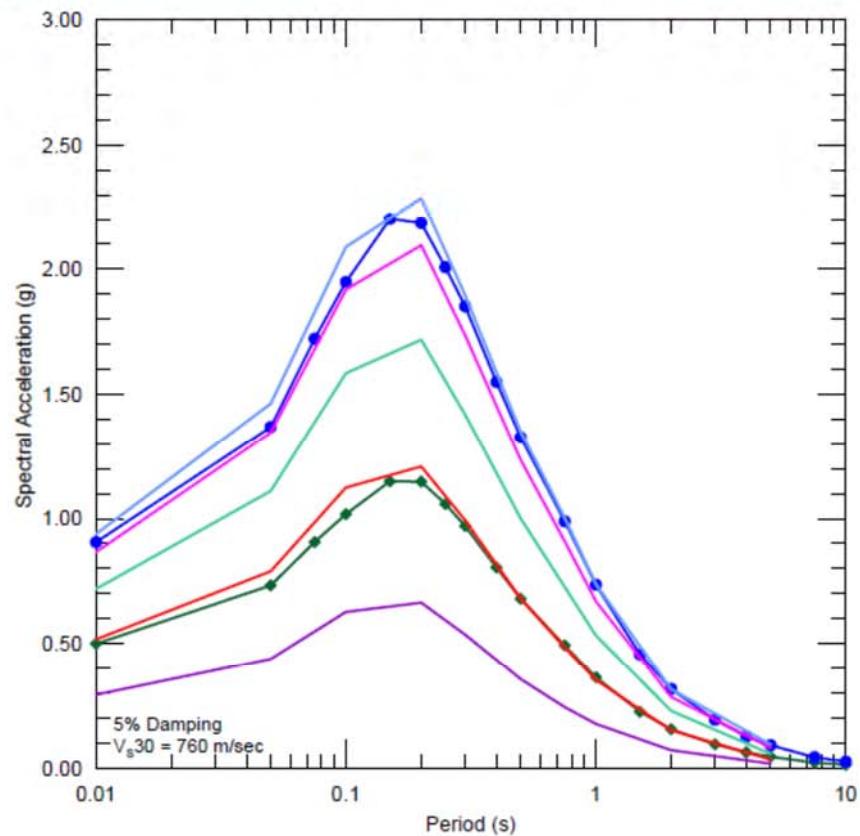
Brigham City, Utah

- 2,475-yr Return Period UHS

Time-Dependent UHS is 45-55% larger than Time-Independent



Comparison of Deterministic Spectrum with UHS - Brigham City Site

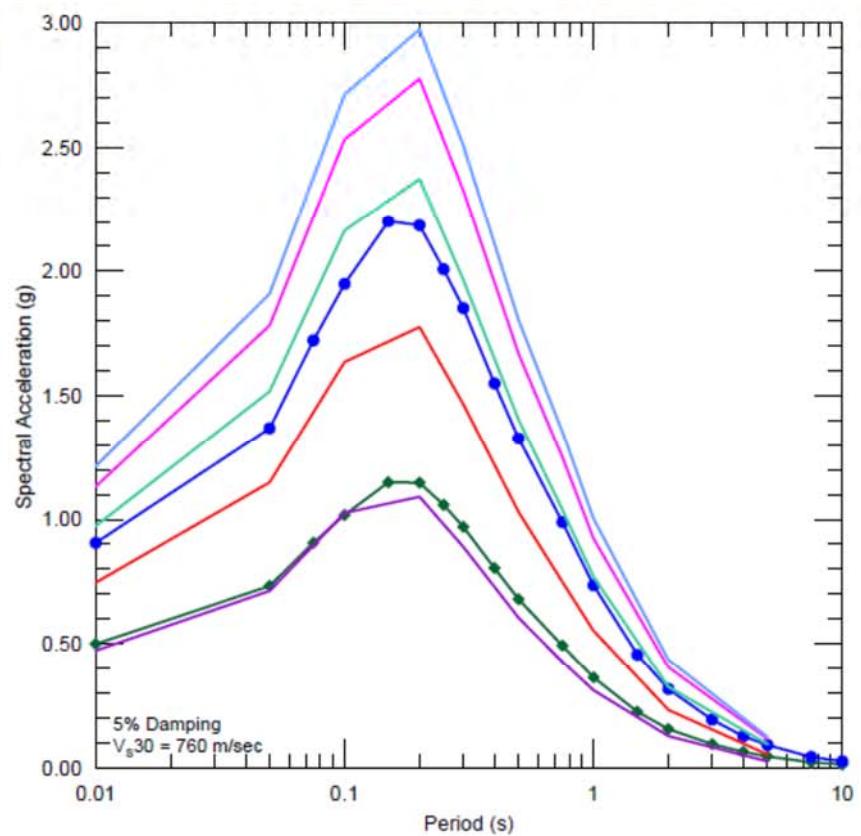


Uniform Hazard Spectra - Time Independent

- 1,000-Year Return Period
- 2,475-Year Return Period
- 5,000-Year Return Period
- 8,000-Year Return Period
- 10,000-Year Return Period

84th Percentile Deterministic Spectra

- Median, M 7.1 Wasatch Event
- 84th Percentile, M 7.1 Wasatch Event

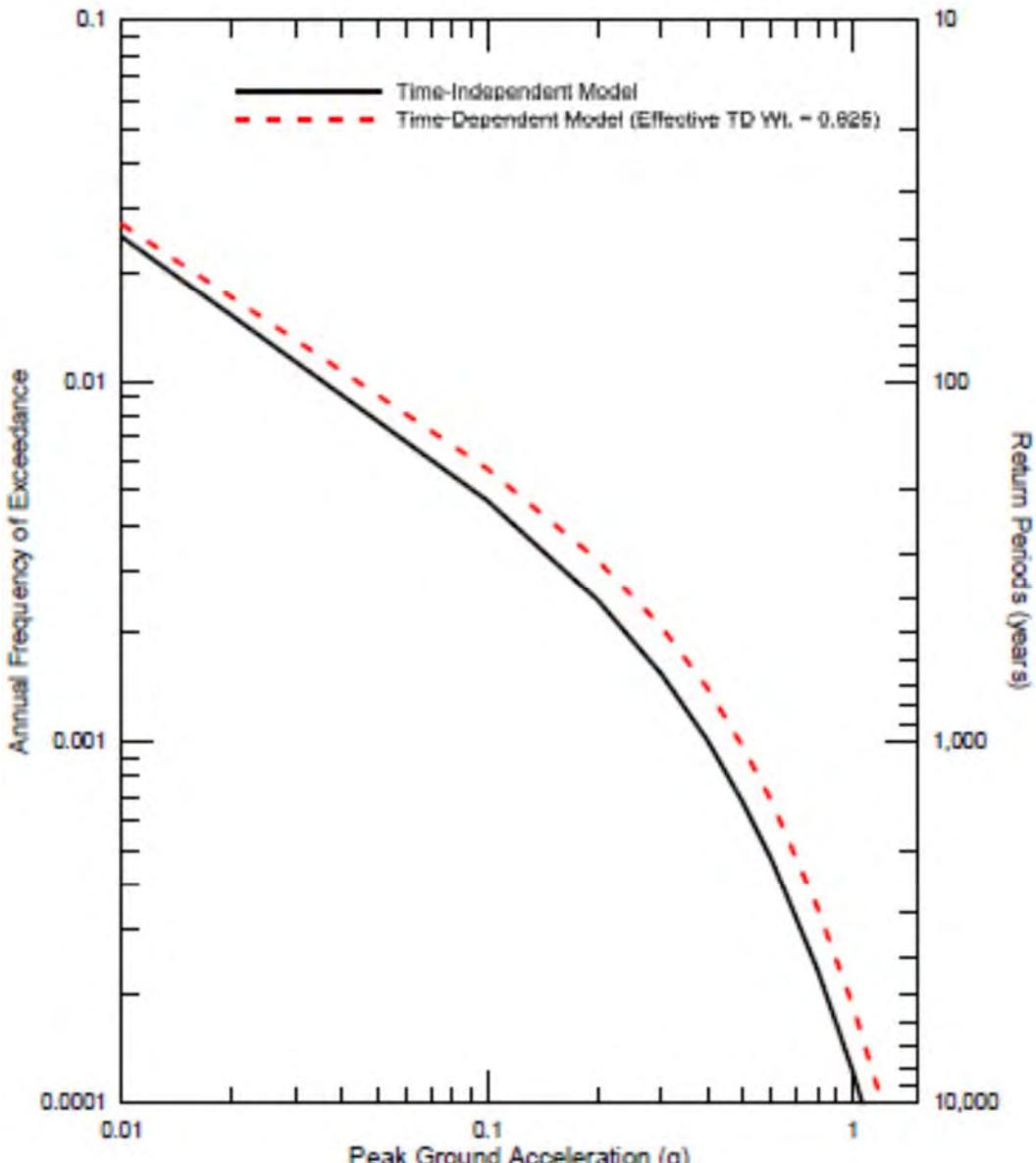


Uniform Hazard Spectra - Time Dependent

- 1,000-Year Return Period
- 2,475-Year Return Period
- 5,000-Year Return Period
- 8,000-Year Return Period
- 10,000-Year Return Period

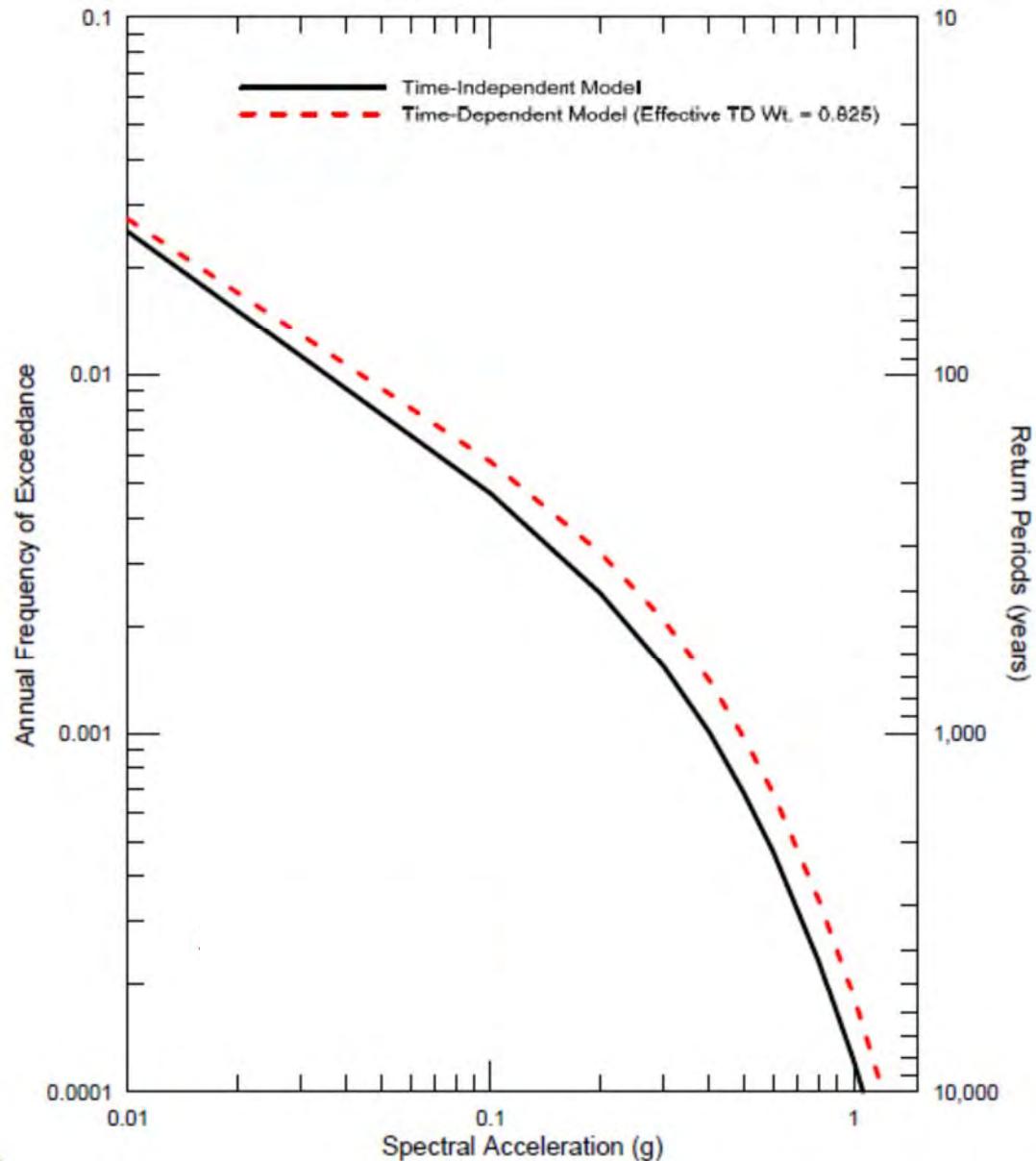
Salt Lake City, Utah

- 2,475-yr Return Period PGA
 TI: 0.64 g
 TD: 0.75 g
- $V_s30 = 760$ m/sec
- NGA-West2 GMM



Salt Lake City, Utah

- 2,475-yr Return Period 1.0 Sec SA
 TI: 0.46 g
 TD: 0.56 g
- $V_s 30 = 760$ m/sec
- NGA-West2 GMM

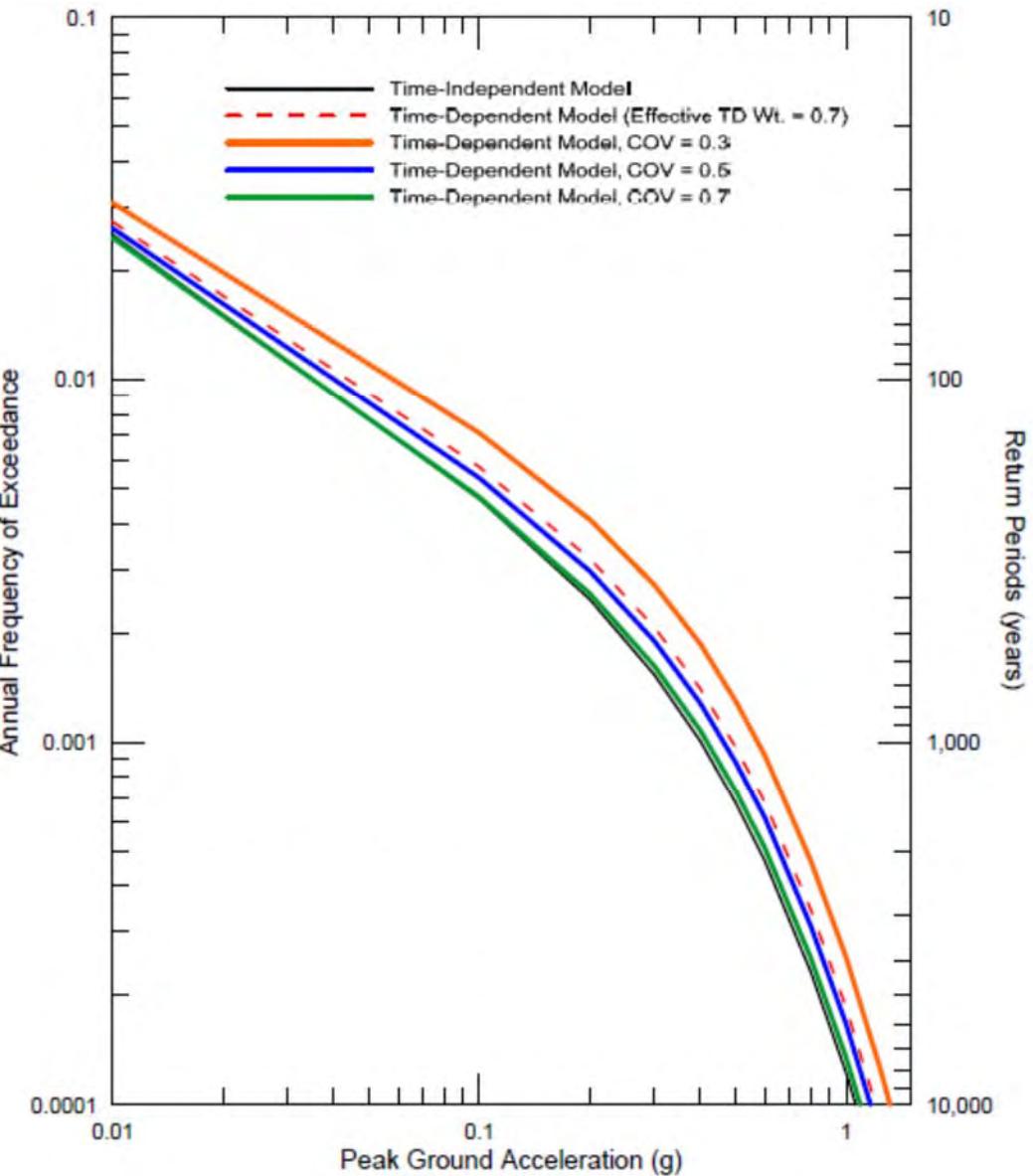


Salt Lake City, Utah

- 2,475-yr Return Period 1.0 sec SA

TI: 0.64 g

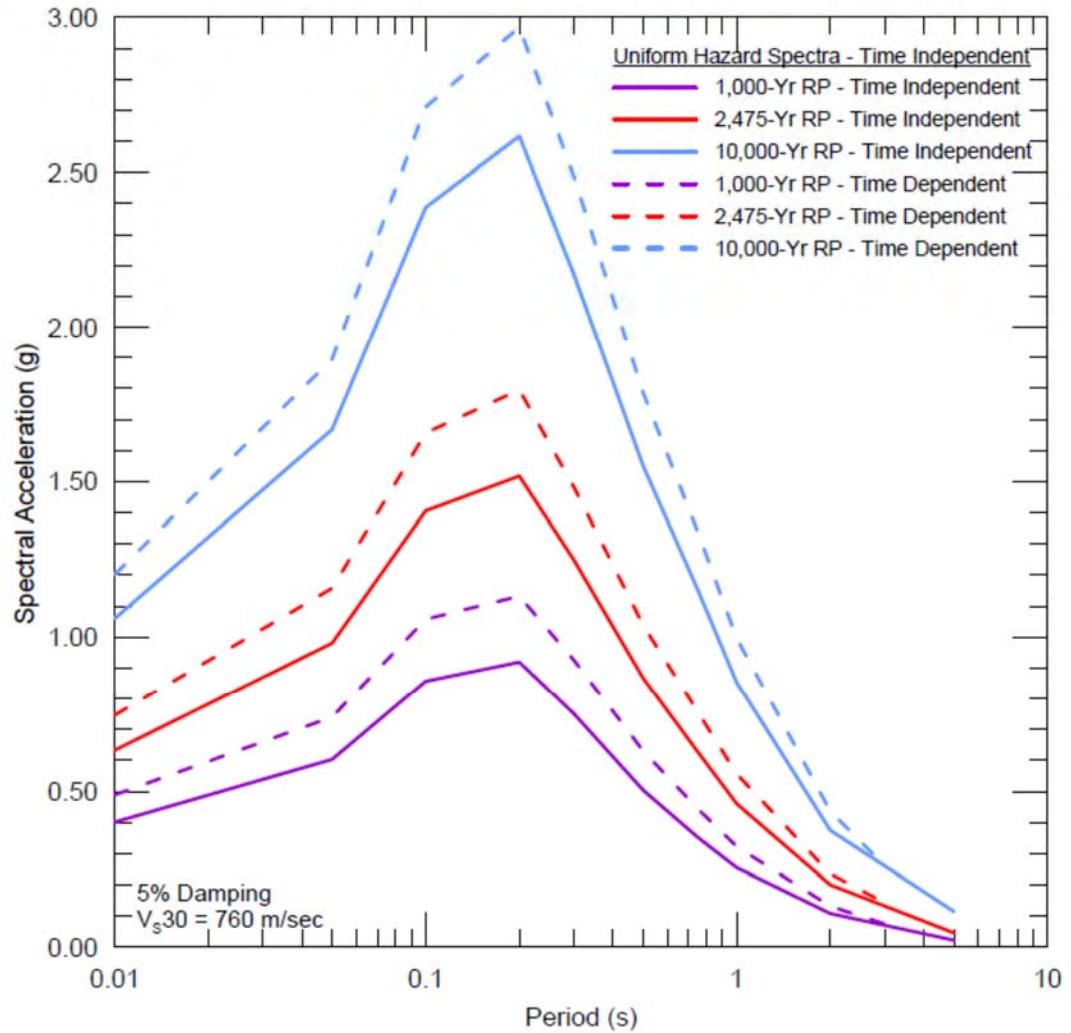
TD, COV=0.3: 0.85 g
TD, COV=0.5: 0.72 g
TD, COV=0.7: 0.66 g



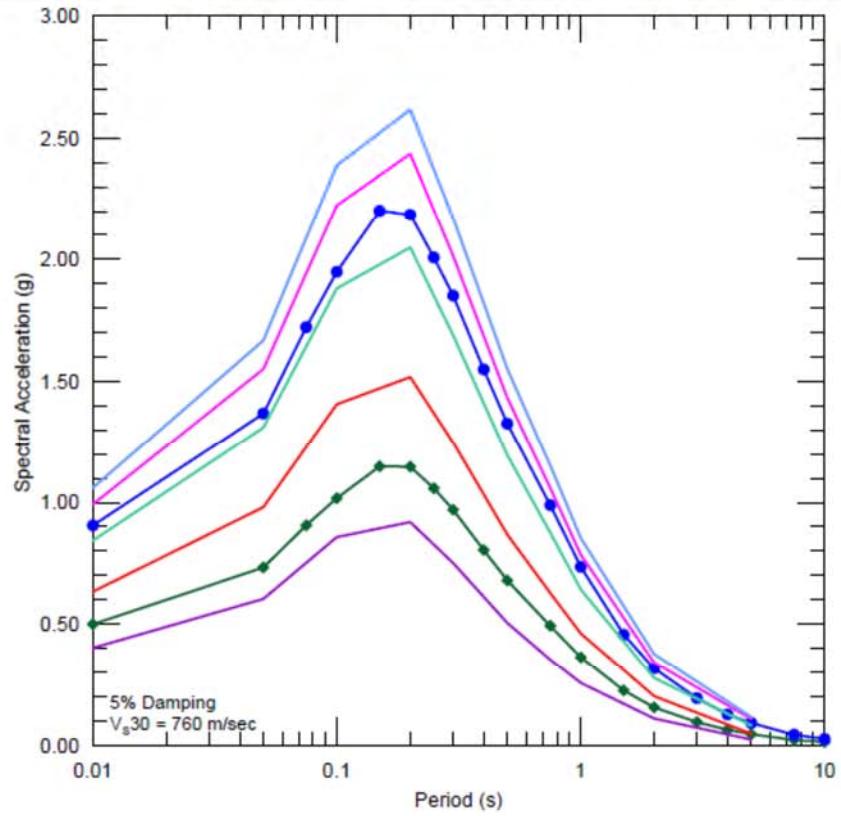
Salt Lake City, Utah

- 2,475-yr Return Period UHS

Time-Dependent UHS is 18-21% larger than Time-Independent



Comparison of Deterministic Spectrum with UHS - Salt Lake City Site

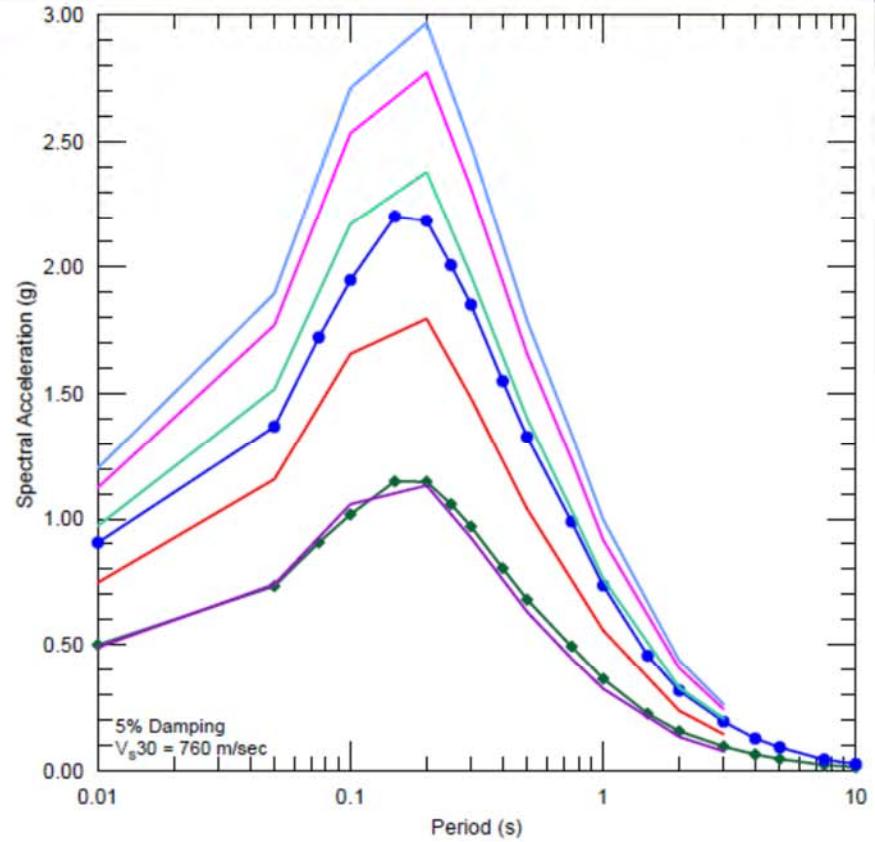


Uniform Hazard Spectra - Time Independent

- 1,000-Year Return Period
- 2,475-Year Return Period
- 5,000-Year Return Period
- 8,000-Year Return Period
- 10,000-Year Return Period

84th Percentile Deterministic Spectra

- Median, M 7.1 Wasatch Event
- 84th Percentile, M 7.1 Wasatch Event

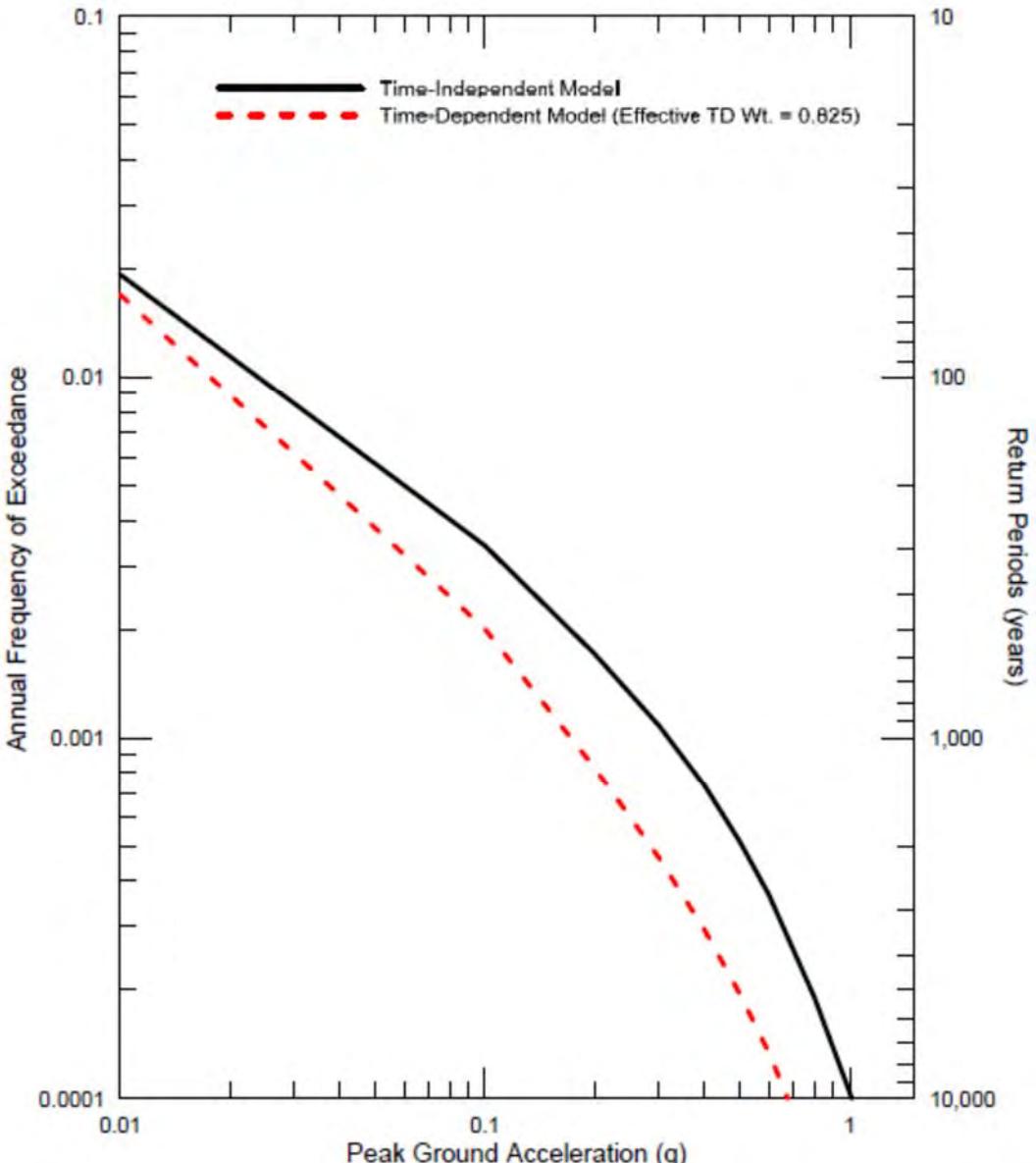


Uniform Hazard Spectra - Time Dependent

- 1,000-Year Return Period
- 2,475-Year Return Period
- 5,000-Year Return Period
- 8,000-Year Return Period
- 10,000-Year Return Period

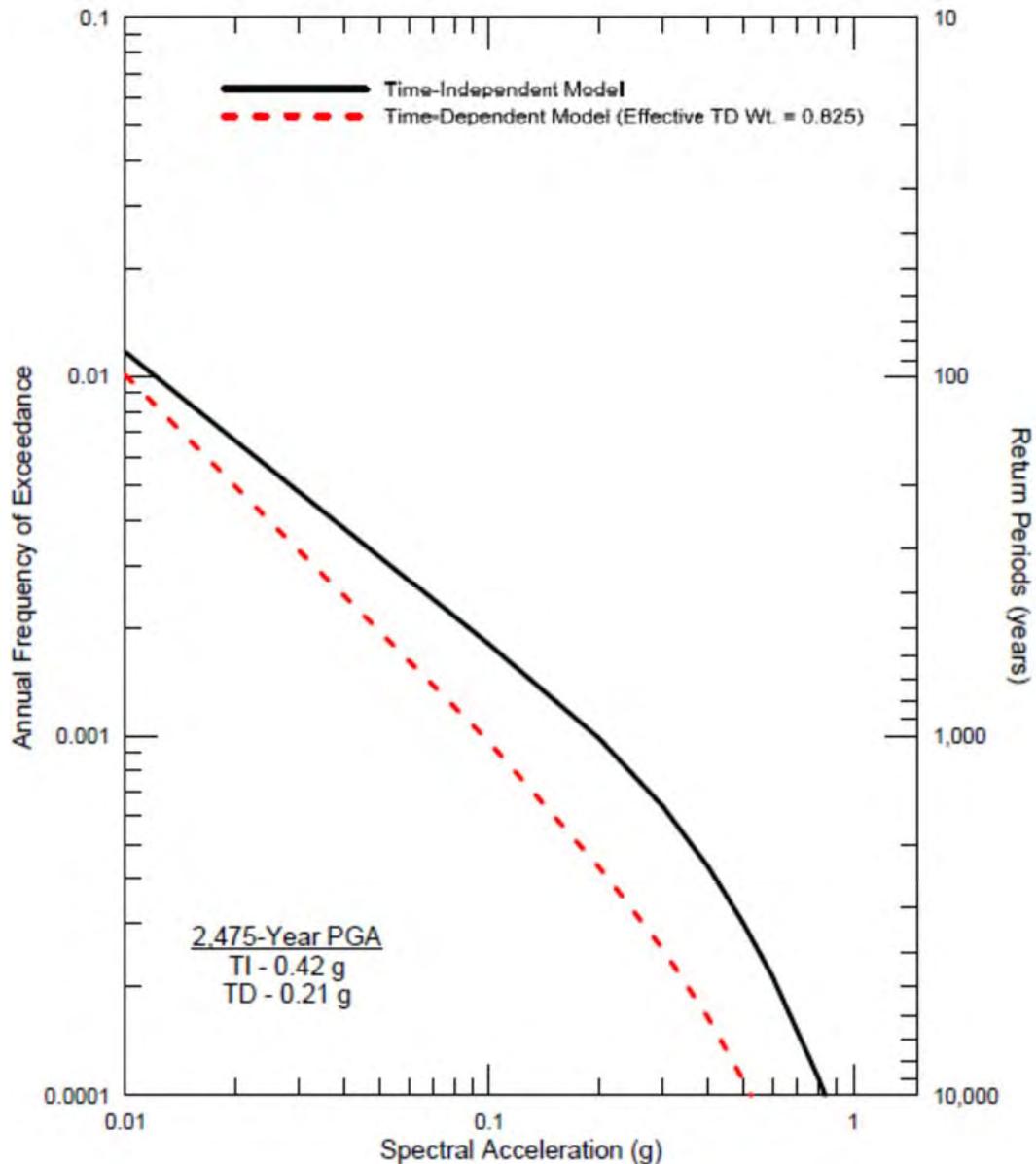
Nephi, Utah

- 2,475-yr Return Period PGA
TI: 0.57 g
TD: 0.33 g
- $V_s30 = 760$ m/sec
- NGA-West2 GMM



Nephi, Utah

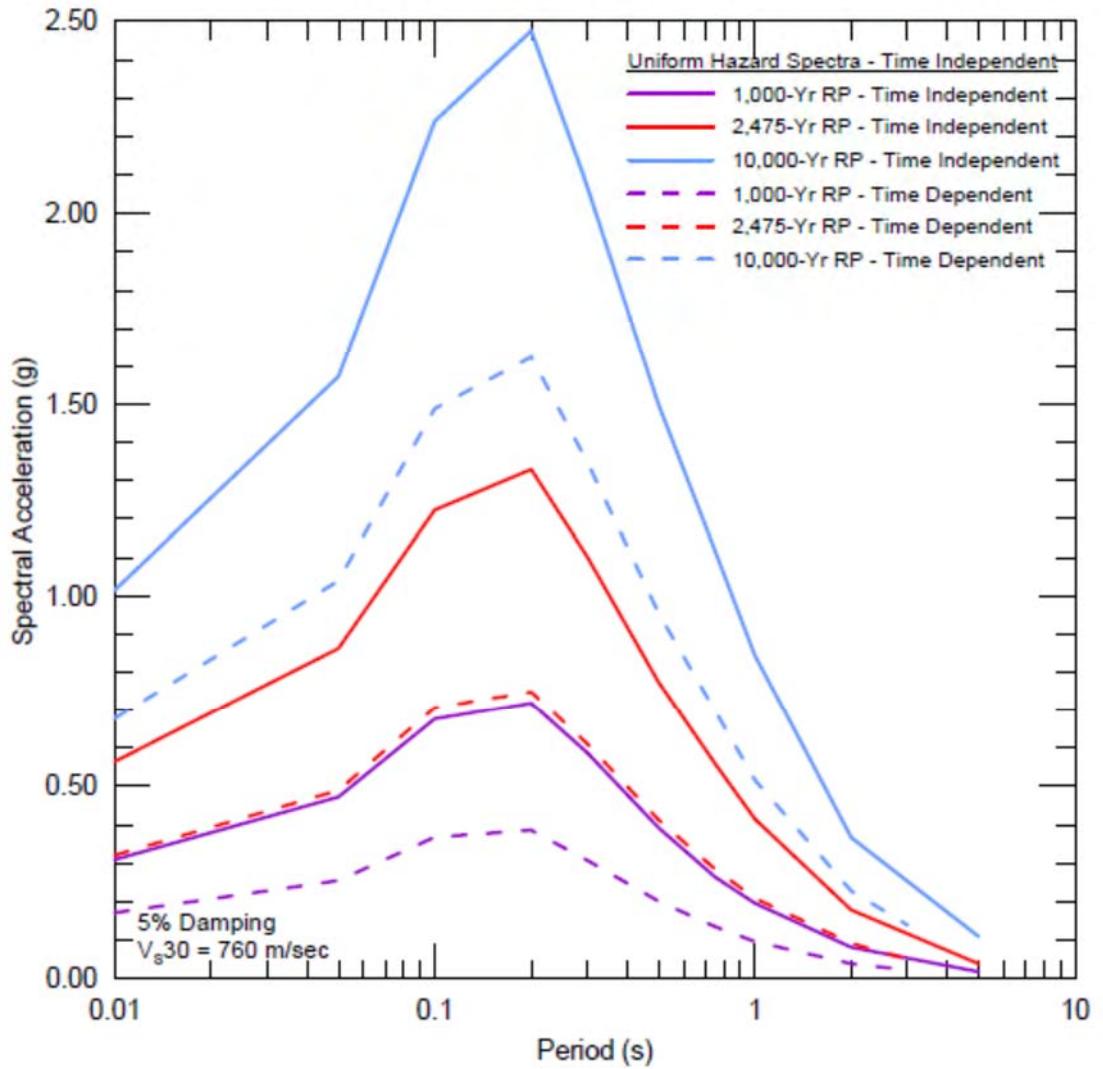
- 2,475-yr Return Period 1.0 sec SA
TI: 0.42 g
TD: 0.21 g
- $V_s 30 = 760$ m/sec
- NGA-West2 GMM



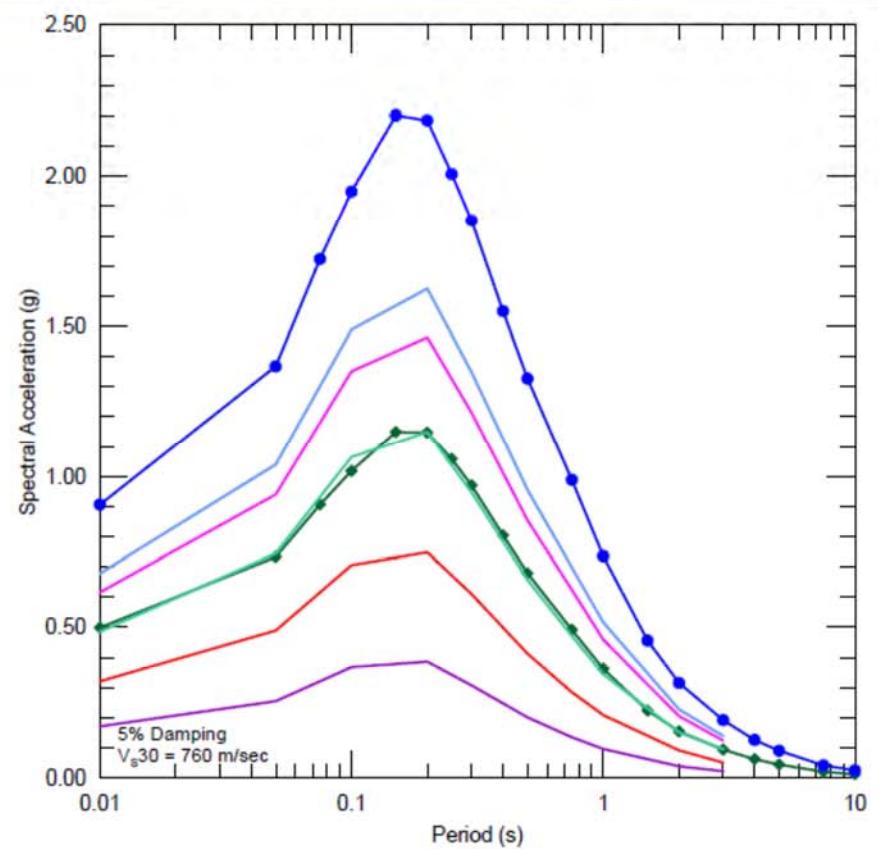
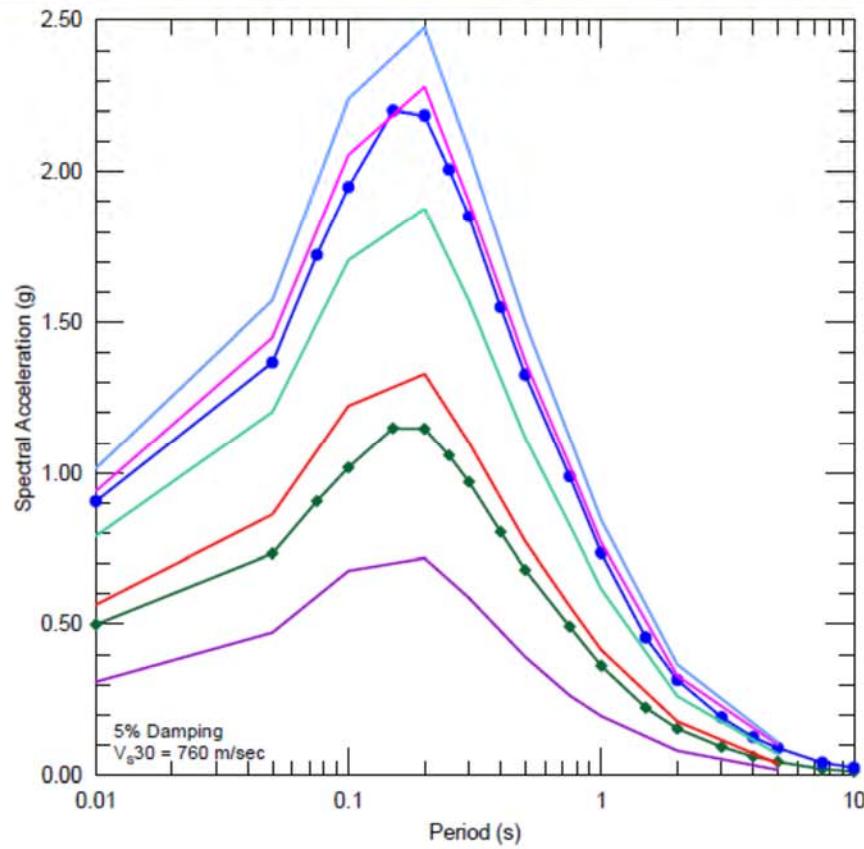
Nephi, Utah

- 2,475-yr Return Period UHS

Time-Dependent UHS is 43-50% smaller than Time-Independent



Comparison of Deterministic Spectrum with UHS - Nephi Site



Conclusions

- Comparison of the time-dependent and time-independent hazard at three cities along the Wasatch Front show significant differences at a 2475-yr return period.
- These differences are due primarily to how the elapsed time since the MRE compares to the average recurrence intervals of the rupture scenarios particularly the single segment ruptures.
- Note that because there is a time-independent component in the time-dependent recurrence intervals, the time-dependent hazard estimates have large uncertainties.
- However, even given those uncertainties, the time-dependent hazard estimates need to be given strong consideration in structural design and safety analyses.



Thank You. Questions?

